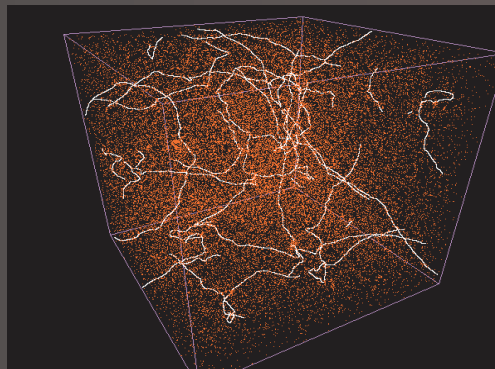


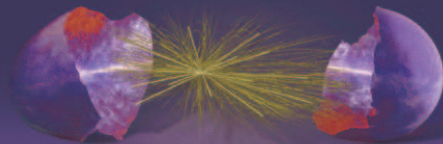
recent developments on cosmic string dynamics



mairí sakellariadou



king's college
london



PASCOS 2011

3-8 July 2011, Cambridge UK
Centre for Theoretical Cosmology

17th
International
Symposium on
Particles
Strings and
Cosmology

outline

- cosmic string evolution in a FLRW background

- numerical results

ringeval, m.s., bouchet JCAP 0702 (2007) 023

- analytical model

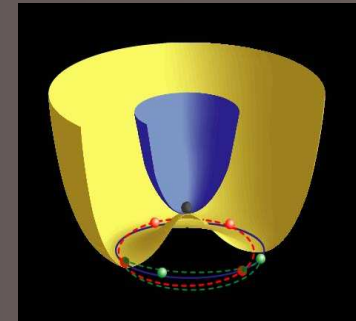
lorenz, ringeval, m.s. JCAP 1010 (2010) 003

- cosmic string evolution in an anisotropic background

kunze, m.s. arXiv:1106.4434

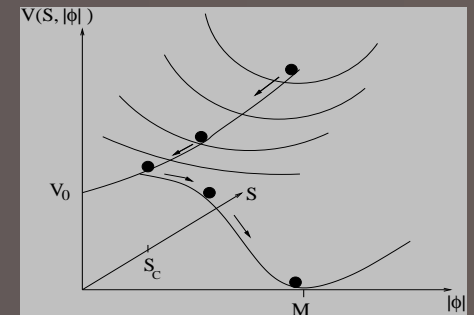
formation

kibble-zurek mechanism



generically formed at the end of F- or D-term
inflation within SUSY GUTs

$$G_{\text{GUT}} \xrightarrow{M_{\text{GUT}}} H_1 \xrightarrow[M_{\text{infl}}]{\Phi_+ \Phi_-} H_2 \longrightarrow G_{\text{GM}}$$



$$G_{\text{GUT}} \times U(1) \xrightarrow{M_{\text{GUT}}} H \times U(1) \xrightarrow[M_{\text{infl}}]{\Phi_+ \Phi_-} H \longrightarrow G_{\text{GM}}$$

jeannerot, m.s., rocher PRD 68 (2003) 103514

evolution (NG cosmic string code)

- FLRW
- fixed unity comoving volume with periodic b.c.
- initial scale factor is normalised to unity
- initial horizon size is a free parameter
- comoving horizon size grows and evolution is stopped before it fills the whole unit volume
- VV initial conditions

evolution

- FLRW
- fixed unity comoving volume with periodic b.c.
- initial scale factor normalised to unity
- initial horizon size is a free parameter
- comoving horizon size grows and evolution is stopped before it fills the whole unit volume
- VV initial conditions

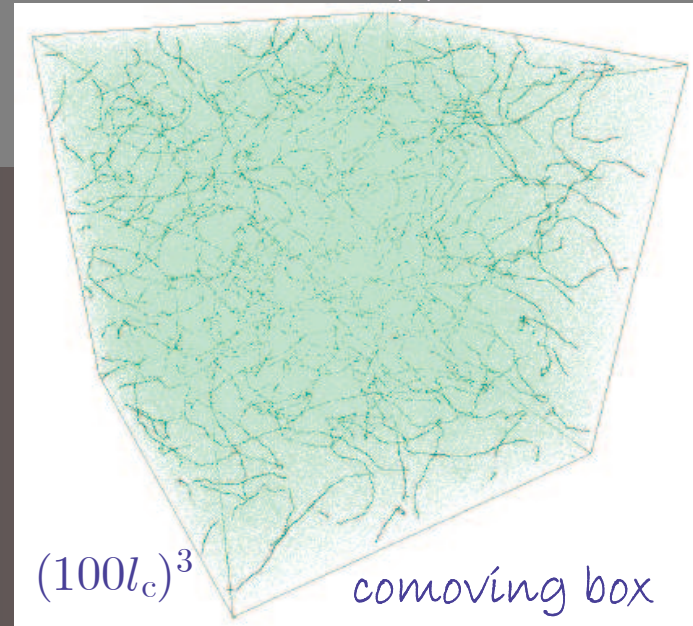
initial string sampling of 20 ppcl

$$d_{h_0} = 0.063 \quad \text{MDE}$$

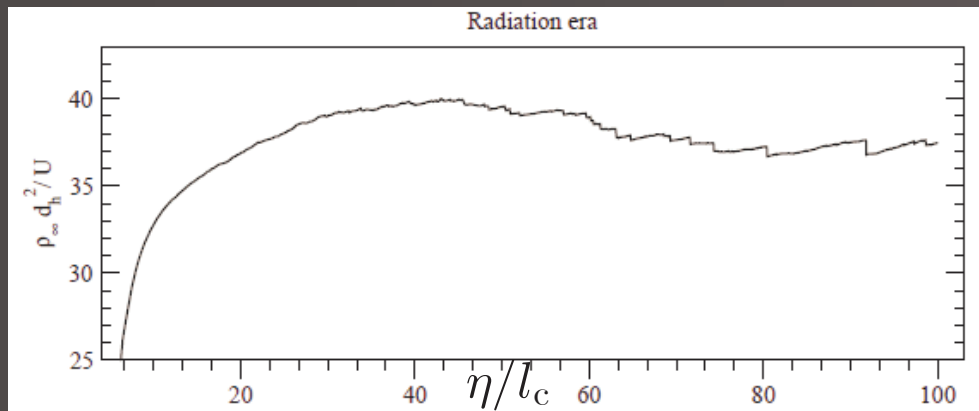
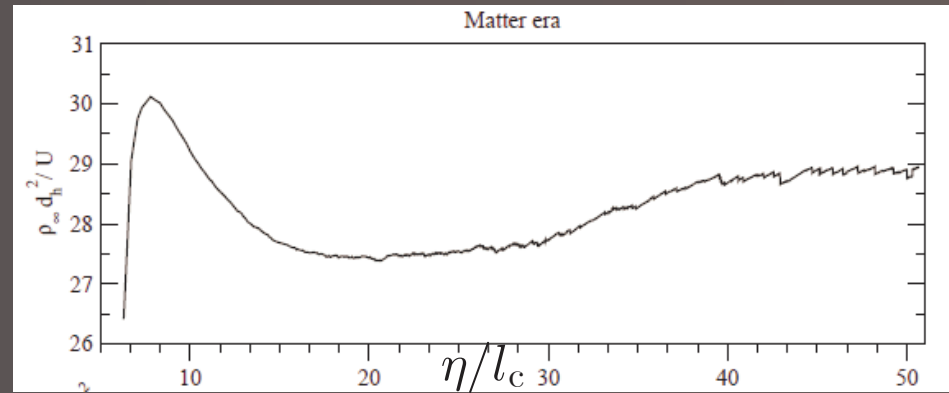
$$d_{h_0} = 0.057 \quad \text{RDE}$$

dynamic range:

520 (MDE) and 308 (RDE) in physical time



scaling regime of long
(super-horizon) strings

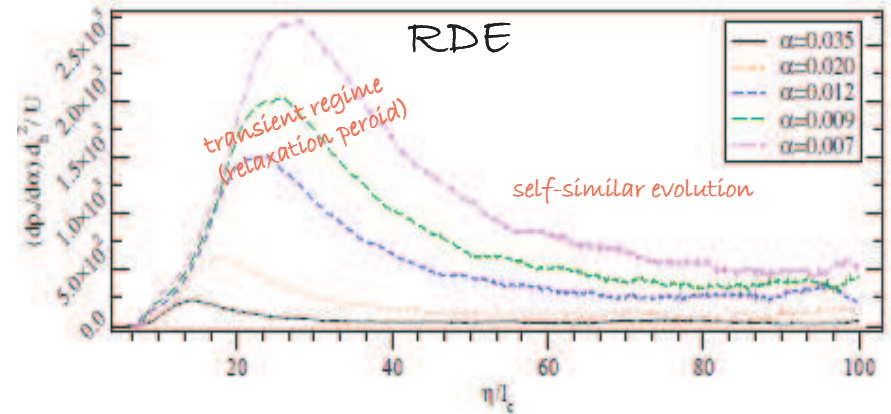
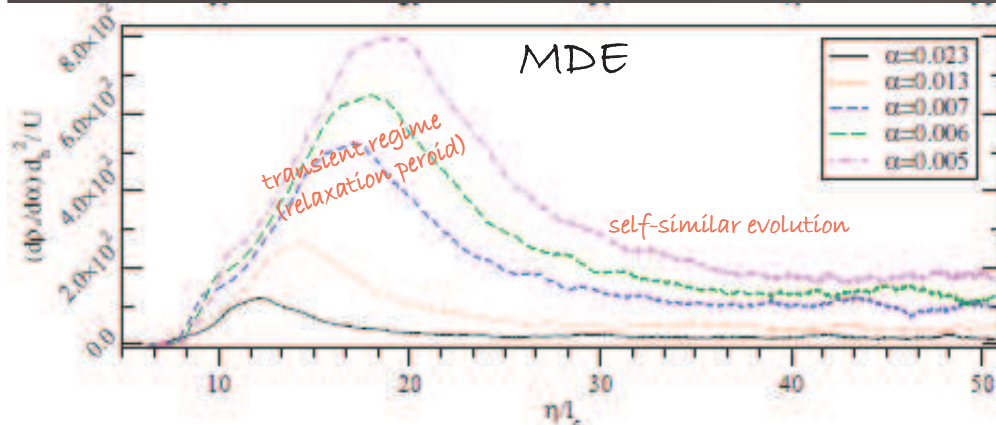


$$\rho_\infty \propto 1/d_h^2$$

$$\rho_\infty \frac{d_h^2}{U} \Big|_{\text{mat}} = 28.4 \pm 0.9, \quad \rho_\infty \frac{d_h^2}{U} \Big|_{\text{rad}} = 37.8 \pm 1.7$$

ringeval, m.s., bouchet JCAP 0702 (2007) 023

scaling evolution for loops as small as a few thousandths the horizon size

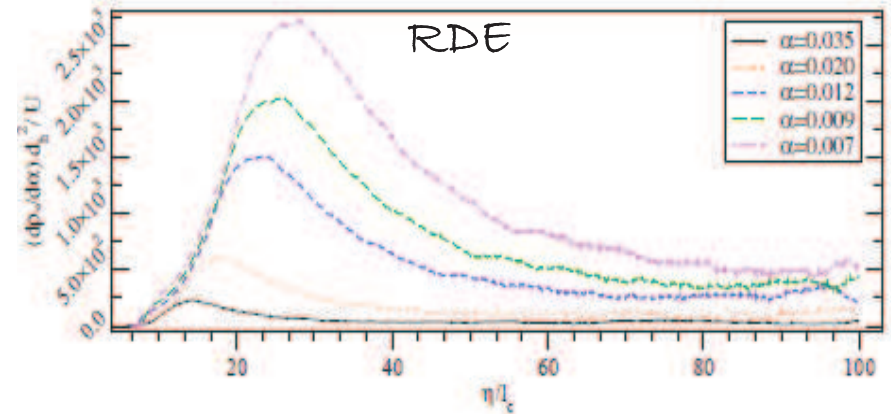
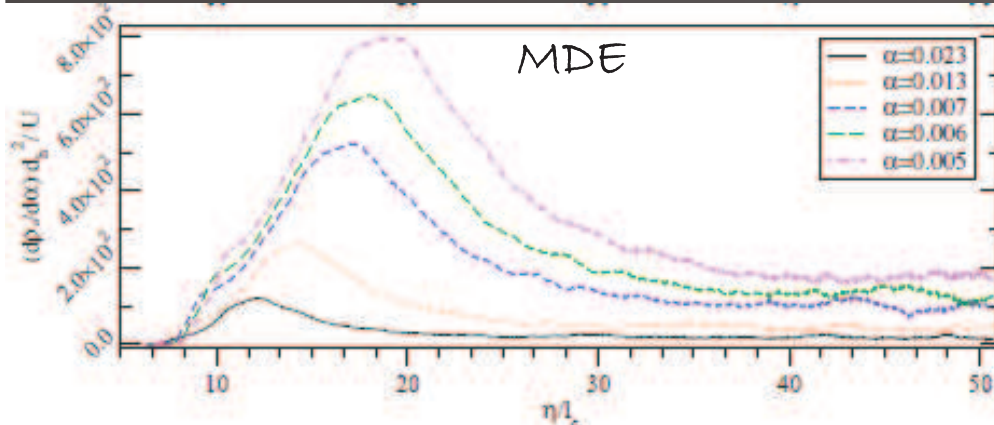


$$d\rho_0 \propto 1/d_h^2$$

$$l_{\text{phys}} = \alpha d_h$$

$d\rho_0(\alpha)$: energy density carried by loops whose length, in units of d_h , is in the range α to $\alpha + d\alpha$

scaling evolution for loops as small as a few thousandths the horizon size



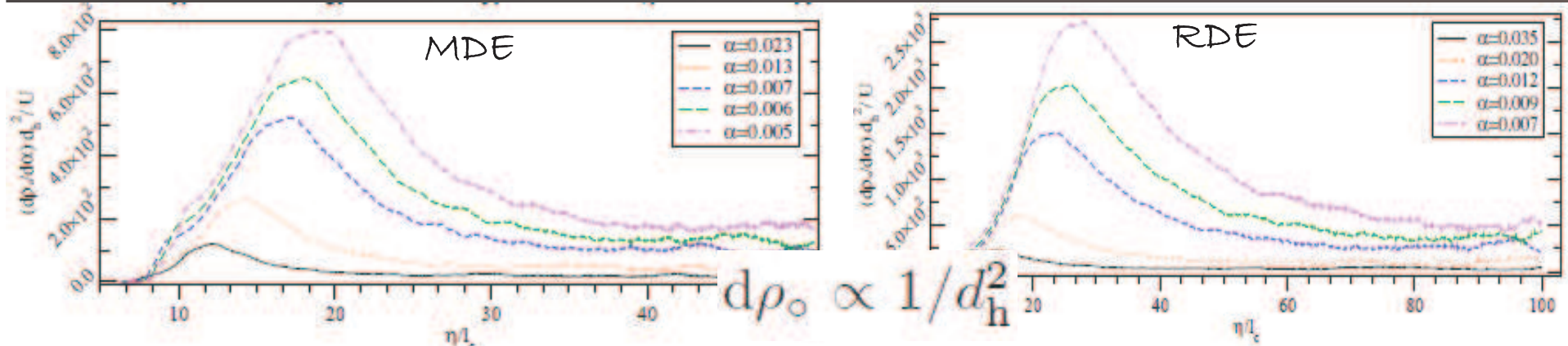
$$d\rho_o \propto 1/d_h^2$$

$$l_{\text{phys}} = \alpha d_h$$

$d\rho_o(\alpha)d_h^2$ remains stationary, for all values of α down to approximately 5×10^{-3}

ringeval, m.s., bouchet JCAP 0702 (2007) 023

scaling evolution for loops as small as a few thousandths the horizon size



intersection processes which create loops from long strings is similar to that for loops themselves
 loop self-interactions give rise to more numerous smaller loops
 → a constant energy flow cascades from long strings to smallest loops
 reconnection process of small loops to long strings/larger loops is negligible

string dynamics and intercommutation lead to a scaling regime:

$$\frac{d\rho_{\circ}}{d\alpha} = \mathcal{S}(\alpha) \frac{U}{d_h^2}, \quad \frac{dn}{d\alpha} = \frac{\mathcal{S}(\alpha)}{\alpha d_h^3}$$

$$\mathcal{S}(\alpha) = C_{\circ} \alpha^{-p}$$

$$\left\{ \begin{array}{l} p \\ C_{\circ} \end{array} \right\}_{\text{mat}} = \left\{ \begin{array}{l} 1.41^{+0.08}_{-0.07} \\ 0.09^{-0.03}_{+0.03} \end{array} \right\}, \quad \text{and} \quad \left\{ \begin{array}{l} p \\ C_{\circ} \end{array} \right\}_{\text{rad}} = \left\{ \begin{array}{l} 1.60^{+0.21}_{-0.15} \\ 0.21^{-0.12}_{+0.13} \end{array} \right\}$$

loop formation is the dominant energy carrying mechanism
(scaling regime does not rely on gravitational back reaction effects)

ringeval, m.s., bouchet JCAP 0702 (2007) 023

cosmic string loops

analytical model

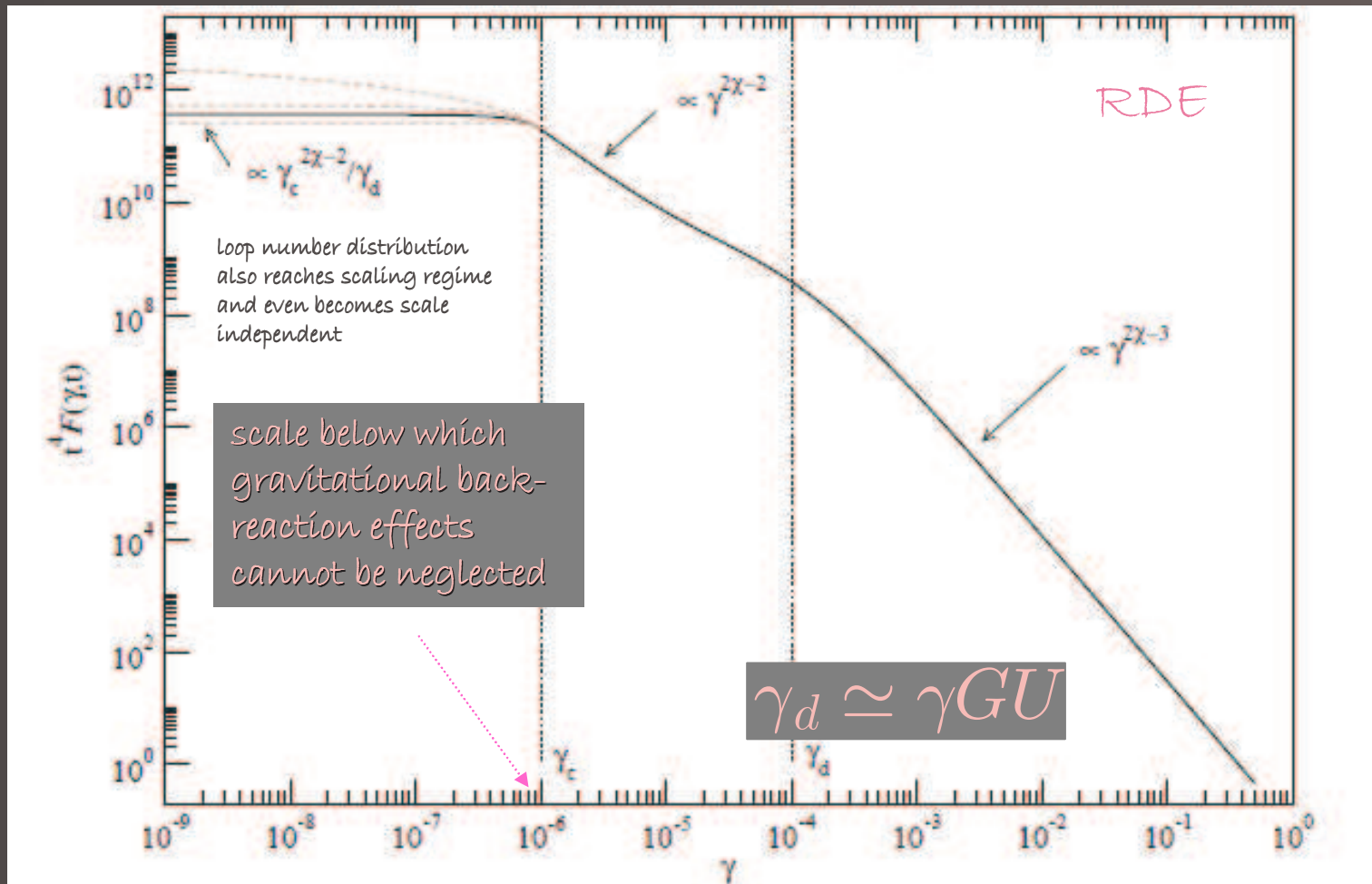
model based on polchinski-rocha loop production function,

$$\frac{\partial}{\partial t} \left(a^3 \frac{dn}{d\ell} \right) - \gamma_d \frac{\partial}{\partial \ell} \left(a^3 \frac{dn}{d\ell} \right) = a^3 \mathcal{P}(\ell, t)$$

$$\frac{d\ell}{dt} = -\gamma_d$$

adjusted to fit simulations and considering loop decay by GW and string smoothing due to gravitational back-reaction

lorenz, ringeval, *m.s. JCAP 1010 (2010) 003*

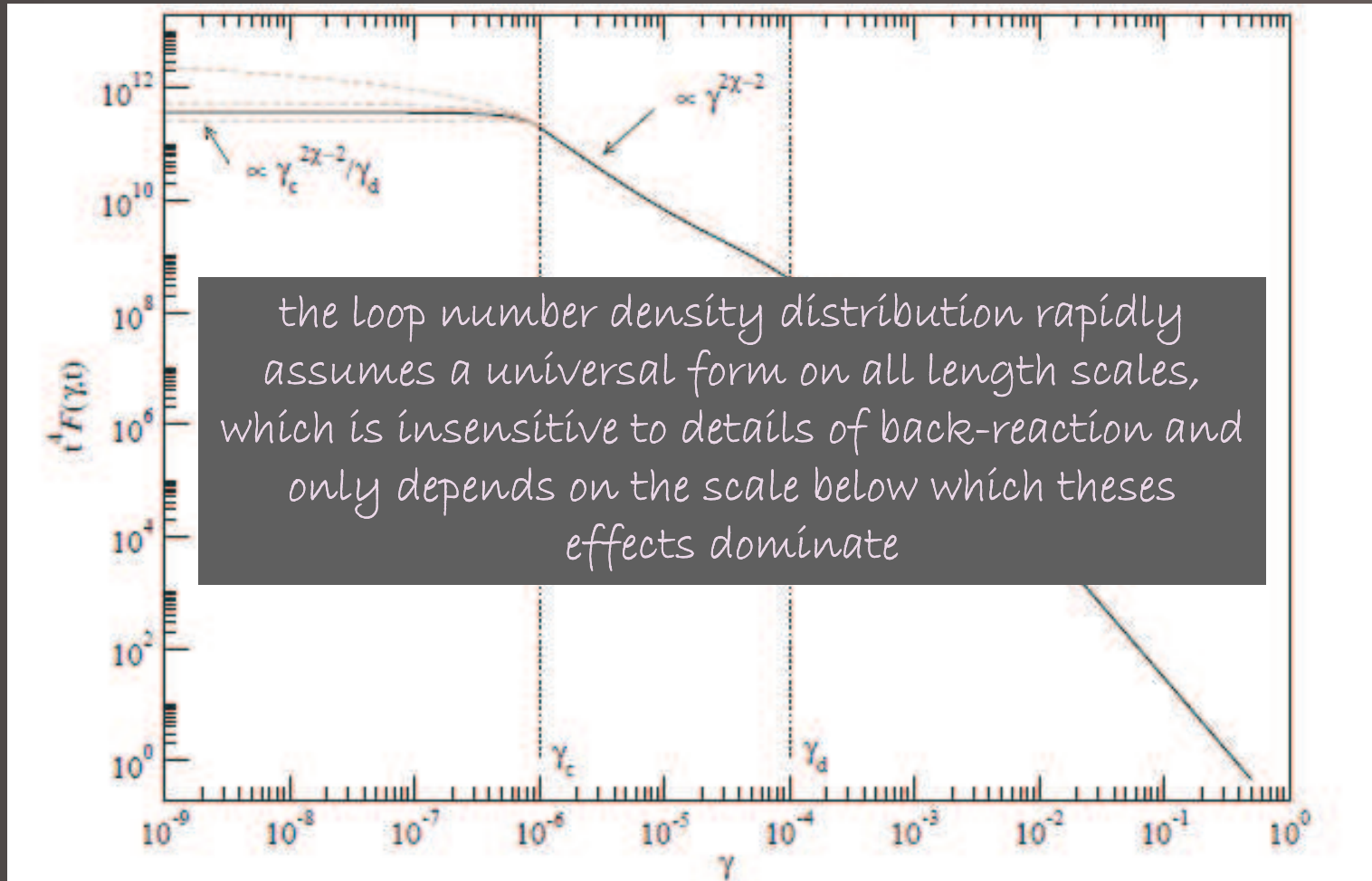


$$\chi = 1 - \frac{p}{2}$$

$$\gamma(\ell, t) \equiv \frac{\ell}{t}$$

$$\mathcal{F}(\gamma, t) \equiv \frac{dn}{d\ell}$$

lorenz, ringeval, m.s. JCAP 1010 (2010) 003



$$\gamma(\ell, t) \equiv \frac{\ell}{t}$$

$$\mathcal{F}(\gamma, t) \equiv \frac{dn}{d\ell}$$

lorenz, ringeval, m.s. JCAP 1010 (2010) 003

- *how long does it take to relax towards this universal form ?*

for any reasonable initial distribution and string formation temperature, the loop distribution reaches full scaling well before BBN

$$\forall GU > 10^{-28} \quad (\sqrt{U} > 100 \text{ TeV})$$

any initial loop remnants have been radiated away at $z_{\text{eq}} \approx 10^4$

- can we still observe traces of loops formed in the RDE in the matter loop distribution ?

loop number density distribution is today in full scaling on all length scales provided $\gamma_d > 10^{-14}$

if $\gamma_d < 10^{-14}$ then some loops having a size $\gamma_c < \gamma \leq \gamma_d$ have been formed in RDE; on the other length scales the distribution matches with the MDE attractor

in the MDE, the loop distribution reaches full scaling, up to some residual loops from the RDE which may be present for extremely low string tension

energy density parameter of loops:

$$\Omega_o \simeq 0.10 \times (GU)^{0.59}$$



for $GU \simeq 7 \times 10^{-7}$

the energy density cannot exceed 10^{-5}



NG strings cannot provide DM candidate

energy density parameter of loops:

$$\Omega_o \simeq 0.10 \times (GU)^{0.59}$$



for $GU \simeq 7 \times 10^{-7}$

the energy density cannot exceed 10^{-5}



NG strings cannot provide DM candidate

lower limit of loop
number density

$$n_L \simeq 5.5 \times 10^{-6} \text{ Mpc}^{-3}$$

small
number

$n_L \propto (GU)^{-1.65}$ loops from very light CS are more numerous
lensing from loops are more frequent for low values of GU

effects of anisotropic dynamics on cosmic strings

motivation

- anomalies in the WMAP data
(alignment of the moments in the lowest multipoles
suppression of the quadrupole)
- overshoot problem in inflation

avelino, martins (2000, 2003)

avgoustidis, shellard (2005)

kunze, m.s. arXiv:1106.4434

moving straight string

$$x^i(\zeta, \tau) = b^i(\tau) + c^i \zeta$$

moving straight string $x^i(\zeta, \tau) = b^i(\tau) + c^i \zeta$

- isotropic case

$$v^i = \dot{b}^i$$

$$v(1 - v^2)^{-\frac{1}{2}} \propto a^{-2}$$

moving straight string $x^i(\zeta, \tau) = b^i(\tau) + c^i \zeta$

- isotropic case

$$v(1 - v^2)^{-\frac{1}{2}} \propto a^{-2}$$

- anisotropic case

$$\dot{v}^i + \left[2 \frac{\dot{a}_i}{a_i} - \frac{\dot{a}_1}{a_1} - \sum_j \frac{a_j \dot{a}_j}{a_1^2} \left(v^j{}^2 - \left(\frac{c^i}{\epsilon} \right)^2 \right) \right] v^i = 0$$

physical velocity of the string $V^i = a_i \frac{dx^i}{dt} = \frac{a_i}{a_1} v^i$

$$\epsilon = \left(\frac{\sum_i a_i^2 (c^i)^2}{a_1^2 - \sum_i a_i^2 (v^i)^2} \right)^{\frac{1}{2}}$$

moving straight string $x^i(\zeta, \tau) = b^i(\tau) + c^i \zeta$

- isotropic case

$$v(1 - v^2)^{-\frac{1}{2}} \propto a^{-2}$$

- anisotropic case

$$\dot{v}^i + \left[2 \frac{\dot{a}_i}{a_i} - \frac{\dot{a}_1}{a_1} - \sum_j \frac{a_j \dot{a}_j}{a_1^2} \left(v^j{}^2 - \left(\frac{c^i}{\epsilon} \right)^2 \right) \right] v^i = 0$$

physical velocity of the string $V^i = a_i \frac{dx^i}{dt} = \frac{a_i}{a_1} v^i$

numerical solutions indicate that the behaviour of a velocity component is inversely proportional to the scale factor in that direction

small perturbations on a static straight string

$$x^i = c^i \zeta + \delta x^i$$

small perturbations on a static straight string

$$x^i = c^i \zeta + \delta x^i$$

$$\delta \ddot{x}^i + \left[2 \frac{\dot{a}_i}{a_i} - \frac{\dot{a}_1}{a_1} + M \right] \delta \dot{x}^i - N (\delta x^i)'' = 0$$

$$M \equiv \frac{\sum_j a_j \dot{a}_j c^j{}^2}{\sum_m a_m^2 (c^m)^2}$$

$$N = \frac{a_1^2}{\sum_m a_m^2 (c^m)^2}$$

small perturbations on a static straight string

$$x^i = c^i \zeta + \delta x^i$$

$$\delta \ddot{x}^i + \left[2 \frac{\dot{a}_i}{a_i} - \frac{\dot{a}_1}{a_1} + M \right] \delta \dot{x}^i - N (\delta x^i)'' = 0$$

$$M \equiv \frac{\sum_j a_j \dot{a}_j c^j}{\sum_m a_m^2 (c^m)^2}$$

$$N = \frac{a_1^2}{\sum_m a_m^2 (c^m)^2}$$

one component $c^j \neq 0$ and the 2 perturbation components $\delta x^i \neq 0$ ($i \neq j$)

one perturbation amplitude $\delta x^j \neq 0$ and the 2 components $c^i \neq 0$ ($i \neq j$)

small perturbations on a static straight string

$$x^i = c^i \zeta + \delta x^i$$

$$\delta \ddot{x}^i + \left[2 \frac{\dot{a}_i}{a_i} - \frac{\dot{a}_1}{a_1} + M \right] \delta \dot{x}^i - N (\delta x^i)'' = 0$$

$$M \equiv \frac{\sum_j a_j \dot{a}_j c^j{}^2}{\sum_m a_m^2 (c^m)^2}$$

$$N = \frac{a_1^2}{\sum_m a_m^2 (c^m)^2}$$

one component $c^j \neq 0$ and the 2 perturbation components $\delta x^i \neq 0$ ($i \neq j$)

one perturbation amplitude $\delta x^j \neq 0$ and the 2 components $c^i \neq 0$ ($i \neq j$)

$$\delta x^i = A^i(\tau) e^{ik\zeta}$$

kunze, m.s. arXiv:1106.4434

- irregularities on super-horizon scales are not frozen-in
(string becomes wigglier or straightens out, depending on the ratio of scale factors)



re-entering the horizon wiggleness may augment



generation of more GW

limits on global anisotropy of early universe

constraints on minimum number of e-folds

effects of anisotropic dynamics on strings loops:

- if the size of a loop is smaller than the horizon (expansion neglected) periodic solutions exist
- derivatives of right- & left-movers describe closed curves on an ellipsoid
- well inside the horizon the condition for cusps formation is the same as for an isotropic and flat geometry



the number of cusps is the same

but

- the shape or opening of the cusp changes
- the string velocity at the cusp may not be the luminal one

