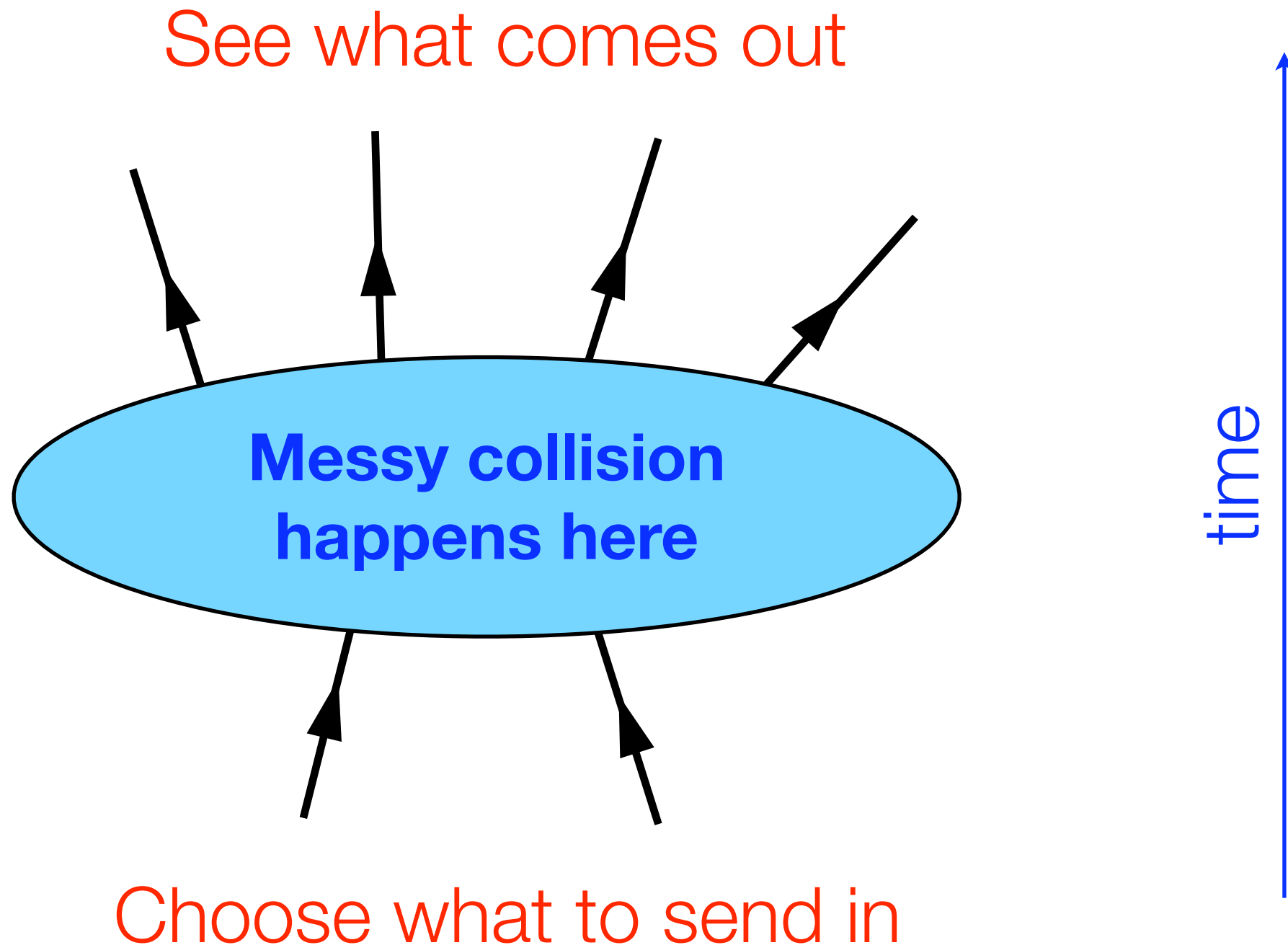


**THE**

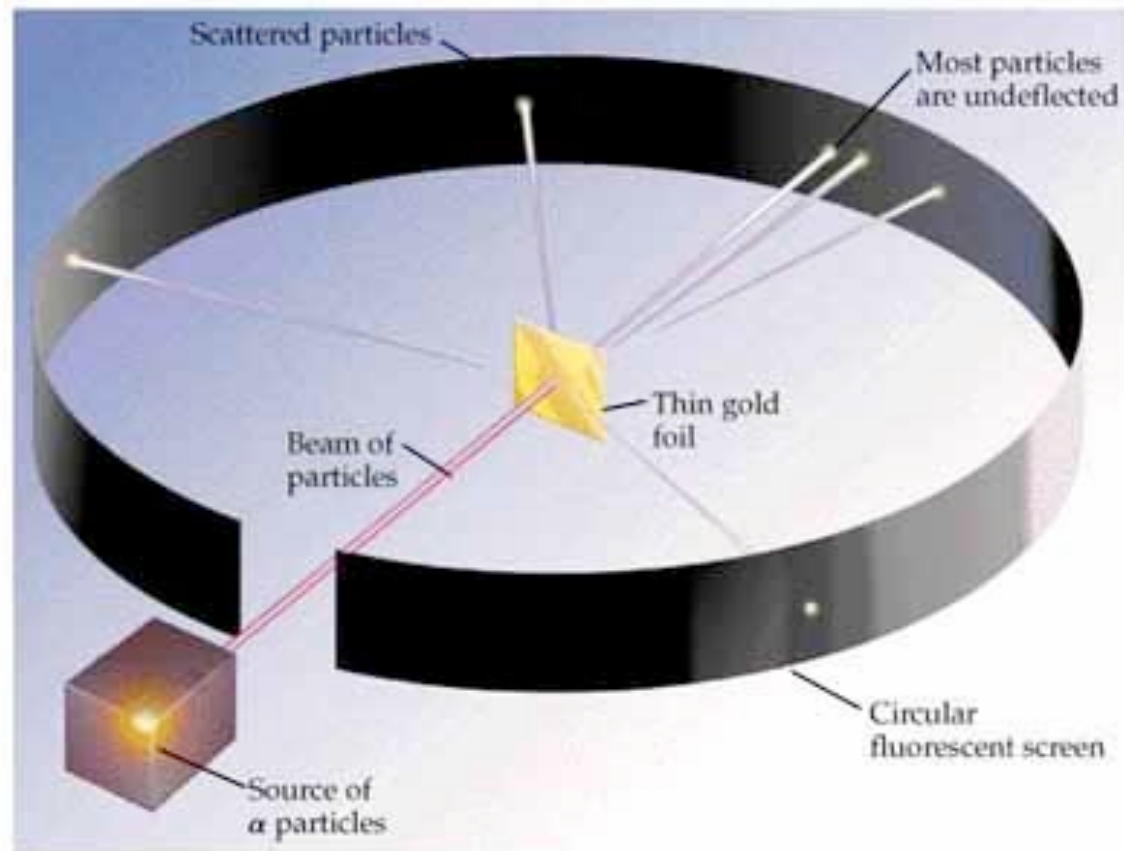
*Secret Life*

**OF SCATTERING AMPLITUDES**

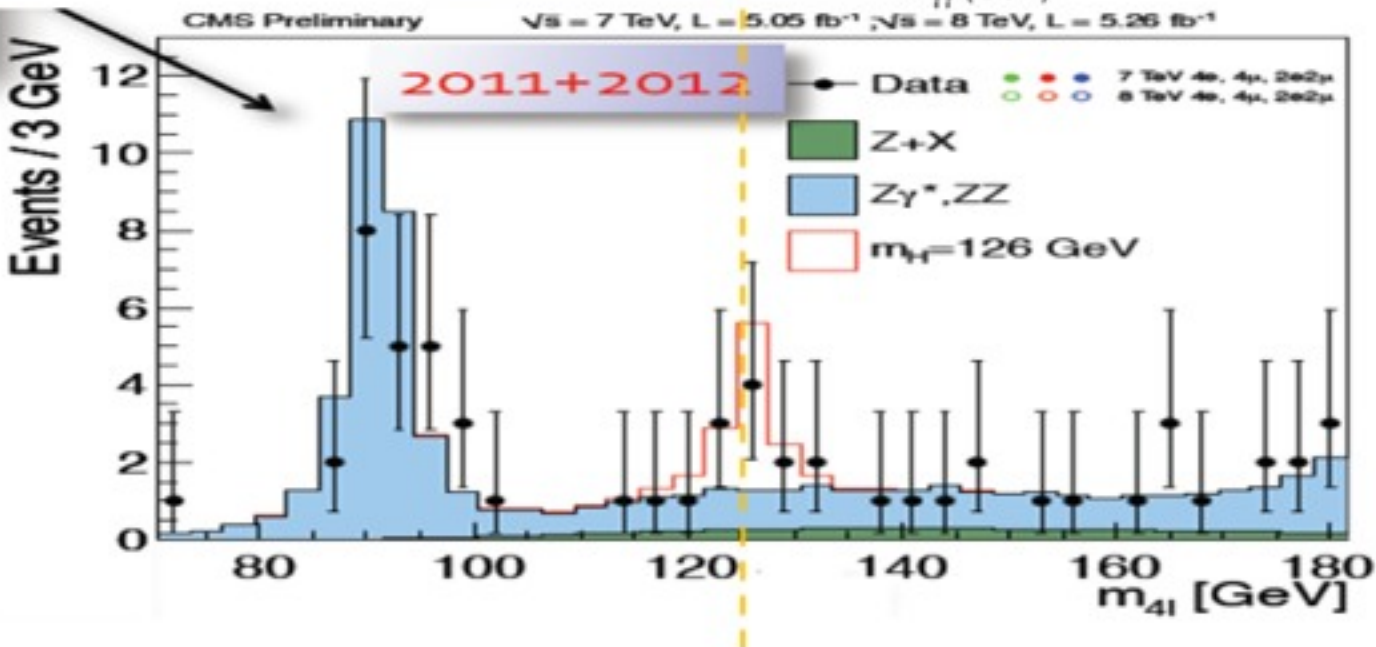
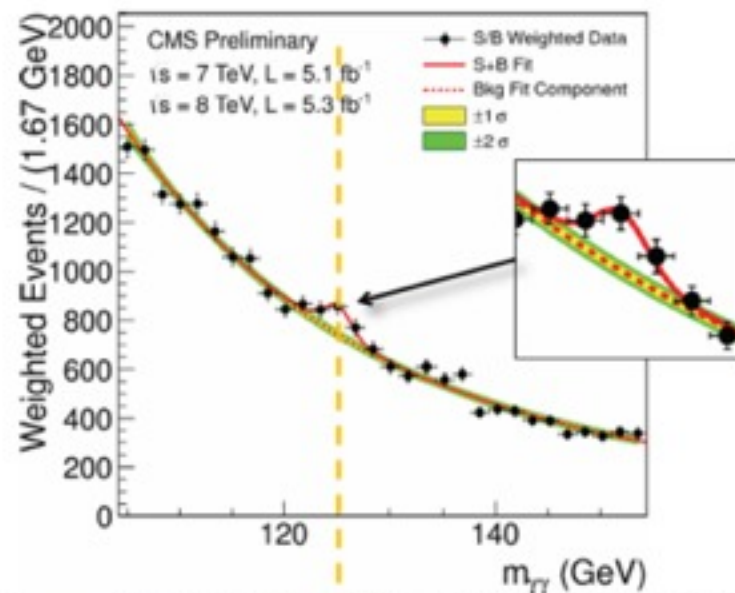
A scattering process is a description of what happens when stuff bumps into other stuff



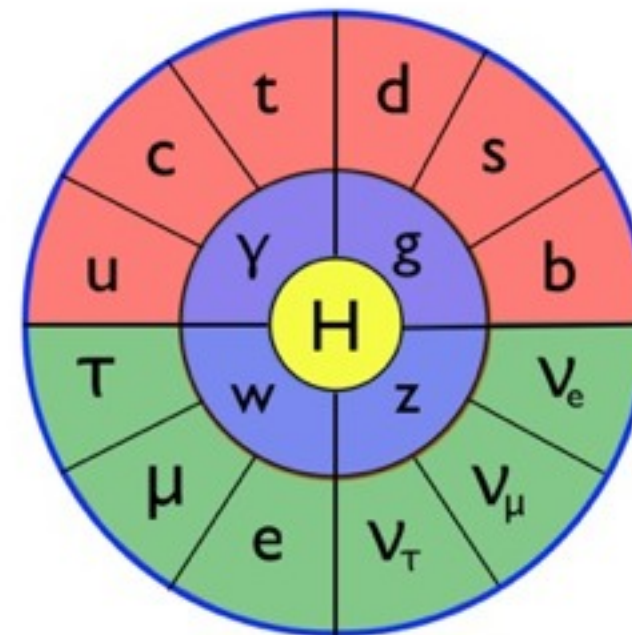
Rutherford discovered the atomic nucleus by scattering  $\alpha$ -particles off thin gold foil



*"It was quite the most incredible event that has ever happened in my life. It was almost as incredible as if you fired a 15-inch shell at a piece of tissue paper and it came back and hit you."*

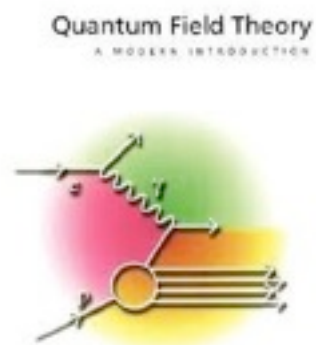
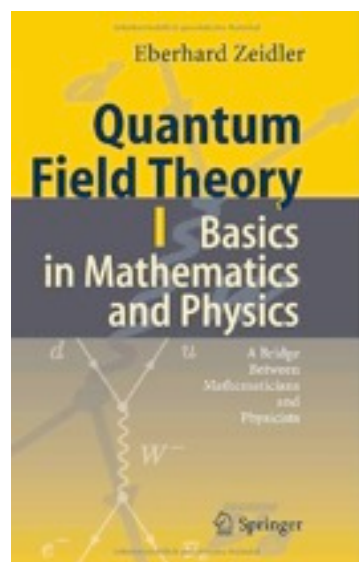


Most of what we know about the Standard Model - our best theory of particle physics - has been gleaned from scattering experiments

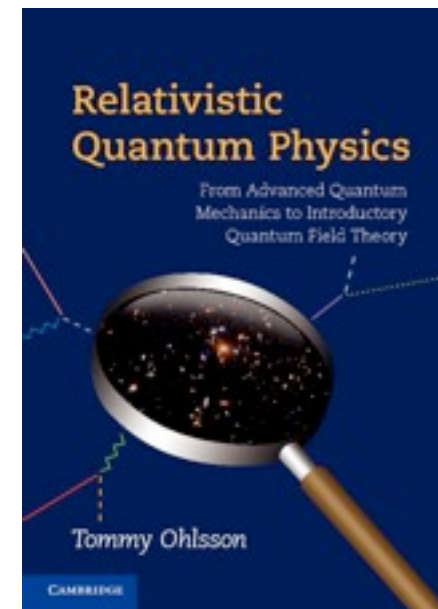
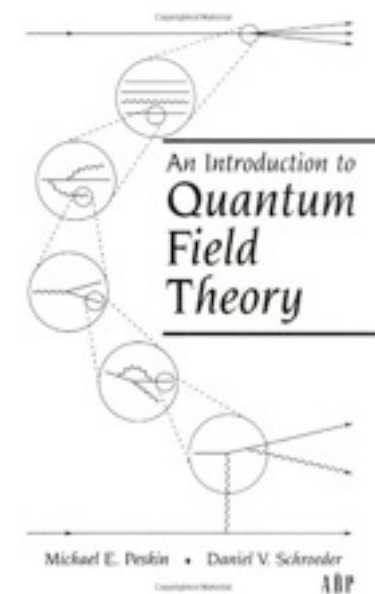
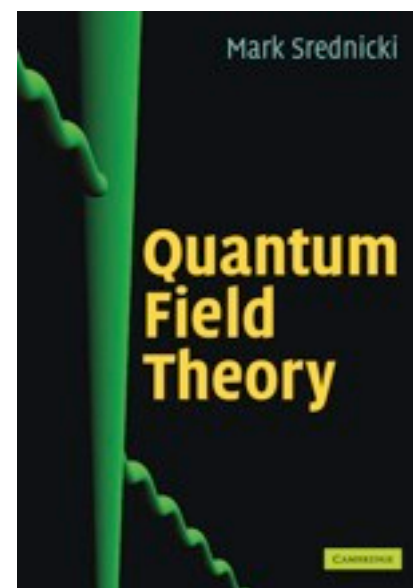
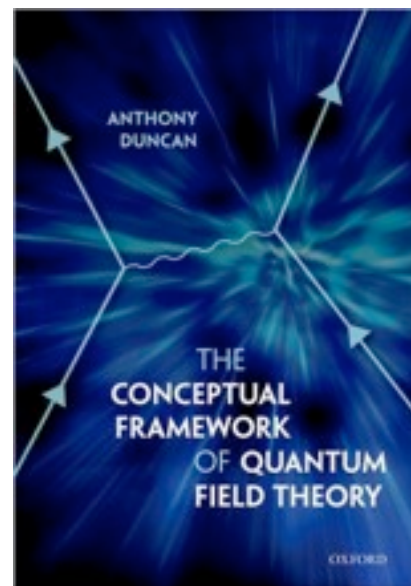


| Fermions | Bosons         |
|----------|----------------|
| Matter   | Force Carriers |
| Quarks   | Gauge bosons   |
| Leptons  | Higgs boson    |

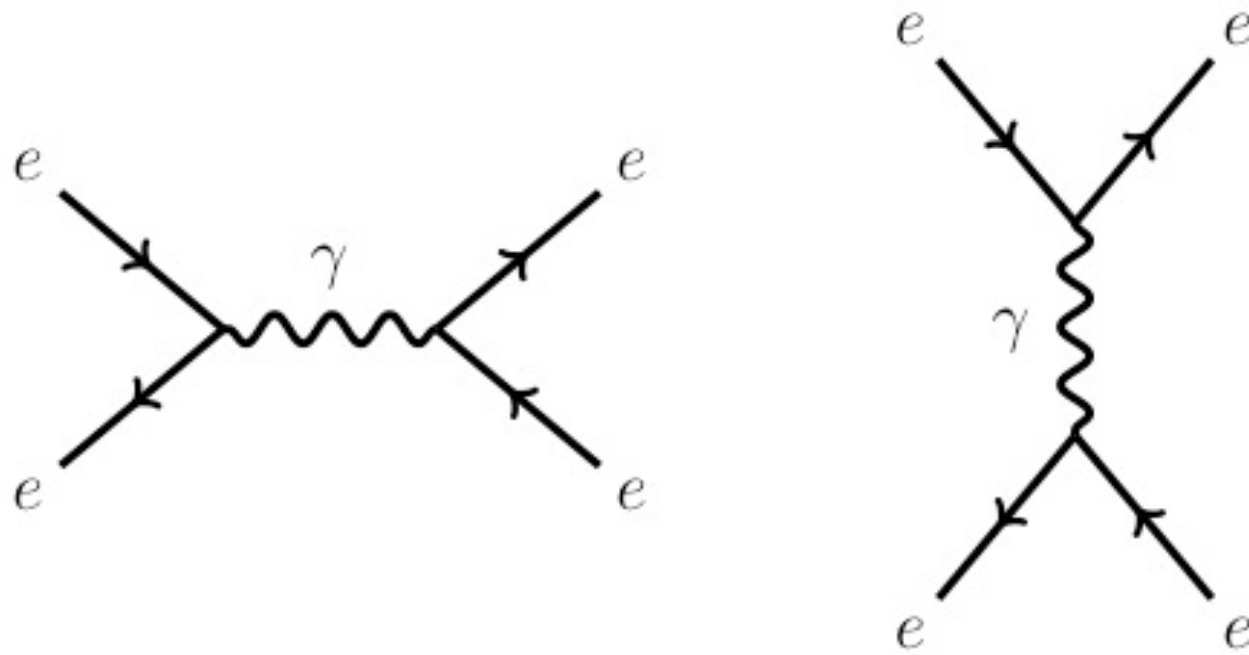
Particles of the Standard Model



Michio Kaku



You draw all diagrams with the same external lines; Feynman then tells you the amplitude



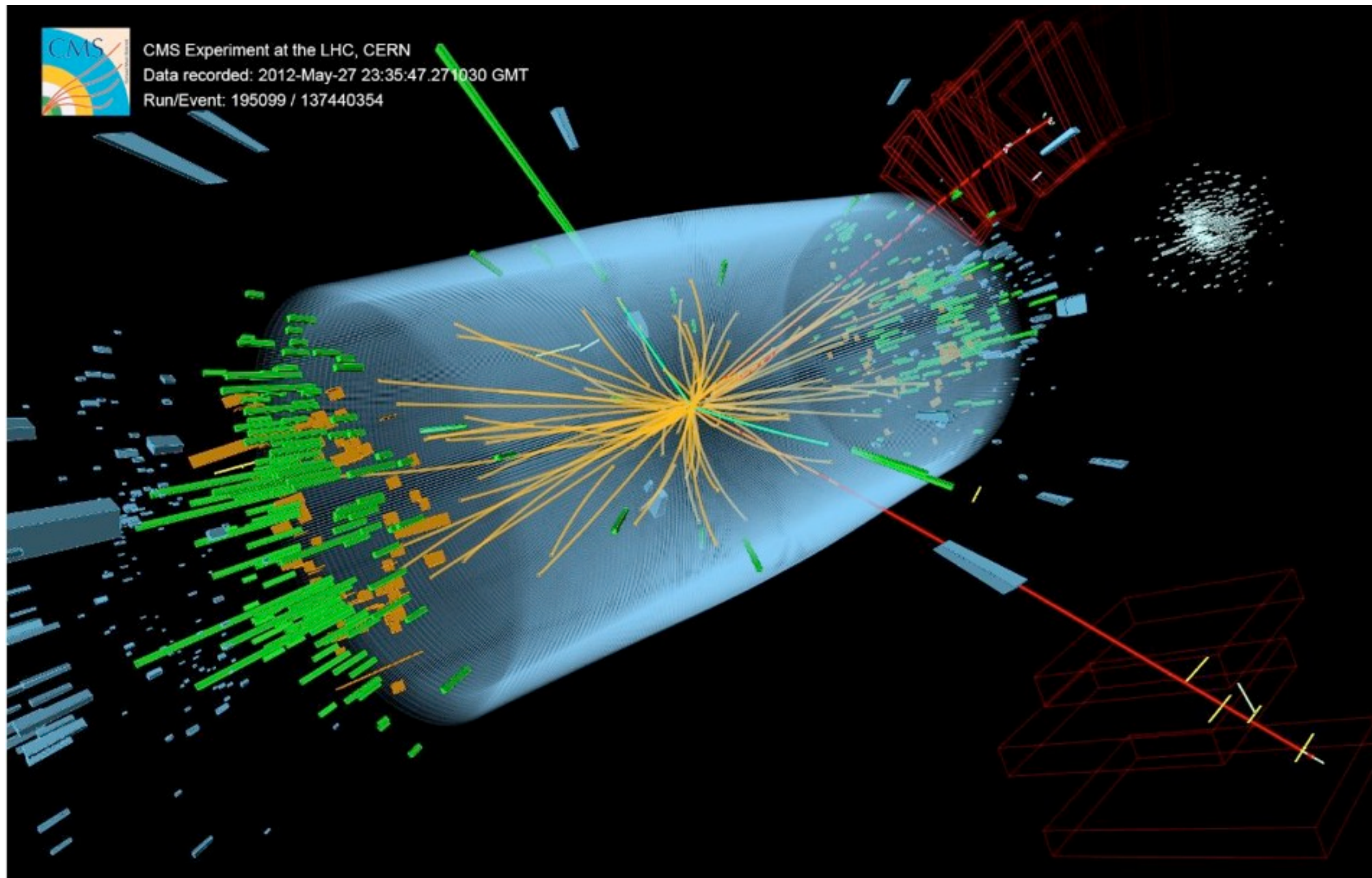
We teach these rules to our Part III students



- the reason they work  
was explained by Freeman  
Dyson in the late 1940s



CMS Experiment at the LHC, CERN  
Data recorded: 2012-May-27 23:35:47.271030 GMT  
Run/Event: 195099 / 137440354

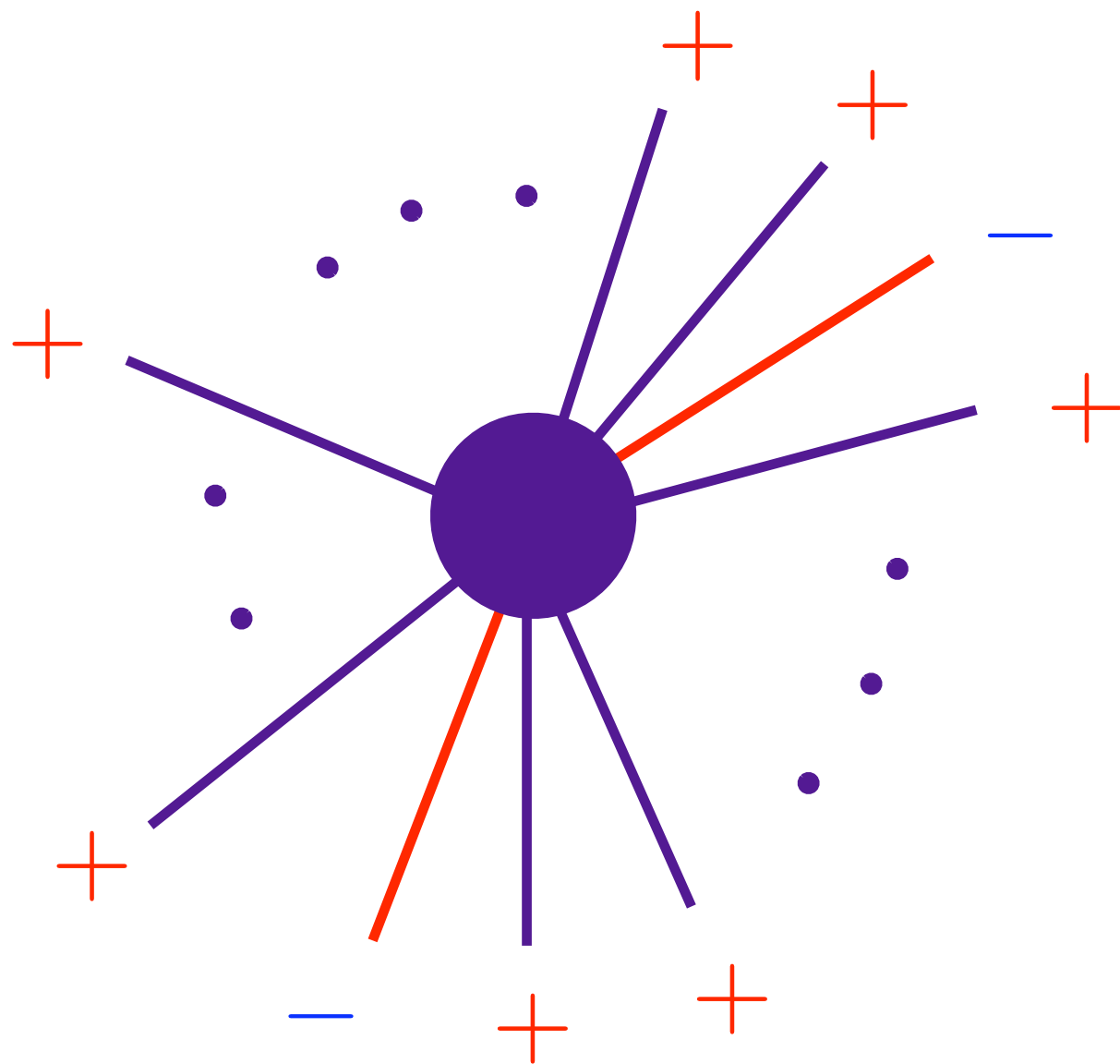


Result of a Feynman diagram calculation for  
2 particles producing a third in a QFT (YM):

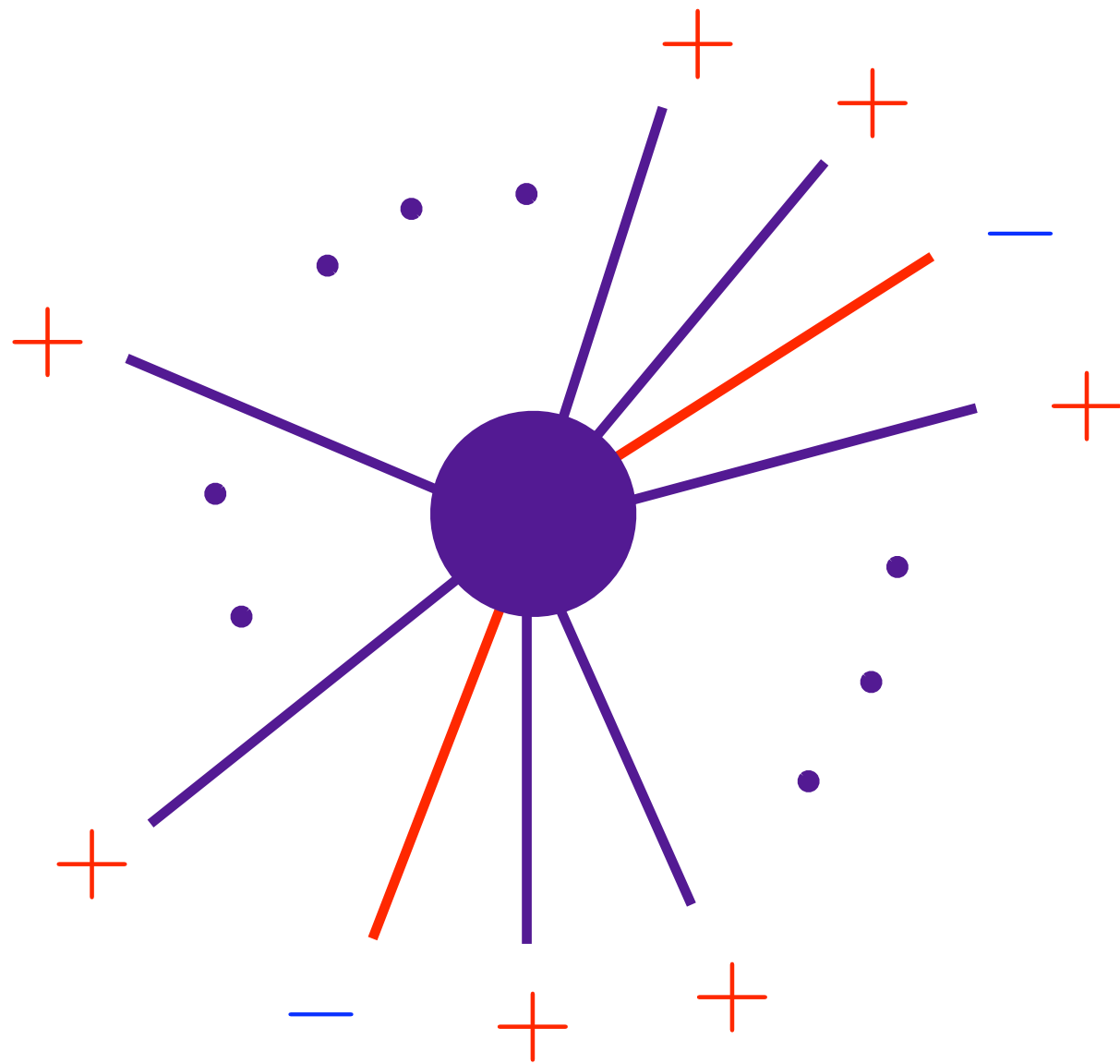
[illegible][illegible][illegible][illegible][illegible]
$$\begin{aligned} & + (c_1 - c_{12}c_2 - c_7c_8 - c_9 + c_{11} - c_6c_7 - c_2c_{10} - c_3 + c_7 - c_7c_{12} - c_7c_9 - c_6 + c_7 - c_3c_7 - c_4c_7 - c_8 + c_{11} - c_3c_{10} - c_{10}c_{12} - c_9)/(2d_1 - d_2) \\ & + (c_1 - c_6c_7 - c_7c_8 - c_2 + c_{11} - c_6c_7 - c_7c_{10} - c_2 + c_7 - c_{11}c_{12} - c_9 + c_7 - c_6c_7 - c_3c_7 - c_4 + c_7 - c_7c_7 - c_6)/(2d_1 - d_2) \\ & + (c_7 - c_{10}c_2 - c_7c_8 - c_7 + c_{11} - c_6c_7 - c_2c_{10} - c_2 + c_7 - c_{11}c_{12} - c_2c_{10} - c_2 + c_{11} - c_3c_7 - c_6c_{10} - c_8 + c_{11} - c_7c_{12})/(2d_1 - d_7) \end{aligned}$$

$$k_1 \cdot k_4 \varepsilon_2 \cdot k_1 \varepsilon_1 \cdot \varepsilon_3 \varepsilon_4 \cdot \varepsilon_5$$

+ seventeen more pages!



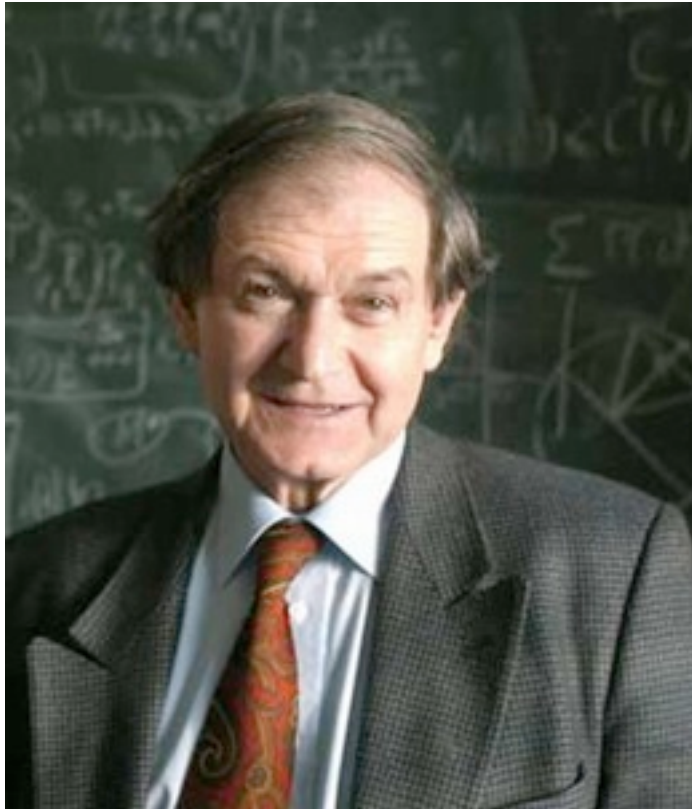
$$\frac{\langle ij \rangle^4 \delta^4(\sum p_i)}{\langle 12 \rangle \langle 23 \rangle \cdots \langle n1 \rangle}$$



$$\frac{\langle ij \rangle^4 \delta^4(\sum p_i)}{\langle 12 \rangle \langle 23 \rangle \cdots \langle n1 \rangle}$$

Why is the answer so simple?

# **TWISTOR THEORY**



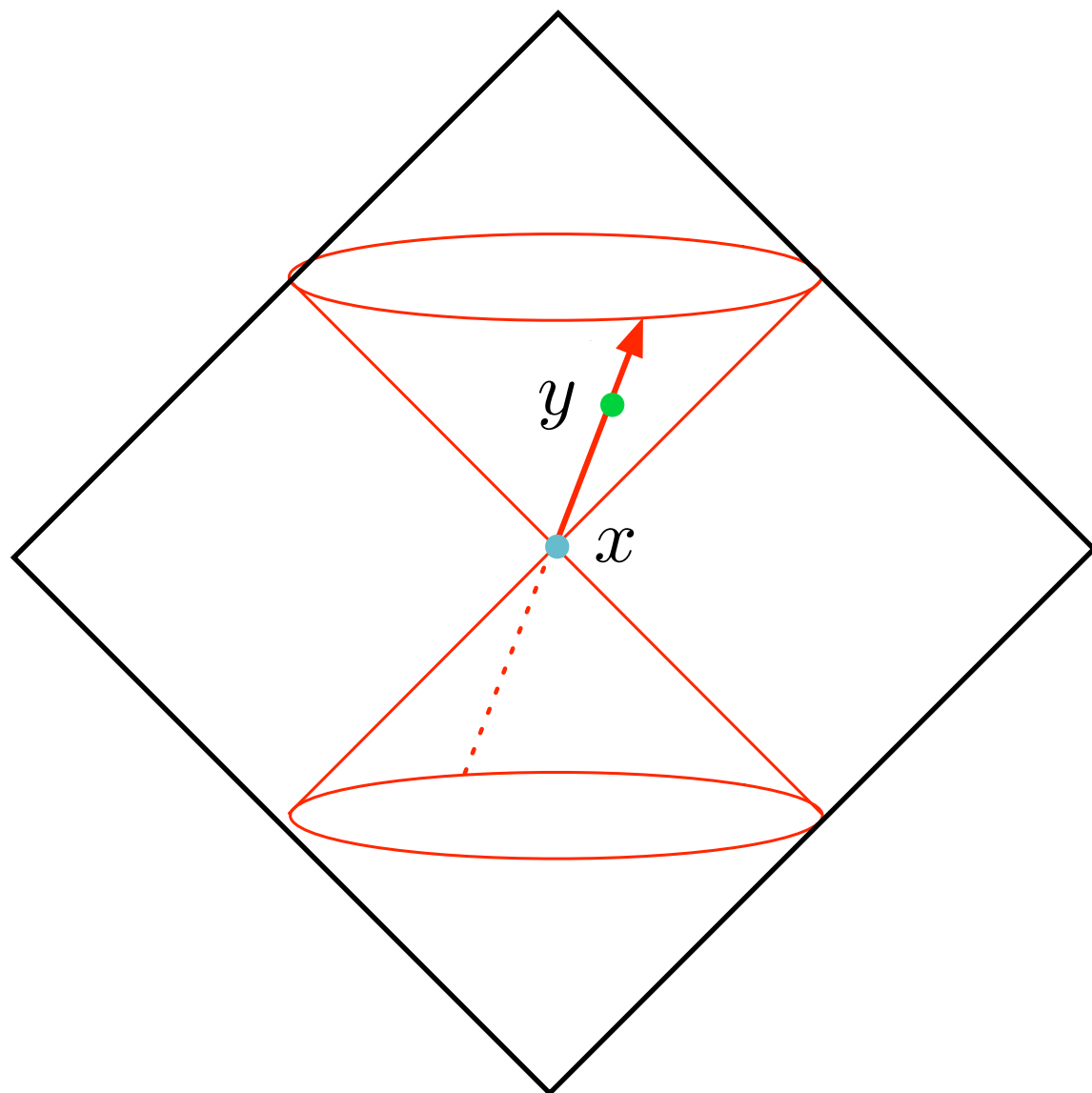
Twistors were developed in the 1970s by Penrose, intended as a new framework for physics

He wished to promote causal relationships between events above the events themselves



Thanks to Atiyah, Hitchin, Ward & many others they quickly found application in *mathematics*, but physics was slow to catch on...

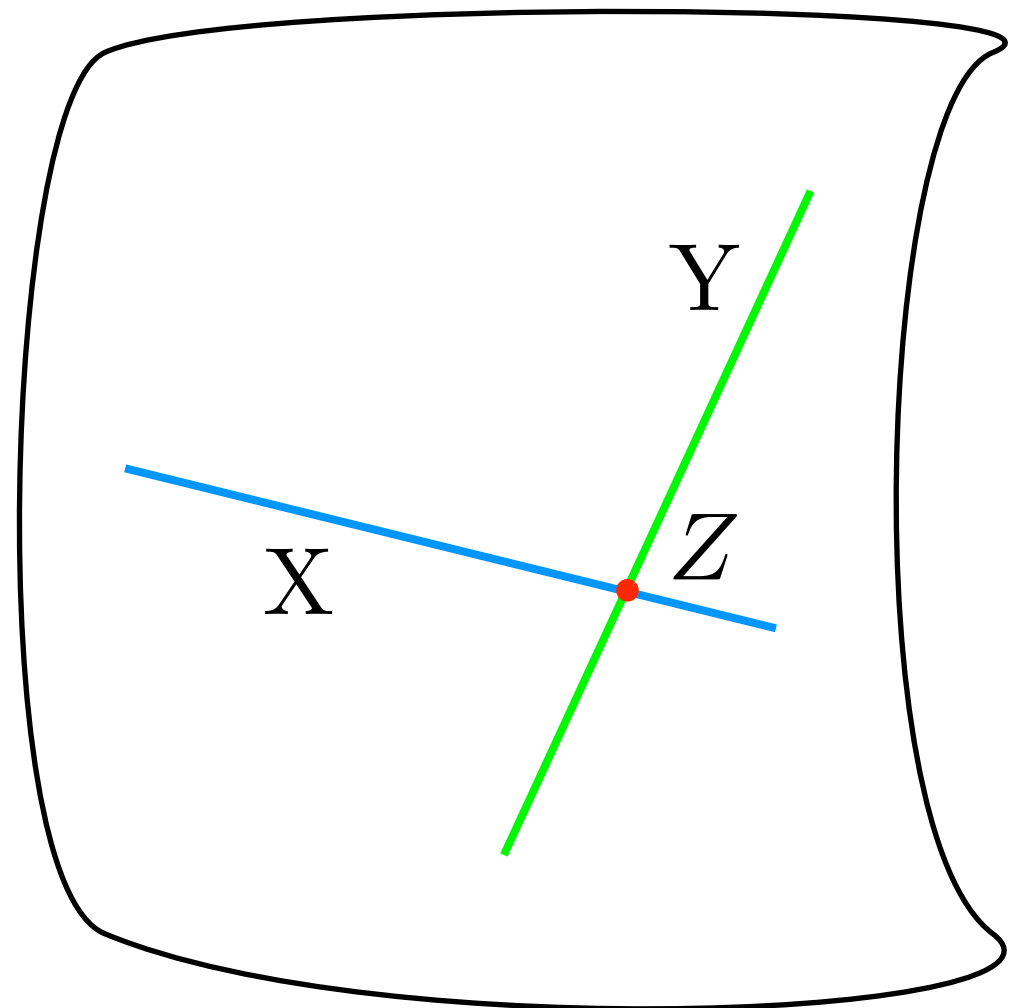
# Space-time



Point in space-time  
Separation is light-like

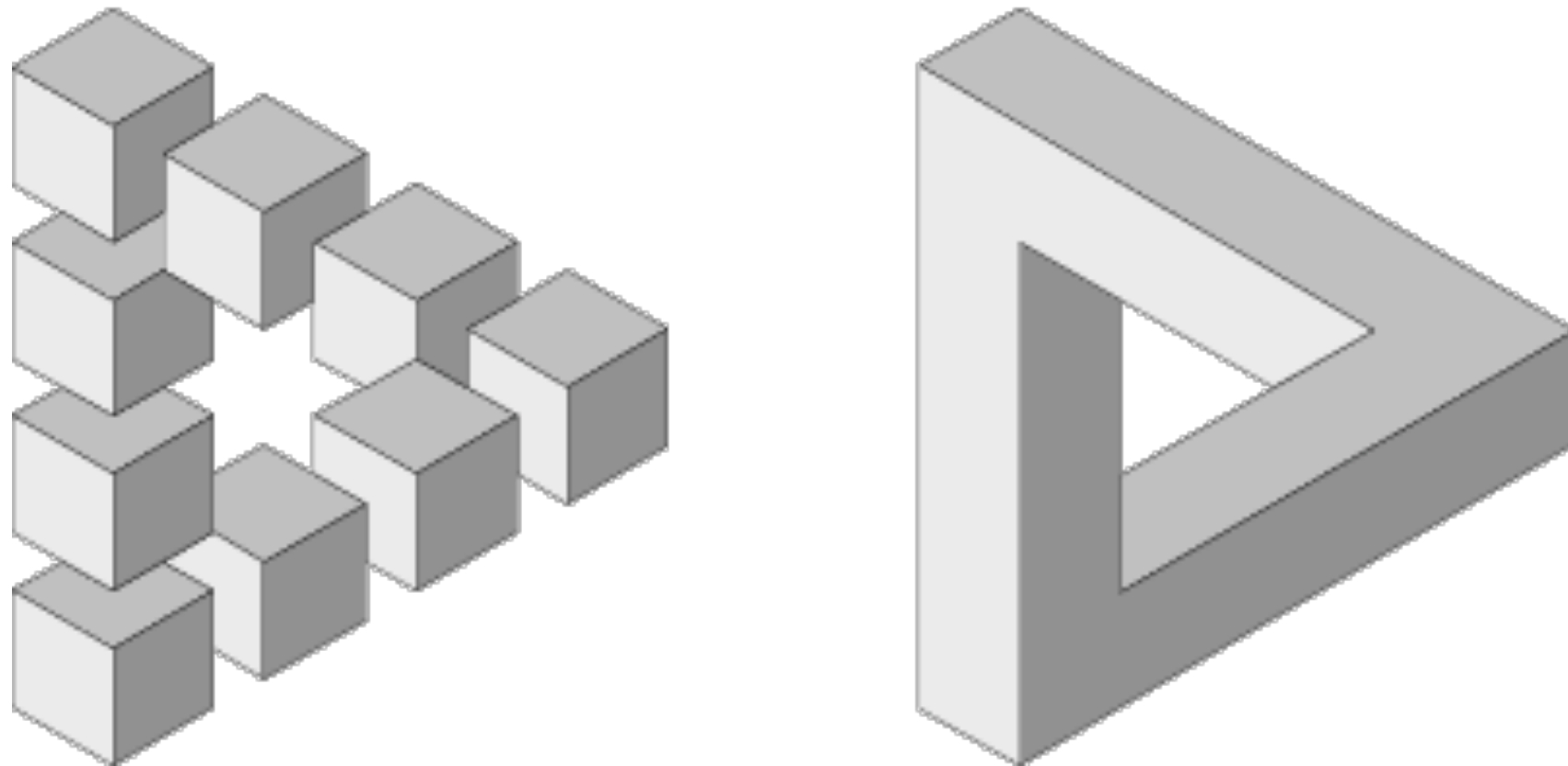


# Twistor space

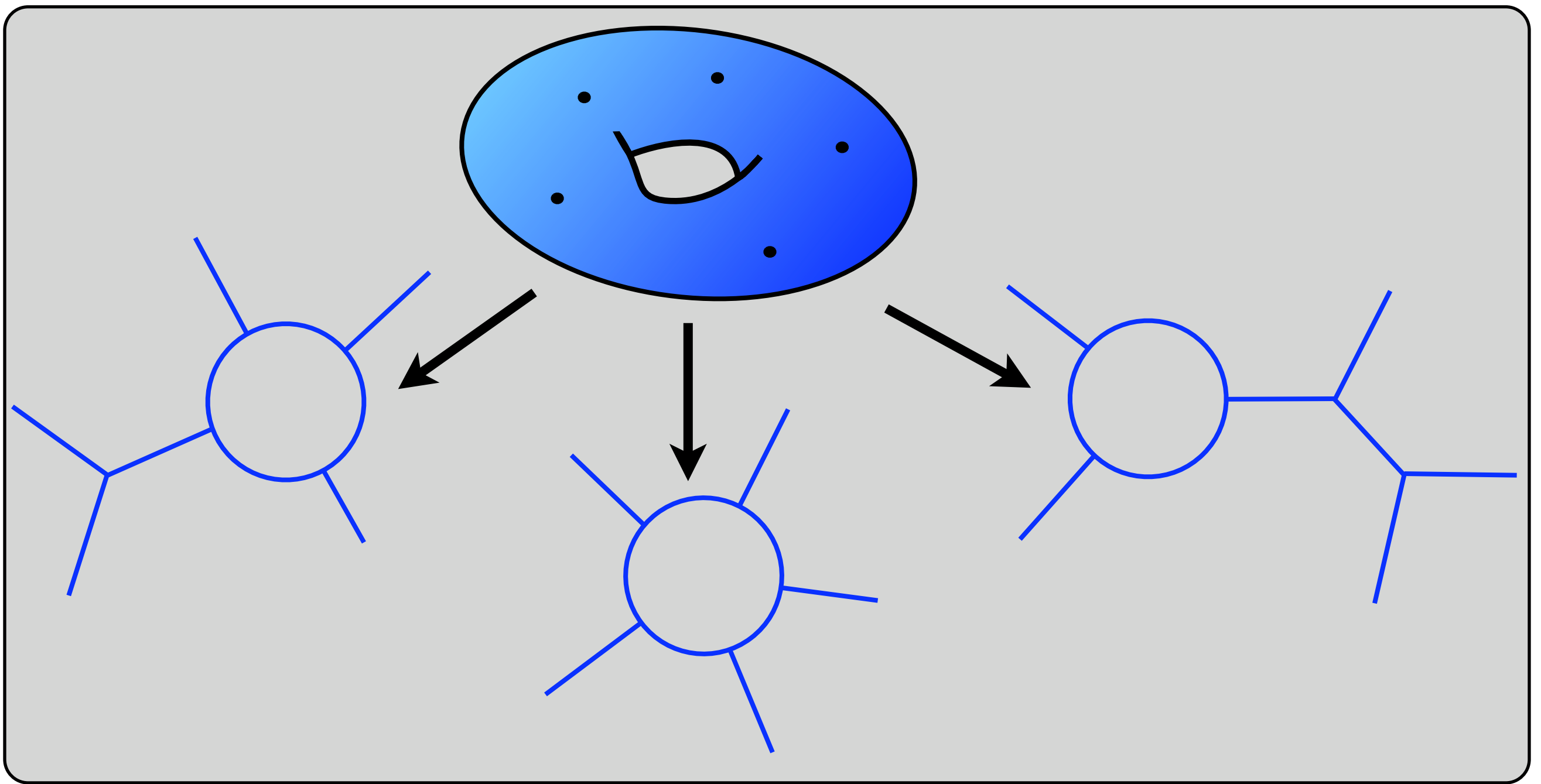


Sphere in twistor space  
Two spheres intersect

Physical objects are encoded in *global* properties of objects in twistor space



Physics is not described by point-like objects on twistor space: no “particles”

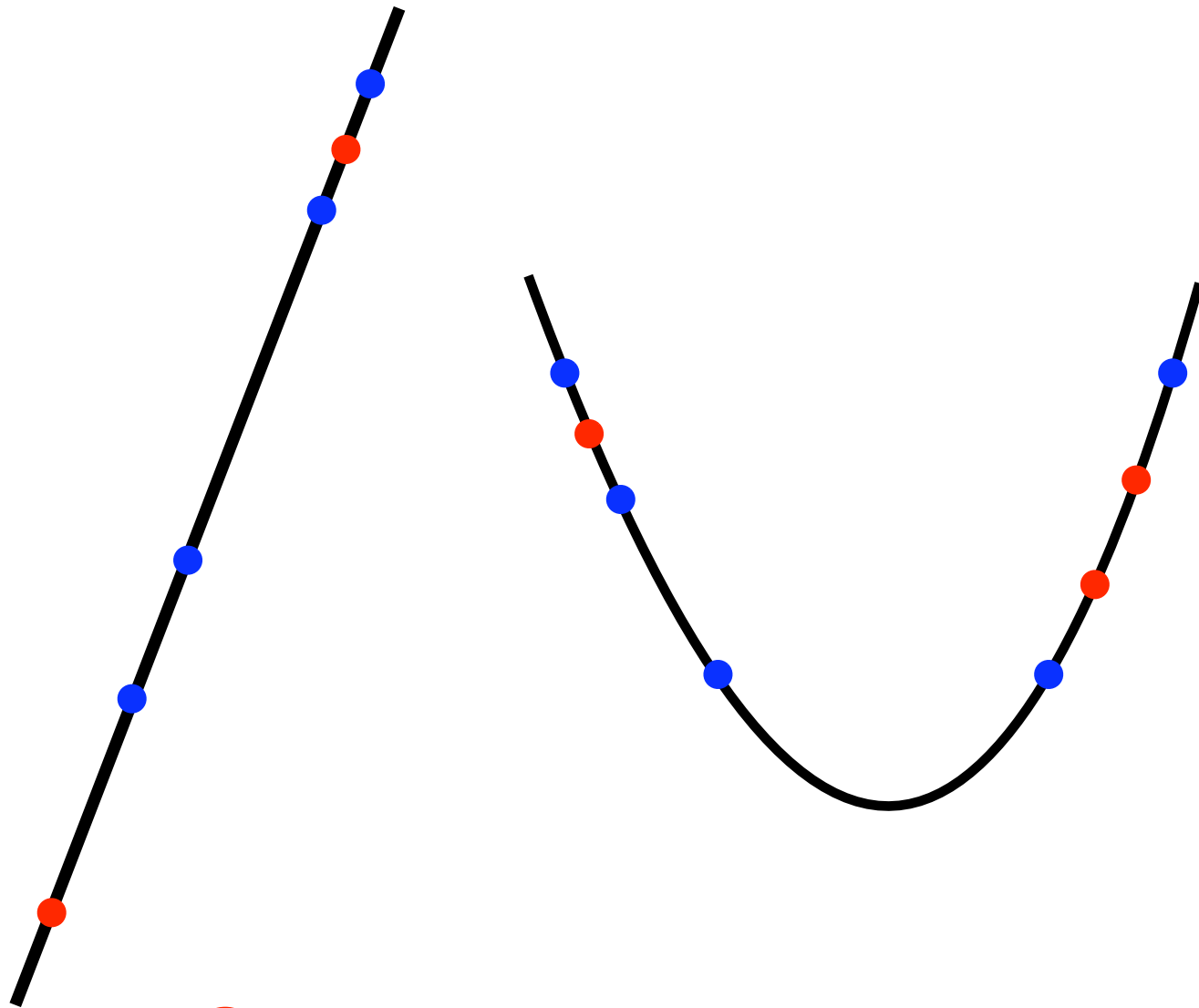


Replacing many Feynman diagrams with one single object is common in string theory, but at a high price:

10 dimensions

Infinitely many new  
types of particle

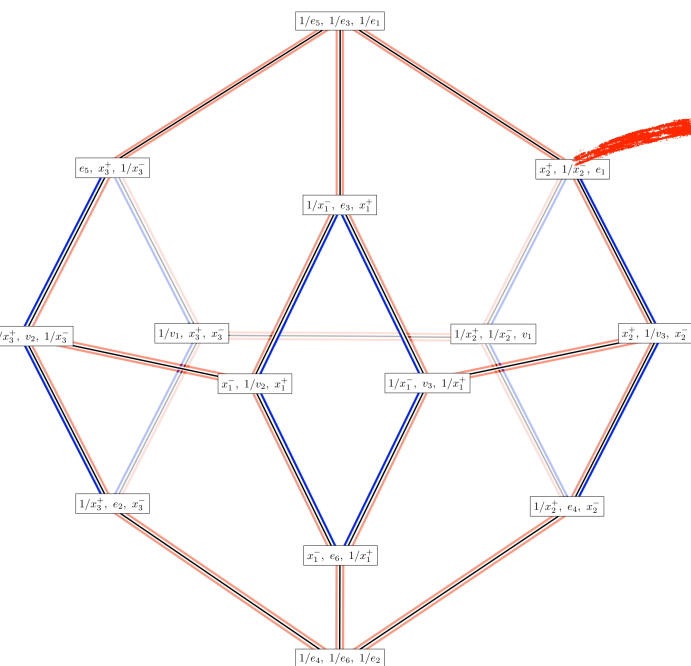
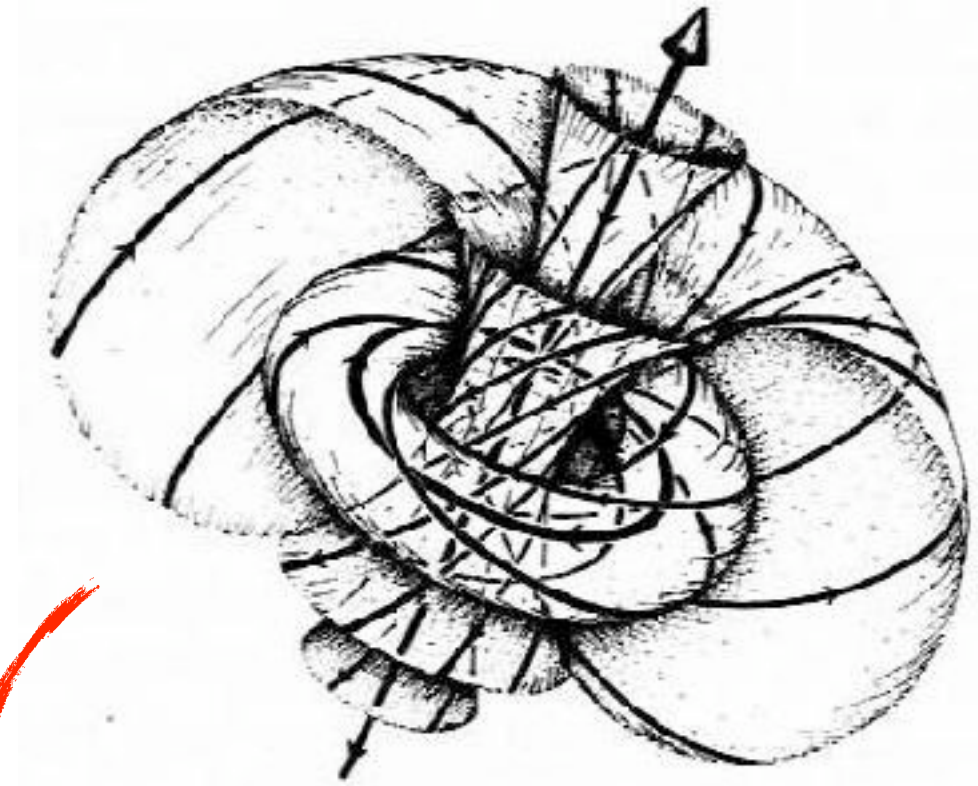
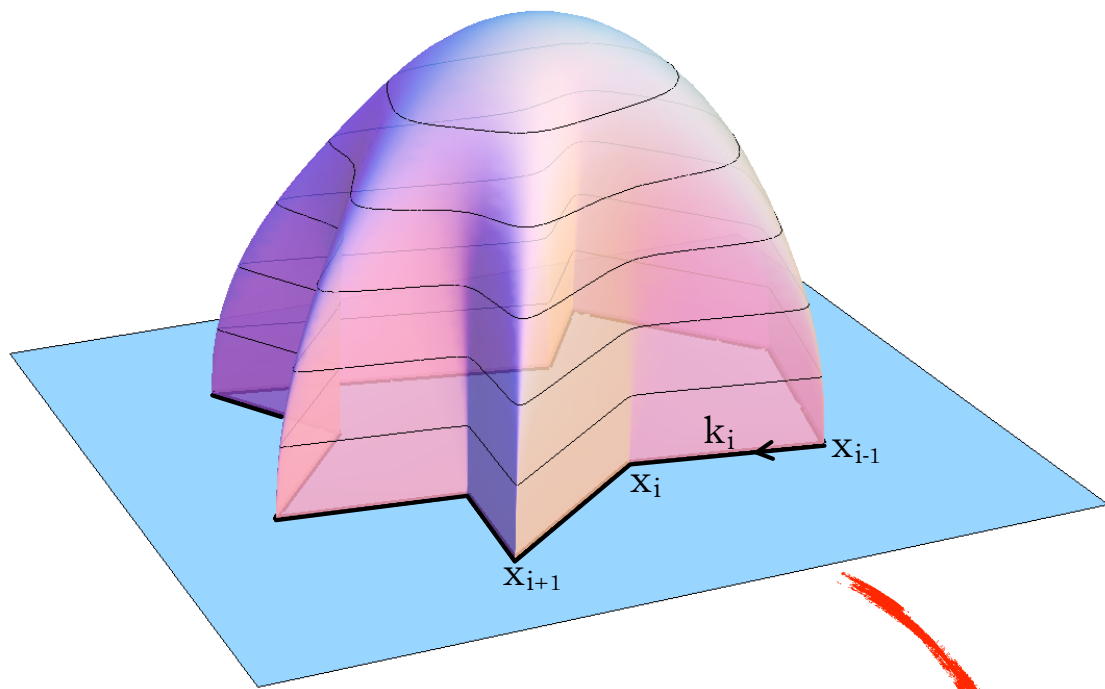
In late 2003, Witten realized that  
a string theory *in twistor space*  
was just what was needed



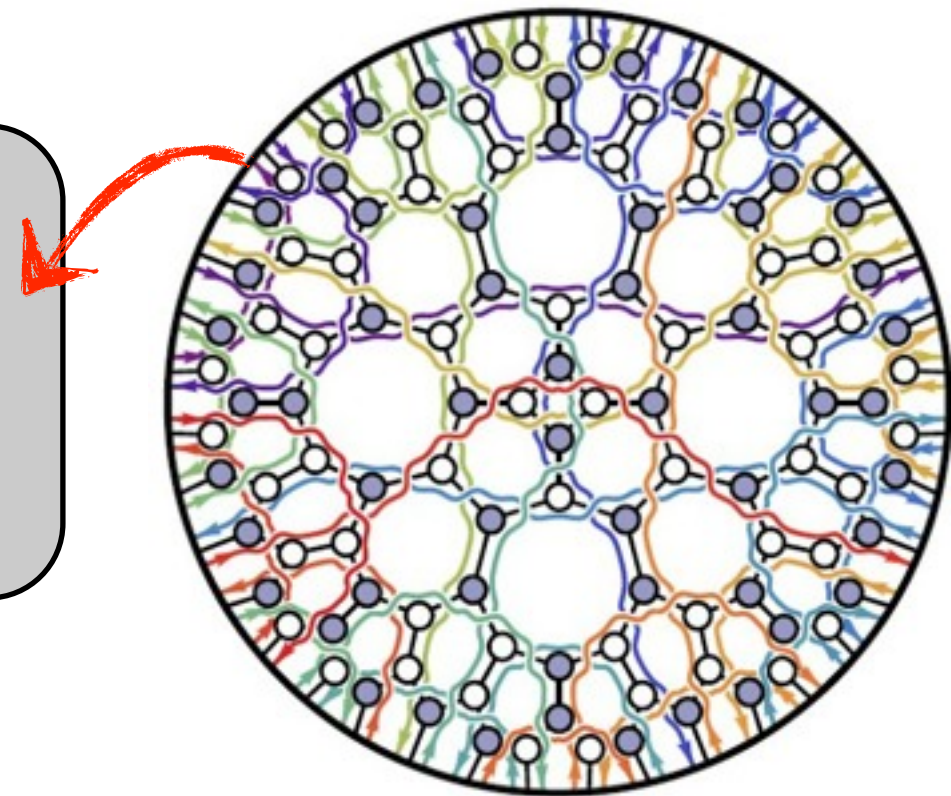
Only 3+1 dimensions

Only particles we've seen





# Scattering Amplitudes



Vast increase in technical power

New structures at the heart of QFT