

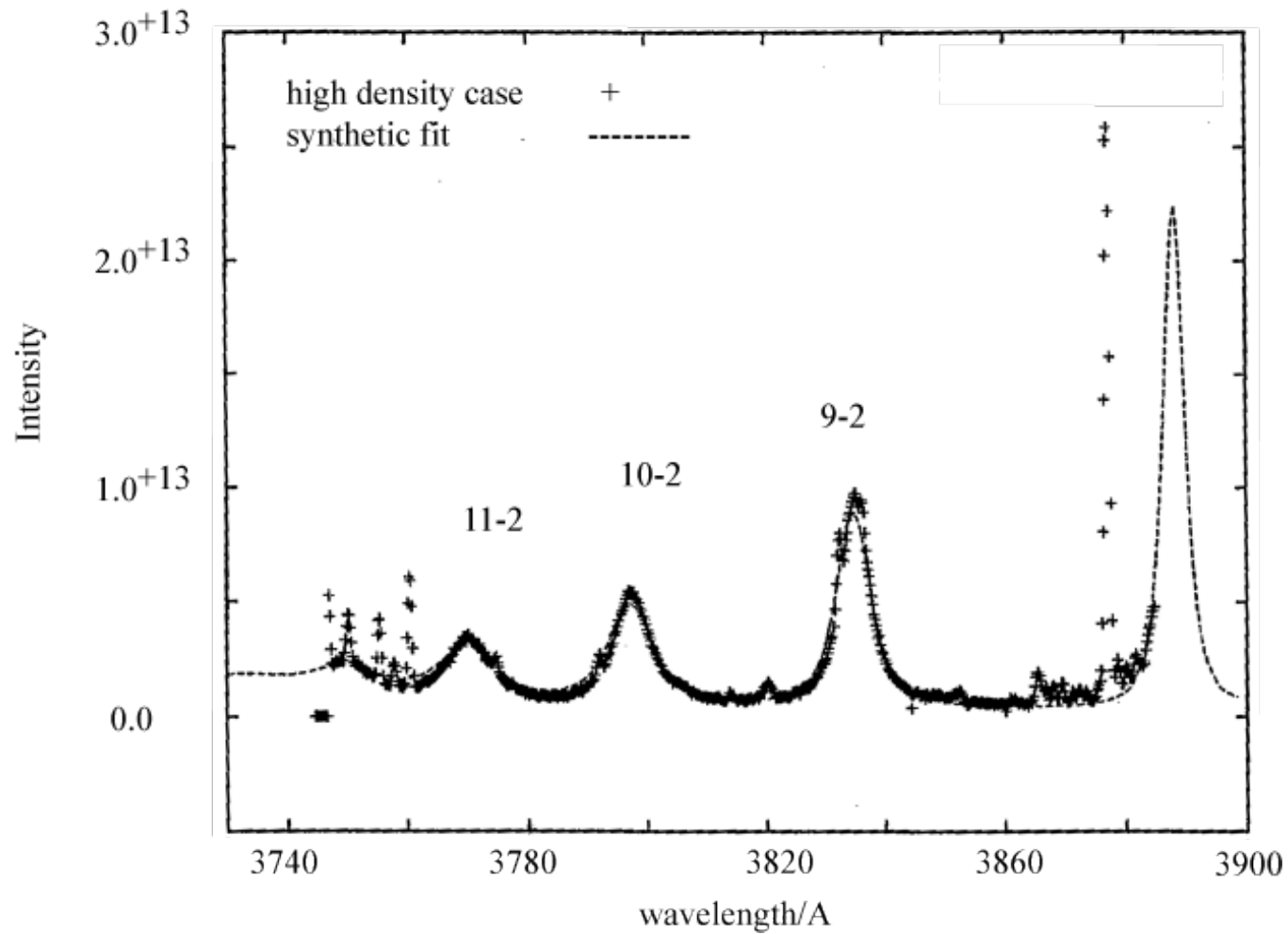
Population structure of atoms and ions in plasmas

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Cambridge

Balmer series spectrum



Fit to JET pulse #43735, Balmer series limit spectrum, track 6, time=18.95s

b and g

Introduce the Saha-Boltzmann population

$$N_i^{SAHA} = N_e N_+ 8 \left(\frac{\pi a_0^2 I_H}{k T_e} \right)^{3/2} \frac{\omega_i}{2 \omega_+} e^{I_i / k T_e}$$

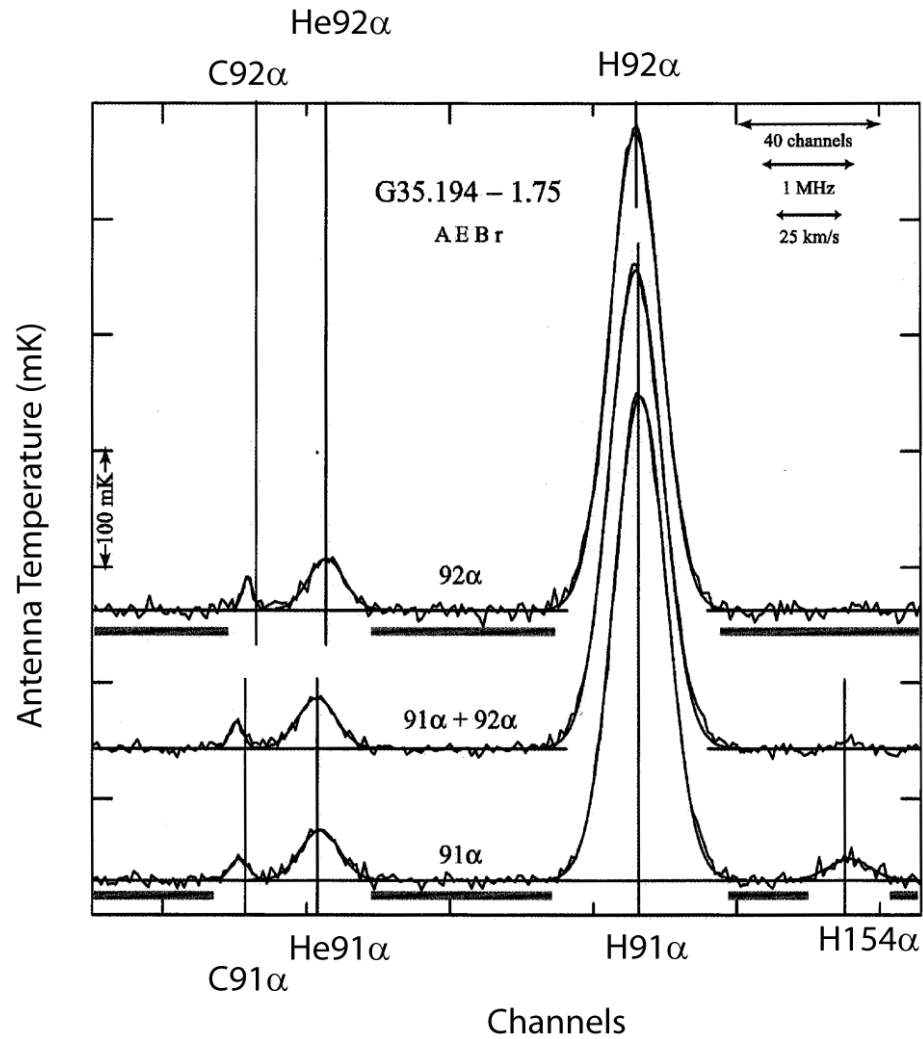
and the Kramer's expression for the oscillator strength

$$f'_{n' \rightarrow n} = \frac{2^6}{3\sqrt{3}\pi} \frac{1}{\omega_{n'}} \left(\frac{1}{n'^2} - \frac{1}{n^2} \right)^{-3} \left| \frac{1}{n^3 n'^3} \right|$$

Then the actual populations and oscillator strength are given by

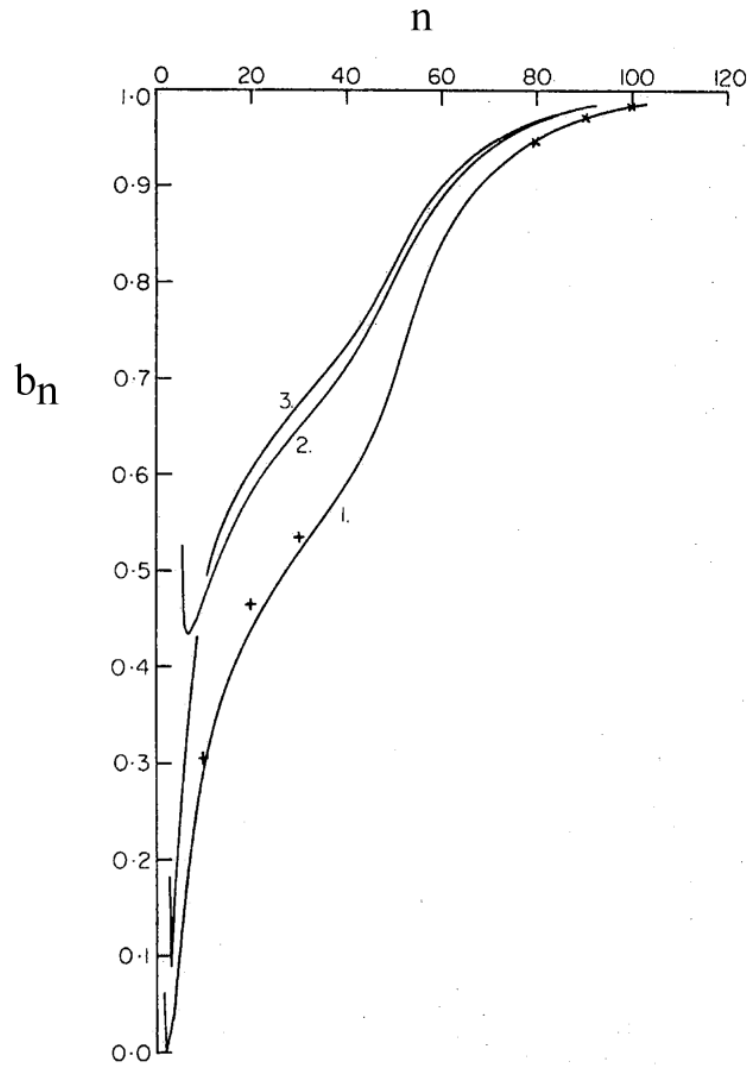
$$N_i = N_i^{SAHA} b_i \quad \text{and} \quad f_{n' \rightarrow n} = f'_{n' \rightarrow n} g_{nn'}$$

Observed microwave recombination-line spectra



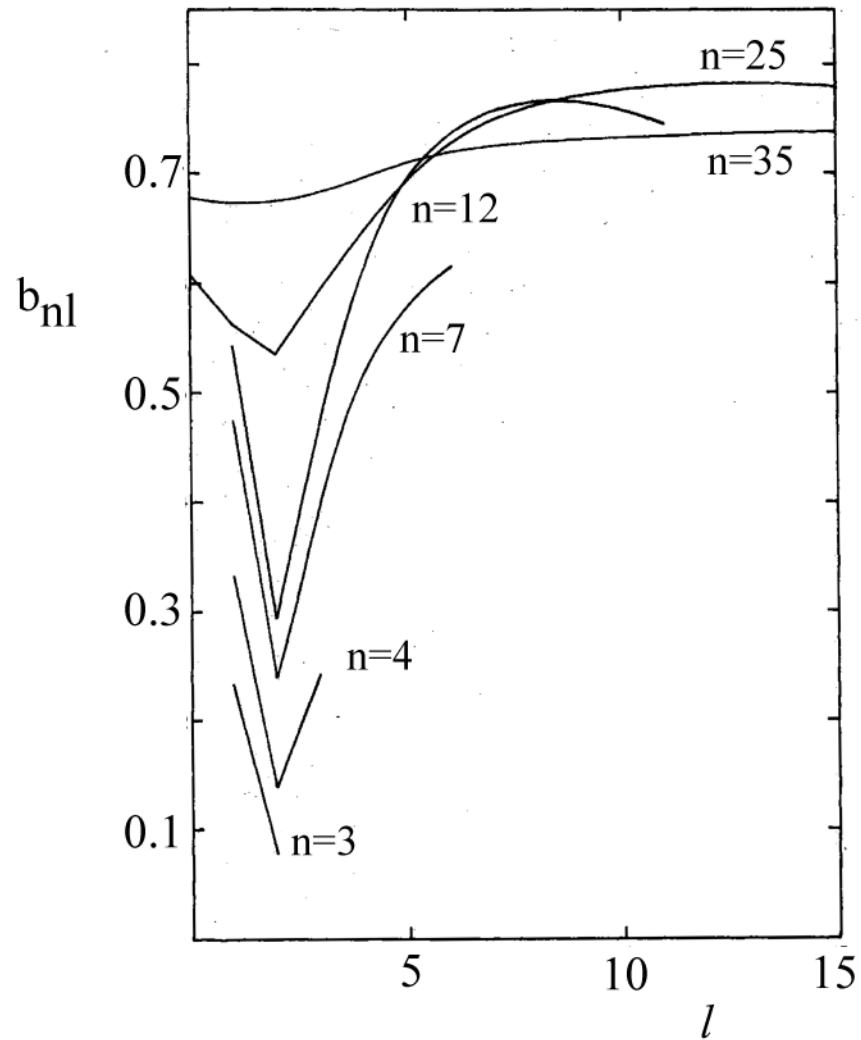
HII region: Quireza et al 2006, *Astrophys. J. Suppl.* 165, 338

H population structure: bundle-n



$T_e=5 \times 10^3$ K, $T_i=5 \times 10^3$ K, $N_e=10^4$ cm $^{-3}$. 1. Case A, $W=10^{-16}$; 2. Case B, $W=10^{-16}$; 3. Case B, $W=10^{-12}$; + Seaton radiative; x Hoang-Binh and Dyson

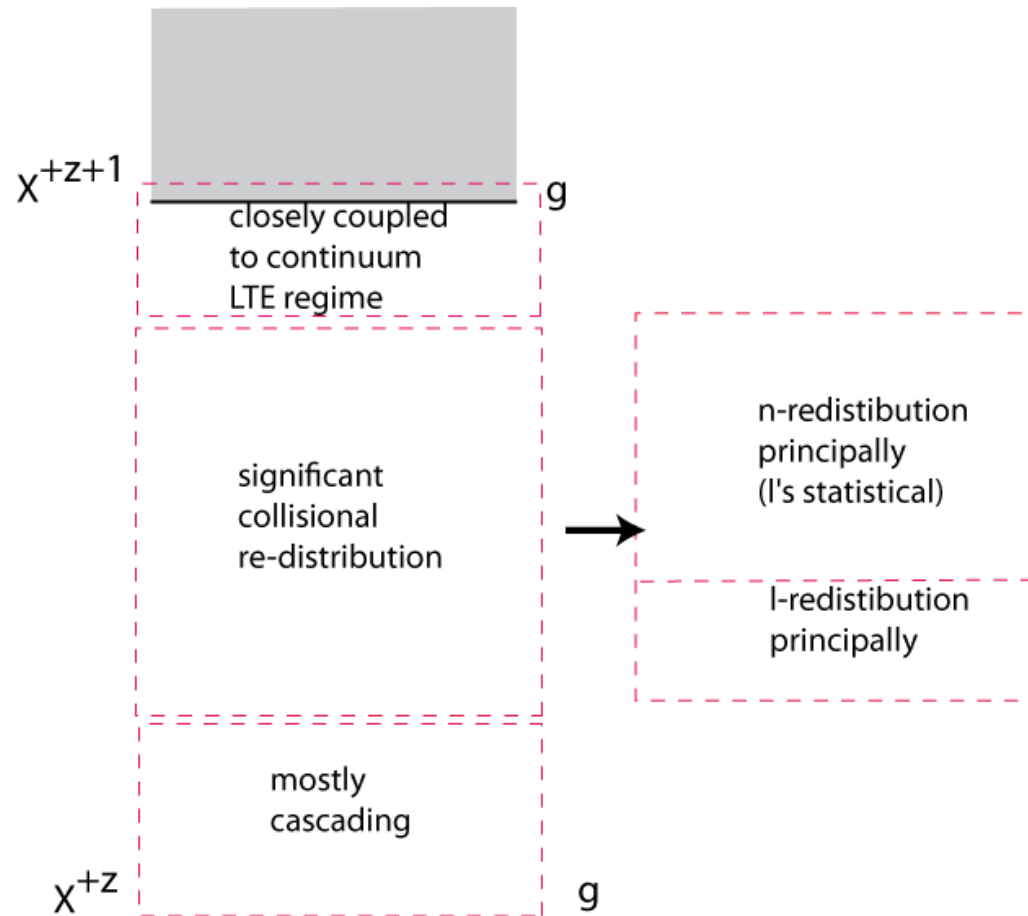
H population structure: bundle-nl



Case B, depopulated $n=2$ levels. $N_e=1.0^4 \text{ cm}^{-3}$, $T_e=1.0^4 \text{ K}$, $N_p=N_e$, $T_p=T_e$

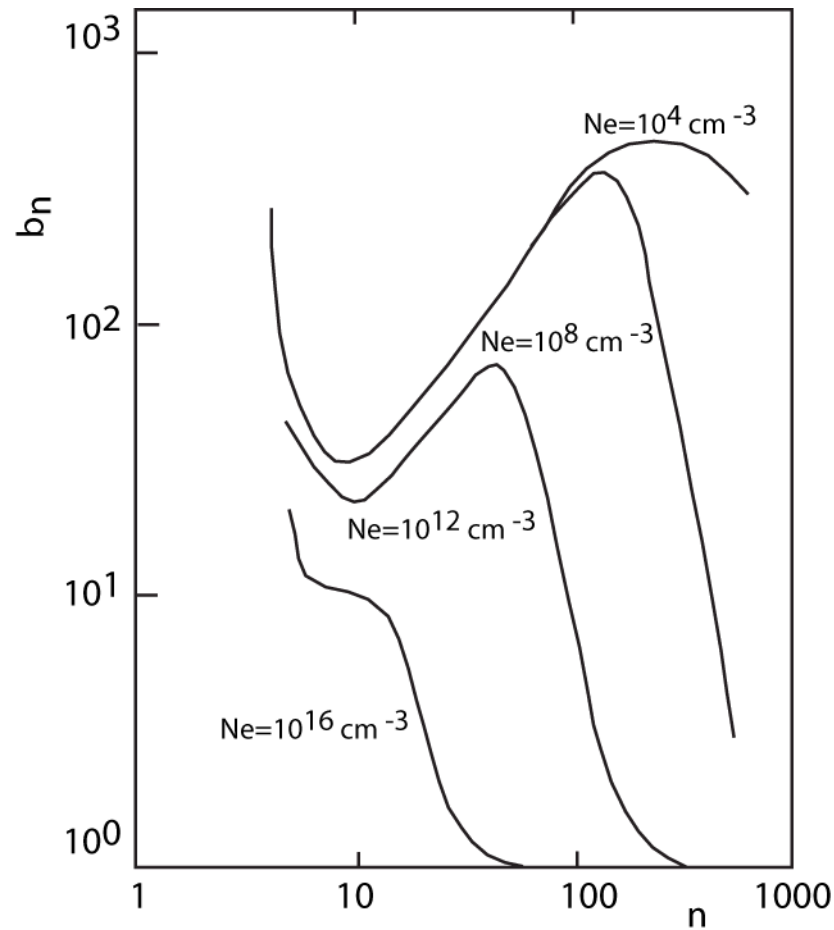
Collisional-radiative modelling schematic

Population regimes



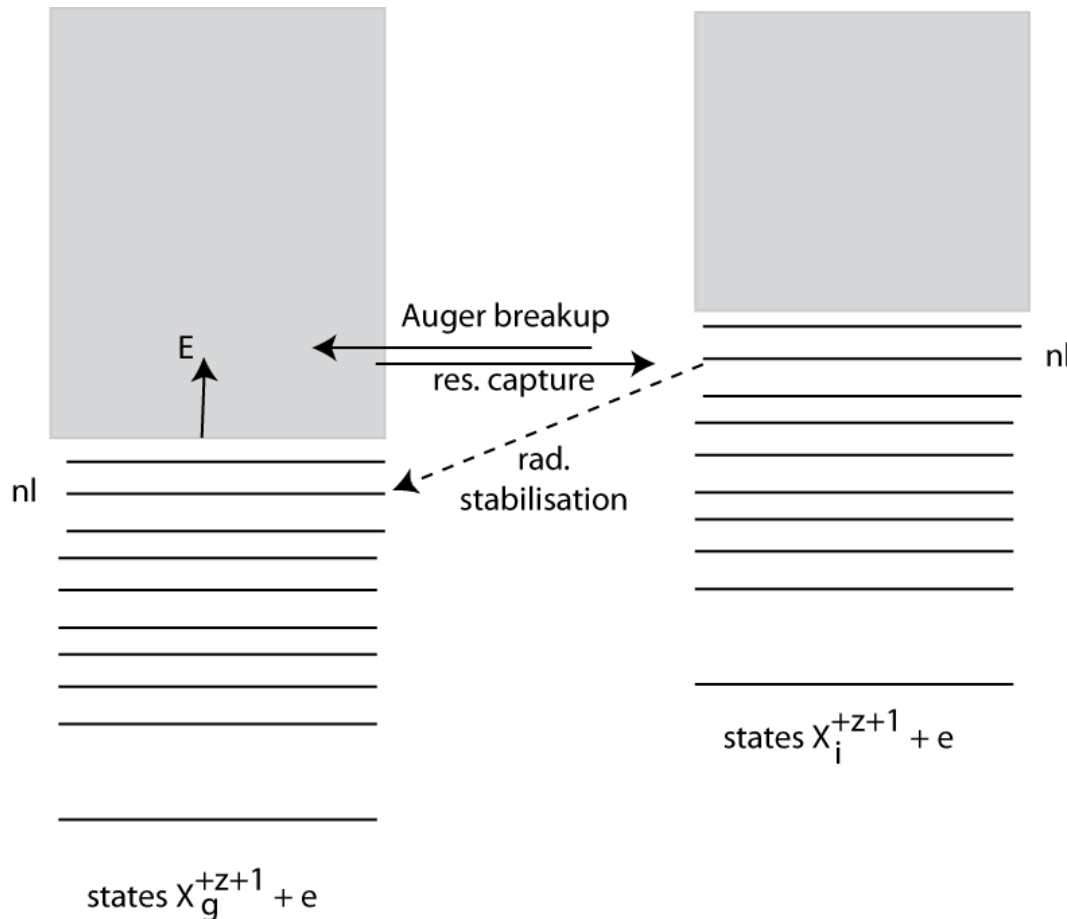
Population structure: bundle-n with DR

singly excited population structure

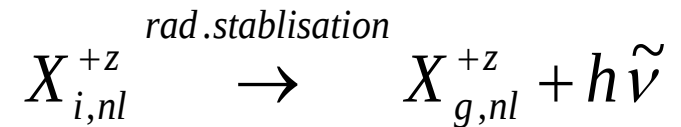
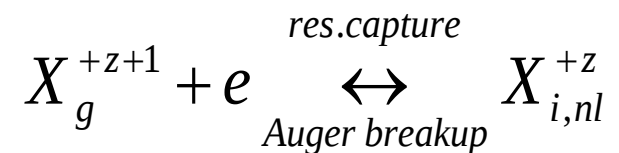


iron population structure Fe⁺¹⁴

CR modelling schematic : DR doubly excited



Reactions:



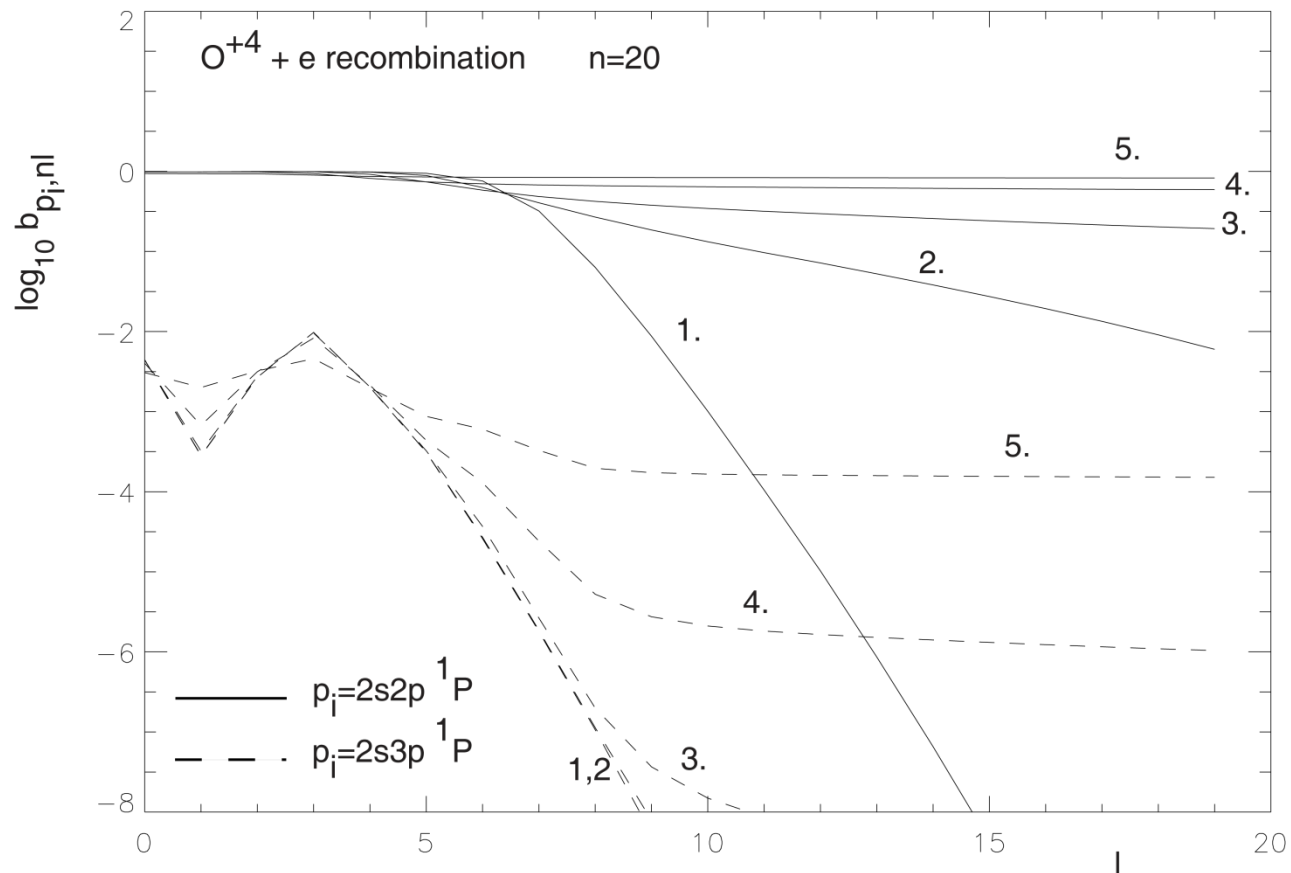
Doubly excited populations:

$$b_{i,nl} = \frac{A_a}{A_a + A_r}$$

$$\alpha_{g,nl}(T_e) = A_r N_{i,nl} / N_e N_g^+$$

At high density there may be re-distribution before stabilisation

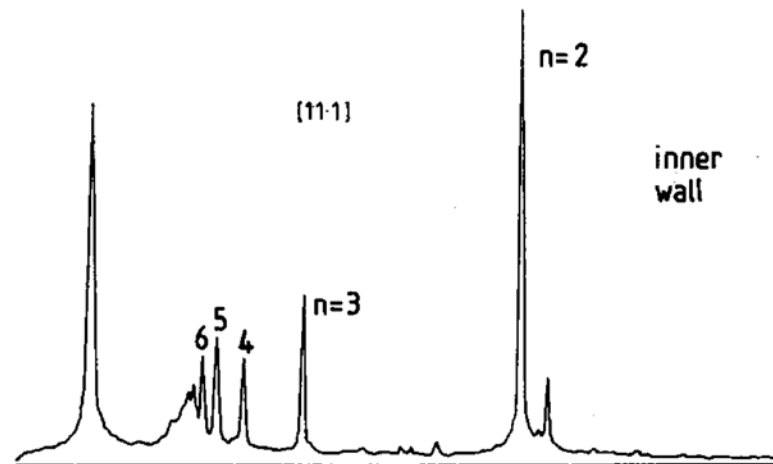
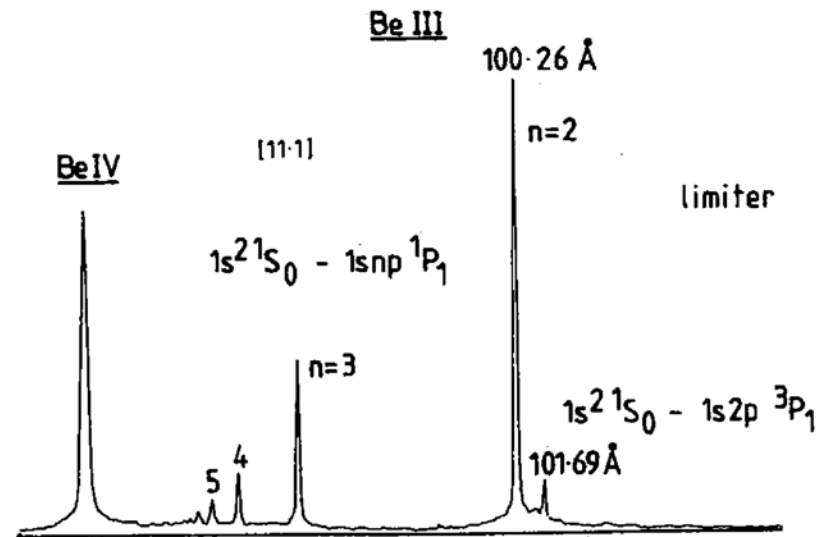
Population structure: bundle-nl, DR doubly excited



1. $N_e=N_p=10^{10} \text{ cm}^{-3}$; 2. $N_e=N_p=10^{12} \text{ cm}^{-3}$; 3. $N_e=N_p=10^{13} \text{ cm}^{-3}$; 4. $N_e=N_p=10^{14} \text{ cm}^{-3}$; 5. $N_e=N_p=10^{15} \text{ cm}^{-3}$

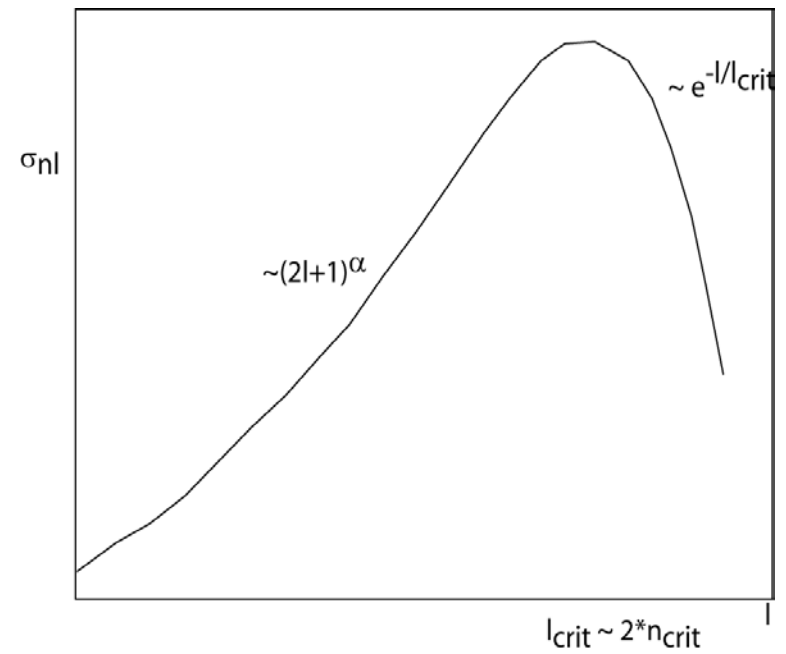
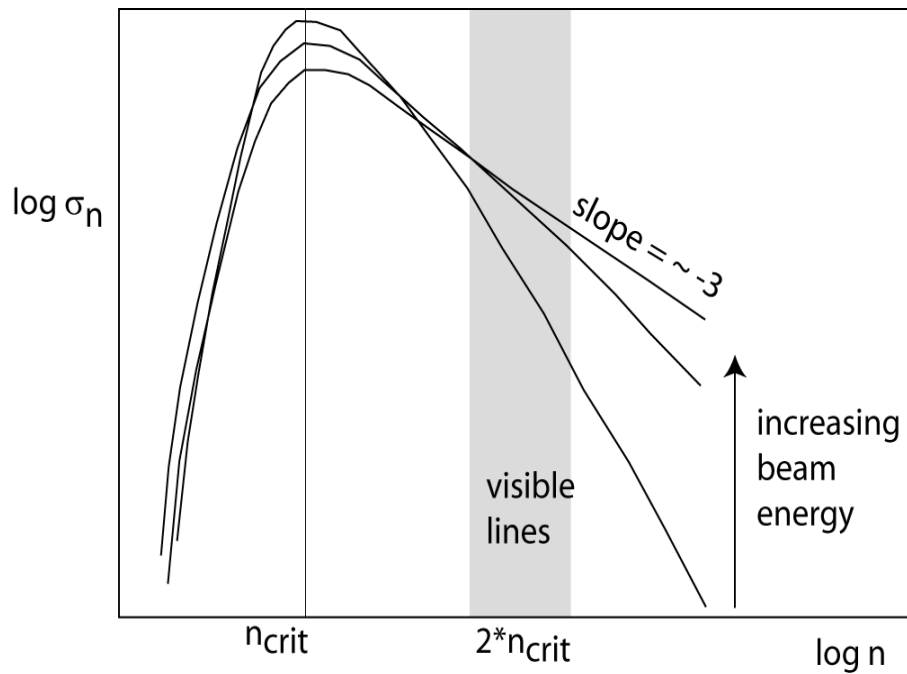
It is ion impact (deuterons in this case) which cause the re-distribution. The population reduction for the $2s3p \ ^1P$ parent is due to the opening of an alternative Auger channel ($\rightarrow 2s3s \ ^1S$).

Be XUV spectrum

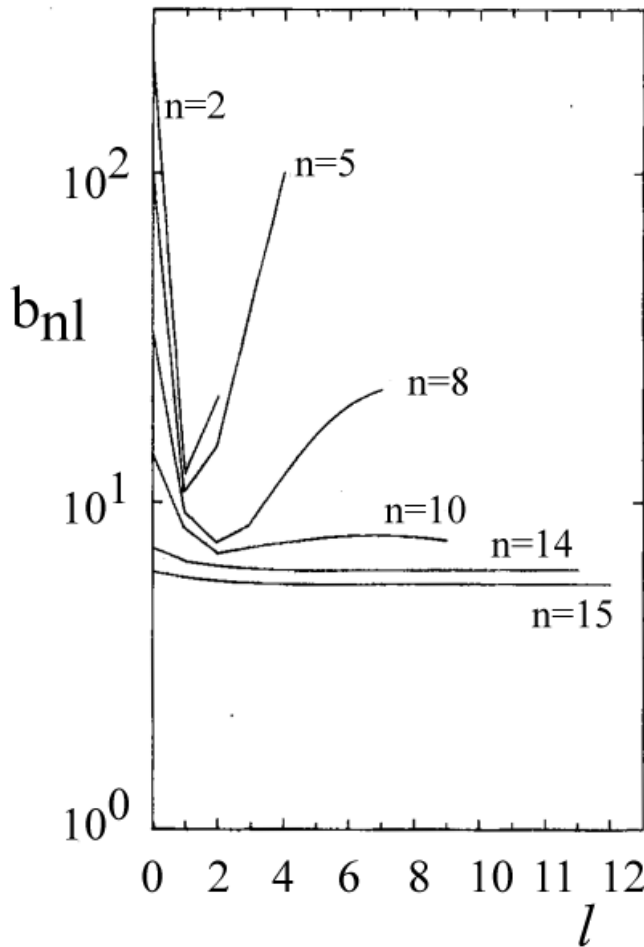


He-like Lyman series decrement as plasma moves into contact with the JET inner wall

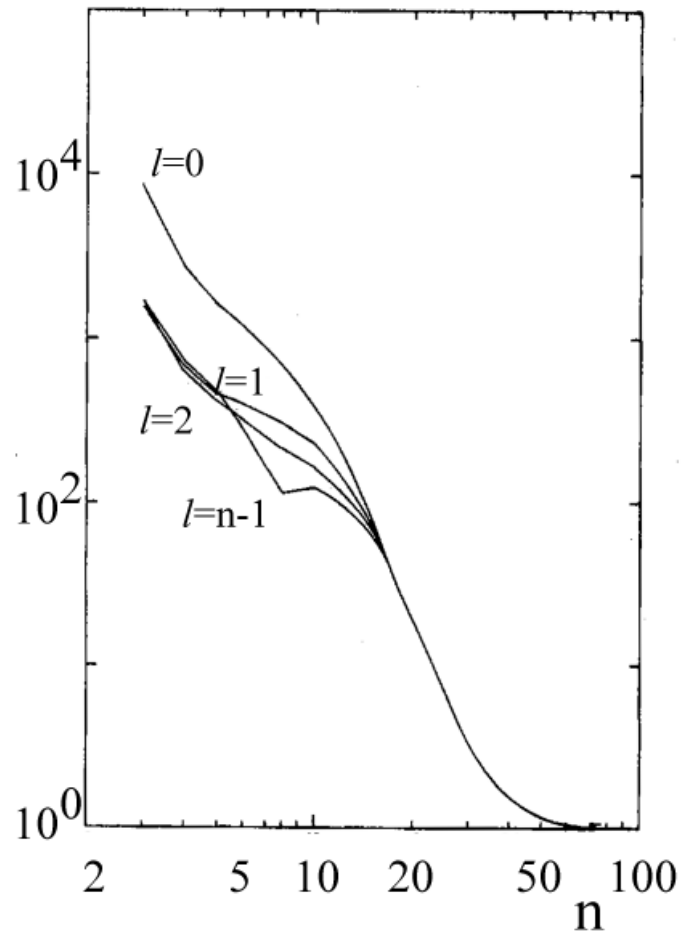
Behaviour of partial charge exchange xsects.



Population structure: bundle-nl with CX

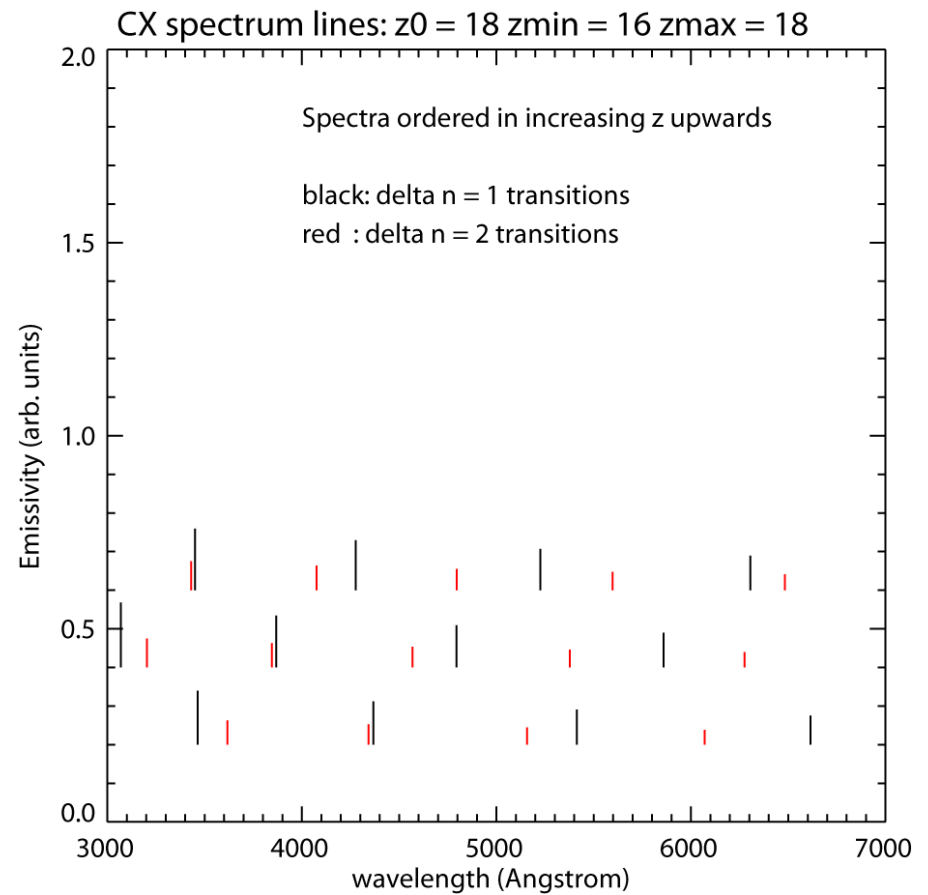
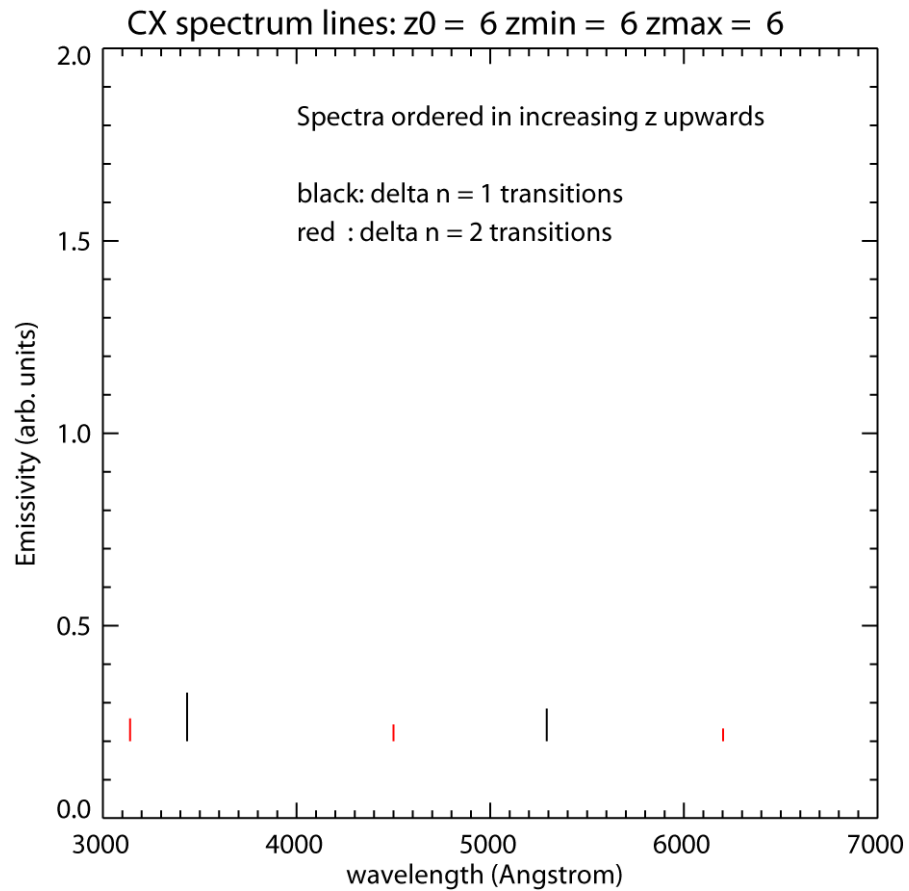


O^{+7} : $T_e=T_p=6.4 \times 10^6$, $N_e=N_p=5 \times 10^{13} \text{ cm}^{-3}$,
 $E_H=25 \text{ keV/amu}$, $N_H=5 \times 10^7 \text{ cm}^{-3}$

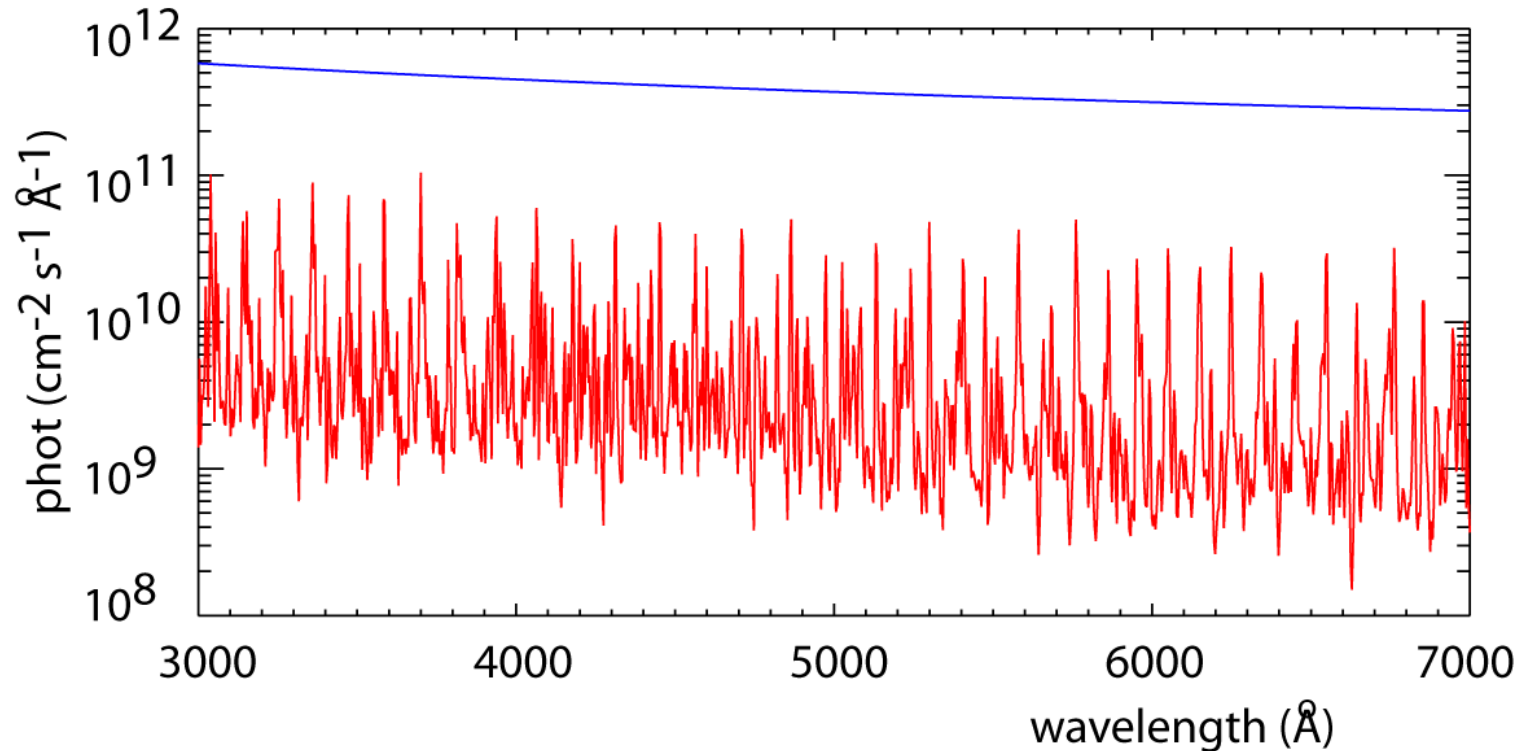


O^{+5} : $T_e=T_p=3.6 \times 10^6$, $N_e=N_p=5 \times 10^{13} \text{ cm}^{-3}$,
 $E_H=25 \text{ keV/amu}$, $N_H=5 \times 10^8 \text{ cm}^{-3}$

Patterns of CXS lines in the visible



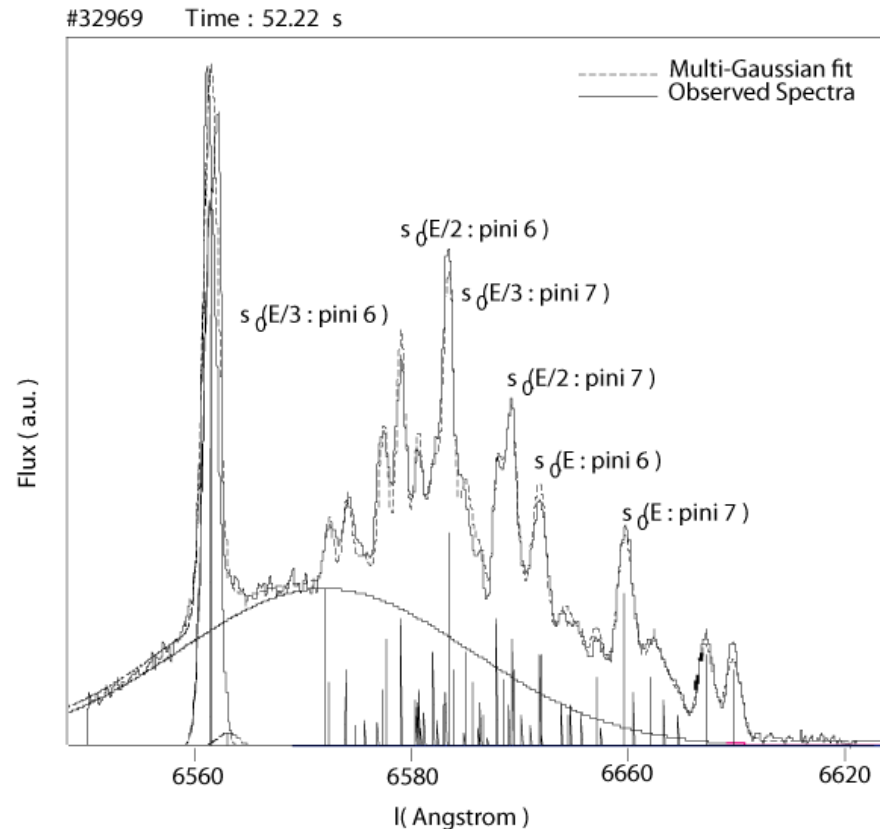
ITER: tungsten CX compared with Bremsstrahlung



- 50 keV/amu D beam (diagnostic NB), JNBI=300A/m², INBI=60A
- Using ITER scenario 2 ($T_e=20\text{keV}$ core, $N_e=1\times 10^{14}\text{cm}^{-3}$)
- No transport – steady state ionisation balance
- Assume looking vertically down on the beam at the core.
- No beam attenuation effects taken into account.
- W concentration = 1×10^{-6} of N_H

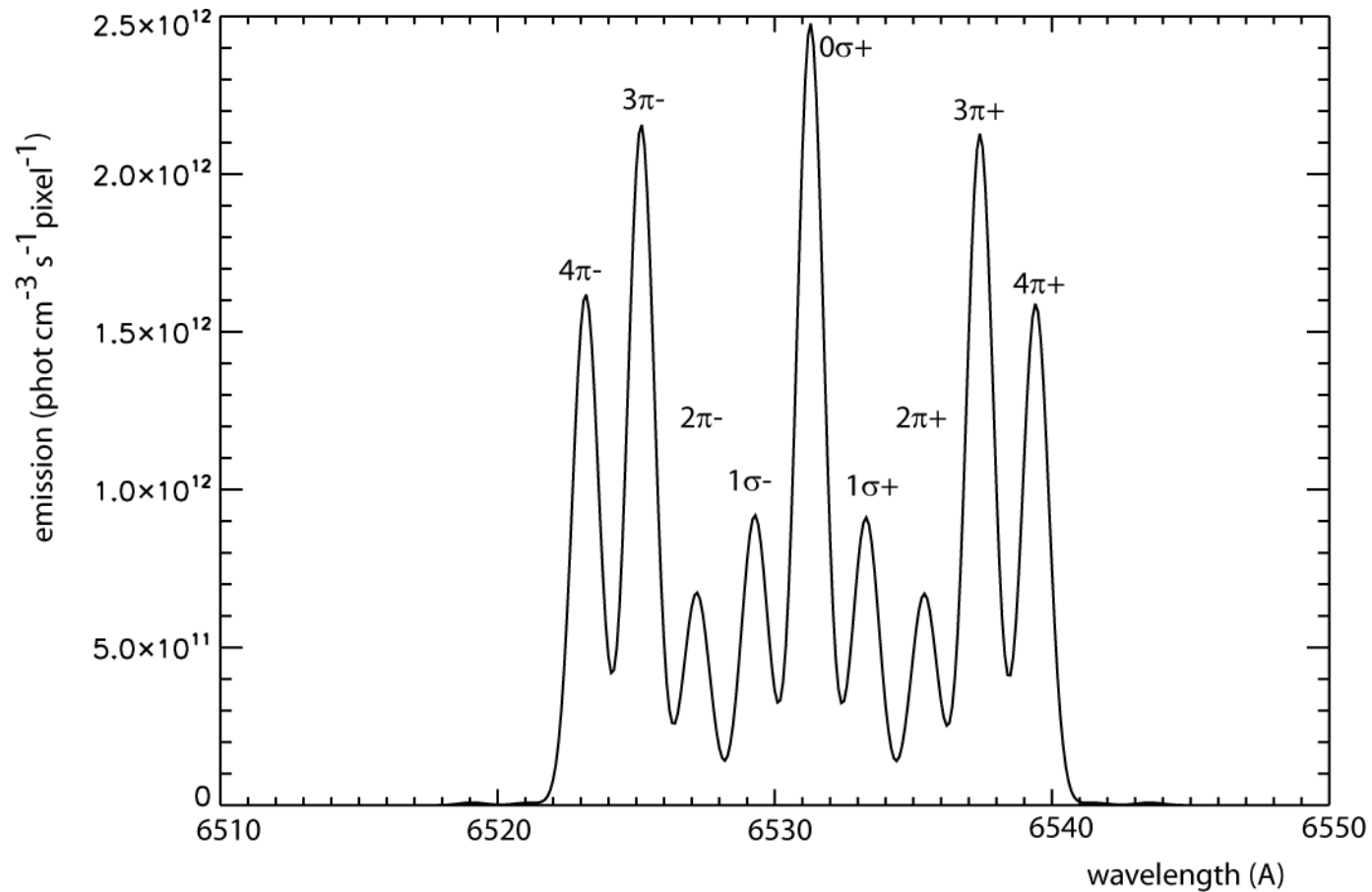
Beam stopping and beam emission

- The beam emission lines appear as Stark multiplets due to the motional electric field in the beam atom frame.



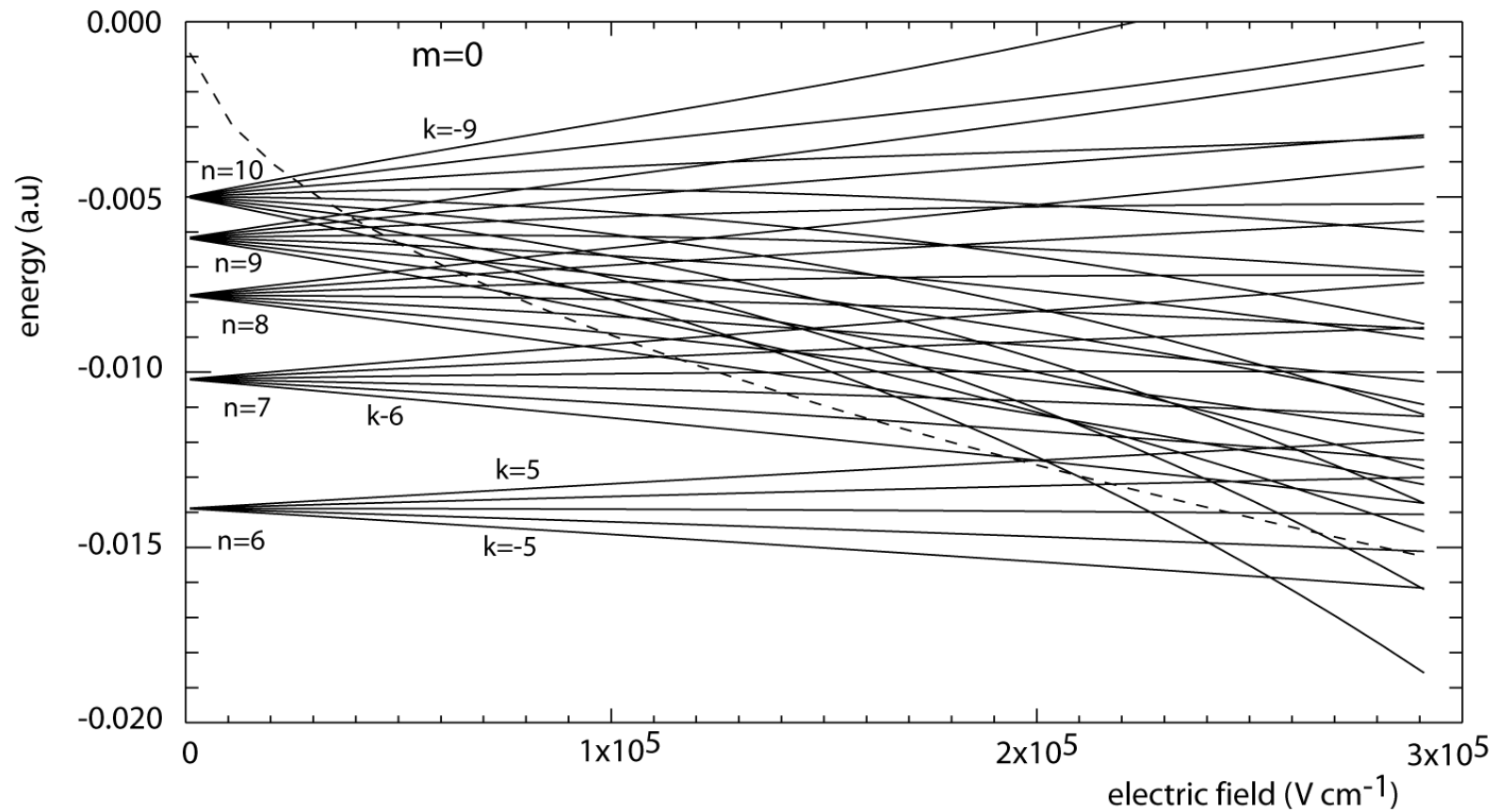
- Stark manifold collisional-radiative models describe the precise wavelengths, the polar distribution and polarisation of emission and the collisional mixing for the low n-shell emission (Balmer and Paschen)

Beam stopping and beam emission

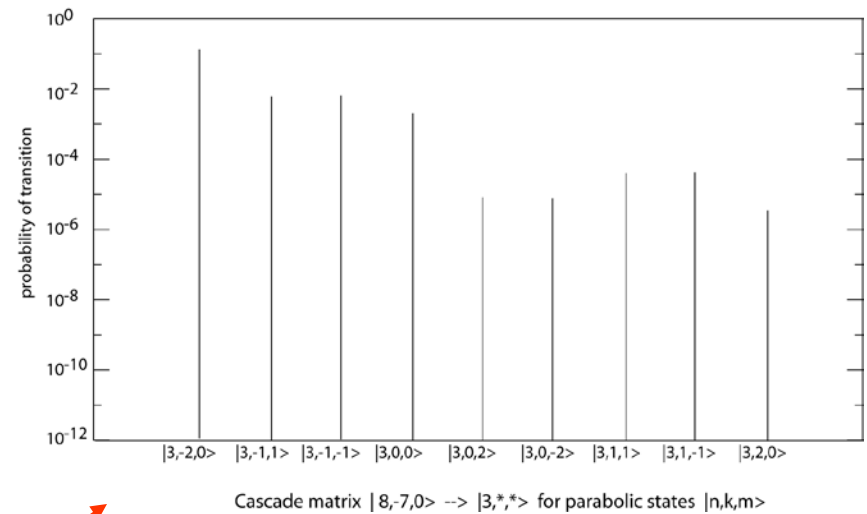
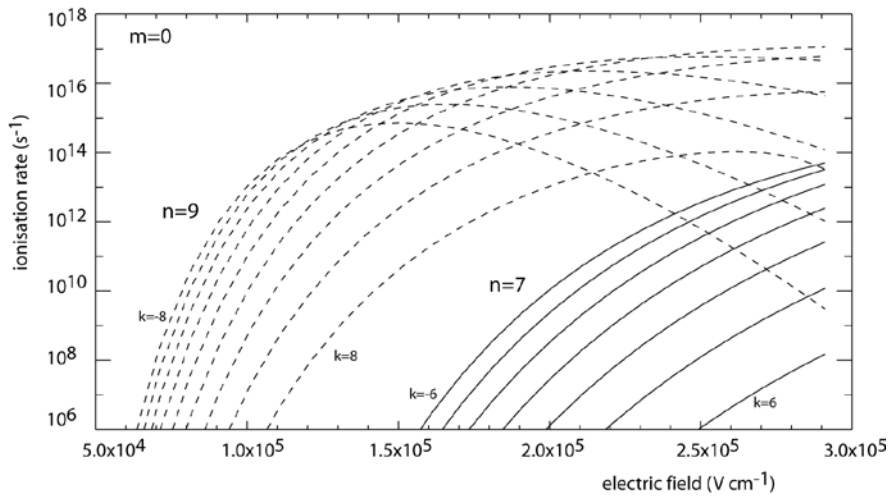


Stark multiplet components of D(n=3-2) beam emission

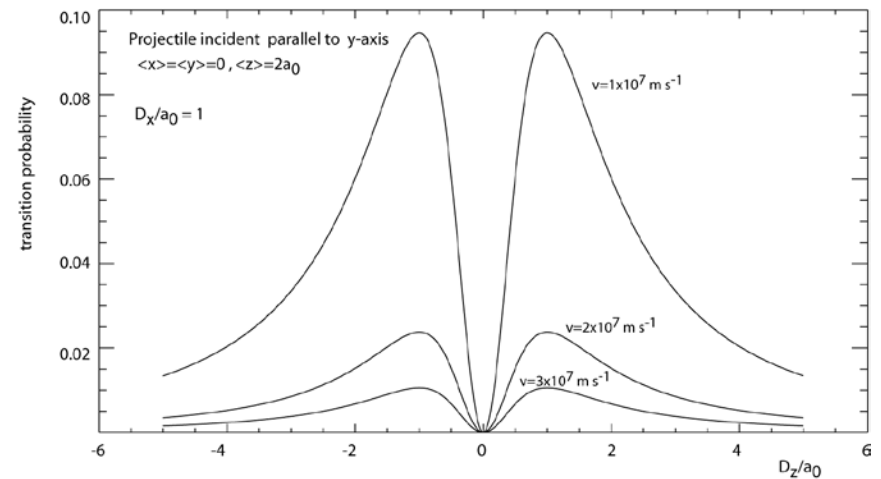
Stark energy levels



Some issues



1. Field ionisation
2. k-cascade
3. Directional, angular differential cross-sections



Fire and Water

(Susan Gamble & Michael Wenyon)



SOHO CDS : NIS-1 & NIS-2 quiet sun spectrum

