Measurement of Cytoplasmic Streaming in Single Plant Cells by Magnetic Resonance Velocimetry

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In the giant cylindrical cells found in Characean algae, multitudes of the molecular motor myosin transport the cytoplasm along opposing spiralling bands covering the inside of the cell wall, generating a helical shear flow in the large central vacuole. Such flows have been suggested to enhance mixing within the vacuole (Phys. Rev. Lett. 101, 178102 (2008)) and thereby to play a role in regulating metabolism. For this to occur the membrane that encloses the vacuole, the tonoplast, must transmit efficiently the hydrodynamic shear generated in the cytoplasm. Existing measurements of streaming flows are of insufficient spatial resolution and extent to provide tests of fluid mechanical theories of such flows and information on the shear transmission. Here, using magnetic resonance velocimetry (MRV), we present the first measurements of cytoplasmic streaming velocities in single living cells. The spatial variation of the longitudinal velocity field in cross sections of internodal cells of Chara corallina is obtained with 16 µm spatial resolution, and shown to be in quantitative agreement with a recent theoretical analysis (Proc. Natl. Acad. Sci. USA 105, 3663 (2008)) of rotational cytoplasmic streaming driven by bidirectional helical forcing in the cytoplasm, with direct shear transmission by the tonoplast. These results highlight the open problem of understanding tonoplast motion induced by streaming. Moreover, this study suggests the suitability of MRV in the characterisation of streaming flows in a variety of eukaryotic systems, and for microfluidic phenomena in general.

1. Introduction

The Characean algae comprise a family of aquatic plants that grow segmented branches, built up from exceptionally large single cells several centimetres in length (figure 1). The contents of these cells undergo an active and highly steady circulation known as cytoplasmic streaming, driven by the motion of the motor protein myosin along bundles of actin filaments at the cell’s periphery. Characean cells have been studied since the early days of microscopy (Corti 1774) and the species are recognised as the closest genetic relatives of land plants (Karol et al. 2001). Charophytes function as a model system for

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FIGURE 1. Geometry of Chara corallina. (a) A branch showing internodal cells separated by nodes from which so-called branchlet cells grow in several directions (b) Cross-section of a Chara internode. Flow is driven in opposing directions along two helical bands separated by indifferent zones visible as light lines on the surface. Velocities are generated in a 10 µm thick layer of cytoplasm at the periphery, but a shear flow extends into the central vacuole that takes up 95% of the volume of the cell. (c) Microscopy image of the sample prior to insertion into the glass tube. The dotted line shows a spiral of dimensionless wavelength $\lambda/R = 42$. (d) Schematic of sample holder enclosed in a horizontal RF coil. The length of the tube is 40 mm.

studies on electrophysiology (Shimmen et al. 1994), intercellular transport (Lucas 1995), and carbon fixation in photosynthesis (Lucas 1975).

Cytoplasmic streaming, also known as cyclosis, is implicated in transport of nutrients towards regions of growth (Ding et al. 1991). It is also hypothesised to aid homeostasis, the stable regulation of metabolite concentrations, by enhancing intracellular mixing (Hochachka 1999). In their seminal work on the phenomenon, Kamiya & Kuroda (1956) established that cytoplasmic streaming in Characean algae takes place not only in the cytoplasm, but also produces fluid flows that extend throughout the entire vacuole. As pointed out long ago (Pickard 1972) this result implies that the vacuolar membrane (the tonoplast) efficiently transmits shear generated in the cytoplasm (Houtman et al. 2007) to the vacuole (figure 1b). While membranes flow under shear is well-known from the "tank-treading" of erythrocytes (Fischer et al. 1978), it is clear from recent studies of lipid vesicles under extensional flows (Kantsler et al. 2007) that sheared membranes can undergo instabilities that lead to complex dynamics. With the ability to image the dynamics of the tonoplast directly in Arabidopsis by means of a green-fluorescent-protein-labelled tonoplast integral channel protein (Cutler et al. 2000), there is fairly clear evidence that such complex dynamics do take place in vivo (VerbeLEN & Tao 1998), and these may have implications for flows throughout the cell. In Chara corallina, for example, the actin-myosin system driving streaming is localised in two opposed helical bands at the cell periphery; the high shear where they meet may create complex tonoplast dynamics.

The possibility that streaming may impact on cellular metabolism by mixing the contents efficiently (Hochachka 1999; Pickard 2006) has been revisited recently through solutions of the coupled advection-diffusion dynamics of rotational cytoplasmic streaming (Goldstein et al. 2008; van de Meent et al. 2008). These calculations of velocities throughout the vacuole assumed that shear transmission by the tonoplast was complete, and showed that vacuolar flows can produce enhanced mixing, providing a possible mechanism for the homeostatic role hypothesised by Hochachka. The first direct measurements of the wall-to-wall velocity profile are those of Kamiya & Kuroda (1956), who studied rhizoid cells, ‘leaf’ cells sprouting from nodes, and internodal cells, and found a constant velocity within the cytoplasm and a curved shear profile within the vacuole. Mustacich &
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Ware (1976) improved on these measurements by using laser-Doppler scattering through a chloroplast-free window obtained by exposure to an argon laser prior to observation. Pickard (1972) obtained velocity measurements for a collection of native particles in an internodal cell of Chara braunii, showing consistency with the velocity deduced under the approximation of non-helical indifferent zones.

While existing measurements are compatible with the simplest hydrodynamic descriptions, no full 2-dimensional measurements of the cross-sectional flow profiles have been presented to date in any single living cell. Here we report a technical advance in the study of cytoplasmic streaming by obtaining the fluid velocity in internodal cells in Chara corallina directly with magnetic resonance velocimetry (MRV). Our results allow for quantitative tests of recent fluid dynamical theories (Goldstein et al. 2008; van de Meent et al. 2008) and suggest further uses for magnetic resonance imaging (MRI) in the study of large-scale streaming flows.

In recent years, MRI techniques have increasingly found use in non-medical applications (Elkins & Alley 2007), and the advent of phase-shift MRV has made it possible to perform non-invasive flow measurements on microscopic scales (Callaghan 1993). In MRV the initial application of a pulsed magnetic field gradient encodes each spin with a ‘label’ describing its position along the direction of the gradient. At a time Δ later (the “observation time”), a reversed gradient is applied, introducing a net phase shift in the orientation of the nuclear spin system that is directly related to the distance travelled in the direction of the gradient. By careful selection of the magnitude of the applied field gradients and the observation time, velocities from \( \sim 10^{-5} \) – \( 10^{-1} \) m/s can be measured, depending on fluid properties. The capabilities of MRV have already found application in a range of settings which aid the development and validation of numerical codes or theoretical models; for example, the visualisation of microfluidics flows (Akpa et al. 2007), the imaging of structure and convection in solidifying mushy layers (Aussillous et al. 2006), bifurcation phenomena in the flow through a sudden expansion in a circular pipe (Mullin et al. 2009), and velocity distributions within a three-dimensional vibro-fluidized bed (Huntley et al. 2007). With sufficient time-averaging, spatial resolutions of 10 – 100 \( \mu \)m can be achieved, allowing imaging of biological systems on scales just slightly larger than those of typical single cells (Choma et al. 2006). This has allowed measurements at tissue level in a variety of plant systems (Scheenen et al. 2001; Kockenberger et al. 2004; Windt et al. 2006), it is in the uniquely sized internodes of Chara that we can obtain measurements of flows internal to single cells.

2. Cylindrical Stokes Flow with Helical Wall Forcing

The Characean internode (figure 1b) is a single cylindrical cell with a diameter up to 1 mm and a length that can exceed 10 cm. The bulk of the volume is occupied by a large central vacuole (figure 1c) that fulfills a multitude of metabolic roles, acting as storage compartment for sugars, polysaccharides, and organic acids, sequestering toxins such as heavy metals, and functioning as a buffering reservoir that helps to maintain ionic and pH homoeostasis in the cytoplasm (Taiz 1992). Additionally, the 0.13M concentration of salts in the vacuolar fluid (Tazawa 1964) produces an outward osmotic pressure of 5 bars that lends the cell its rigidity. At the cell periphery, a layer of cytoplasm of roughly 10 \( \mu \)m in thickness encloses the vacuole. In Charophytes most organelles common to higher plants are found in the cytoplasm. Somewhat uniquely, the millions of chloroplasts cover the cell wall, packed into helical rows that spiral along the inner surface (figures 1b,c). On the inside of those rows, bundled actin filaments act as tracks for myosins that drag structures within the cell (Kachar 1985; Kachar & Reese 1988) and thereby entrain...
cytoplasm. With streaming rates as high as 100 μm/s, the myosin XI found in Chara is the fastest known (Shimmen & Yokota 2004). As a result of a reversed polarity of the actin filaments, the flow is organised in two opposing bands, producing a “barber-pole” velocity at the cell periphery. These bands are separated by indifferent zones, identifiable by the absence of chloroplasts and visible as two light lines crossing the cell surface.

From a hydrodynamic perspective, the geometry of Characean internodes naturally lends itself to a description as a helical shear flow, where the cytoplasmic bands impose a constant velocity at the boundaries. As typical Reynolds numbers are about 0.03, the problem is most readily treated as a Stokes flow in a cylinder, which can be solved as an expansion in Fourier-Bessel modes (Meleshko et al. 2000) where the velocity at the boundary may be used to close a system of linear equations in the coefficients.

For the purposes of studying the flow away from the end-points we can approximate the geometry as an infinite cylinder, since the aspect ratio of these cells generally lies upwards of 30. This has the advantage that it allows simplification of the problem to a three-dimensional flow with helical symmetry, where the Stokes equations depend only on the radial coordinate \( r \) and a helical angle \( \varphi = \theta - (2\pi/\lambda)x \), which is the polar angle \( \theta \) offset by the rotation of the helical bands, with wavelength \( \lambda \). The problem then reduces to solving the equations

\[
\eta \nabla^2 u(r, \varphi) = \nabla p(r, \varphi) , \quad \nabla \cdot u(r, \varphi) = 0 .
\]

The basis vectors of the coordinate system can be expressed in terms of the cylindrical coordinates \((r, \theta, z)\) as

\[
e_r = e_r , \quad e_\varphi = \frac{1}{h}(e_\theta - \kappa re_z) , \quad e_H = \frac{1}{h}(\kappa re_\theta + e_z) ,
\]

where

\[
\kappa = \frac{2\pi}{\lambda} , \quad h = \frac{1}{\sqrt{1 + \kappa^2 r^2}} .
\]

The helical symmetry implies a natural decomposition into a downstream component \( v \) along the axis of helical symmetry \( e_H \) and the gradient of a stream-function \( \Psi \) containing the transverse components of flow (van de Meent et al. 2008):

\[
u = v(r, \varphi)e_H - \frac{1}{h}\nabla\Psi(r, \varphi) \times e_H .
\]

The boundary velocity at \( r = R \) is taken to be piecewise constant value \( U \) over the top and bottom domains \( \varphi = [0, \pi] \) and \( \varphi = [\pi, 2\pi] \). At the indifferent zones located at \( \varphi = 0 \) and \( \varphi = \pi \), the direction of flow reverses over a narrow neighbourhood \( \epsilon \) of order 10 μm. Rather than approximating the boundary velocity with a step-function, with poor convergence of the Fourier expansion due to ringing artifacts, we use a hyperbolic-tangent dependence near the indifferent zones to obtain a continuous cross-over:

\[
v(R, \varphi) = \begin{cases} 
U \tanh(\varphi/\epsilon) & 0 \leq \varphi < \pi/2 \\
-U \tanh((\varphi - \pi)/\epsilon) & \pi/2 \leq \varphi < 3\pi/2 \\
U \tanh((\varphi - 2\pi)/\epsilon) & 3\pi/2 \leq \varphi < 2\pi 
\end{cases} .
\]

Following Meleshko et al. (2000), the hydrodynamic solution can thus be obtained from the boundary conditions as a mode expansion (Goldstein et al. 2008). Because of the additional terms in the Laplacian and gradient operators in the helical coordinates, the problem is most easily treated in cylindrical coordinates. The \( \theta \) and \( z \) dependence in the general solution takes the form of a double sum over Fourier modes. In our particular case the symmetry of the problem implies that only combinations of modes that depend
on $\varphi = \theta - \kappa z$ contribute to the solution. Performing one of the two sums yields

$$u_r(r, \varphi) = \sum_{n \text{ odd}} u^o_r(r) \cos(n\varphi), \quad u_\theta(r, \varphi) = \sum_{n \text{ odd}} u^o_\theta(r) \sin(n\varphi), \quad (2.6a)$$

$$u_z(r, \varphi) = \sum_{n \text{ odd}} u^o_z(r) \sin(n\varphi), \quad p(r, \varphi) = \sum_{n \text{ odd}} \eta P^n(r) \cos(n\varphi). \quad (2.6b)$$

The fact that the two bands are identical up to a reversal in the direction of flow implies a pseudo-symmetry $v(R, \varphi) = -v(R, -\varphi)$ in the boundary conditions, which means only the odd terms in the sum need to be considered.

To find the radial modes, we write $u^o_r = -(a^n + b^n)/2$ and $u^o_\theta = -(a^n - b^n)$, after which the solution takes the form of a combination of modified Bessel functions,

$$u^o_r(r) = \frac{1}{I_n(\kappa R)} \left[ A^n I_{n+1}(\kappa nr) + \frac{P^n \kappa L}{2\pi} I'_{n+1}(\kappa nr) \right], \quad (2.7a)$$

$$b^o_r(r) = \frac{1}{I_n(\kappa R)} \left[ B^n I_{n-1}(\kappa nr) + \frac{P^n \kappa R}{2\pi} I'_{n-1}(\kappa nr) \right], \quad (2.7b)$$

$$u^o_z(r) = -\frac{1}{I_n(\kappa R)} \left[ C^n I_n(\kappa nr) + \frac{P^n \kappa}{2\pi} I'_{n}(\kappa nr) \right], \quad (2.7c)$$

$$p^o_r(r) = -\frac{1}{I_n(\kappa R)} \left[ \frac{P^n \kappa}{\pi} I_n(\kappa nr) \right]. \quad (2.7d)$$

The form above satisfies the momentum equation. The coefficients $A^n$, $B^n$ and $C^n$ can now be obtained from the boundary conditions, by using the continuity equation to relate the coefficients for the pressure to the components of flow: $P^n = -n\pi(A^n + B^n - 2C^n)$. One may verify that in the limit $\lambda \to \infty$, where the indifferent zones are straight, a cylindrically symmetric solution is obtained,

$$u_z(r, \theta) = \sum_{n \text{ odd}} D^n r^n \sin n\theta. \quad (2.8)$$

A step-function boundary velocity yields the solution due to Pickard (1972),

$$u_z(r, \theta) = \frac{2U}{\pi} \arctan \frac{2(r/R)\sin \theta}{1 - (r/R)^2}. \quad (2.9)$$

In general, the resulting linear system of equations can be solved readily using linear algebra software, after which the forms $v(r, \phi)$ and $\Psi(r, \phi)$ are obtained by a transformation from the solution in cylindrical coordinates. The stream-function components, which potentially play a role in the enhancement of intracellular mixing in younger cells, are expected to have a magnitude less than 1 $\mu$m/s in mature internodal cells whose helical wavelength is typically quite long (10-30 mm). Such speeds are below the effective noise limit of the MRV measurements. Our experiments do however provide a comparison with the downstream profile to an extent not previously possible, allowing us to examine the degree to which the vacuolar flow is consistent with constant imposed velocity at the boundary.

In the results presented here, 64 modes were used for the expansion. The cross-over width was equivalent to $\epsilon = 11$ $\mu$m. To allow comparison with the MRV measurements, which obtain the mean flow along a volume of several millimetres along the $x$-axis, a series of profiles was averaged along a length of 3 mm, using a Gaussian weighting with a spread of 1 mm full-width at half maximum, as was used in the experiments.
3. Magnetic Resonance Velocimetry Measurements

Our experiments were performed on internodes excised from Chara corallina v. australis, originally obtained from the Botanic Garden of the University of Cambridge, courtesy of J. Banfield. The plants were grown in a non-axenic culture, rooted in non-fertilised soil in a 100 litre tank filled with Artificial Pond Water (1 mM NaCl, 0.4 mM KCl, 0.1 mM CaCl$_2$). The tank was kept at room temperature and illuminated with a bench lamp on a 16/8 hour day-night cycle. During illumination, the light intensity at the top of the tank was $\sim 250$ lux. Samples of suitable size were placed in a Petri dish under a microscope to verify healthy streaming.

To measure the cross-sectional flow inside the internodal vacuole, a sample was inserted into a horizontal solenoidal radio-frequency (RF) coil (figure 1d), in a 1.6 mm inner diameter glass capillary 40 mm in length, which was pre-filled with Forsberg medium (Forsberg 1965). The capillary tube was closed with PDMS plugs and a small volume of silicone grease to ensure a good seal over the measurement time of 192−256 minutes needed to obtain the cross-sectional resolutions of 16 $\mu$m $\times$ 31 $\mu$m in our experiments.

Velocimetry measurements were performed on a Bruker Spectrospin DMX 200, 4.7 T magnet with a 20 mm long solenoidal coil of diameter 3 mm. $^1$H images were acquired at 199.7 MHz. Spatial resolution was achieved using 3-axis shielded gradient coils providing a maximum gradient strength of 49 G cm$^{-1}$ in each direction. Transport is measured over the observation time, $\Delta$, and since the RMS displacement increases as $\Delta^{1/2}$ due to diffusion and as $\Delta^1$ due to convection, for short $\Delta$ diffusive (incoherent) displacements can dominate over convective (coherent) ones, particularly in slowly convecting systems. Therefore, to weight the measurement towards the convective field a stimulated echo sequence was used to enable a large observation time for motion encoding. Further spatial imaging gradients were applied after the motion encoding to minimise
diffusive attenuation. Hard 90° RF pulses were used except for the final pulse which was a Gaussian-shaped selective 90° RF pulse 512 μs in duration. Experimental parameters used for the velocity images were: observation time, Δ = 500 ms; velocity gradient duration, \( d = 1.62 \) ms; gradient increment, \( g_{\text{inc}} = 10 \) G cm\(^{-1}\); number of velocity gradient increments, 2; recycle time, \( TR = 1.9 \) s; number of scans = 16; field-of-view = 2 mm × 2 mm; pixel array size \( N_{\text{read}} \times N_{\text{phase}} = 128 \times 64 \); in-plane spatial resolution = 16 μm × 31 μm; slice thickness = 1 mm; measurement duration = 64 min.

For each data set, 4 measurements were taken between 3 and 7 hours apart and subsequently averaged. A Gaussian smoothing with 31 μm FWHM was selectively applied to the streaming region whilst avoiding blurring at the cell periphery. The streaming velocity in the individual measurements was not observed to vary significantly over the 15 hour period of acquisition. Throughout the measurements the temperature was maintained at 298 K by a regulated airflow system.
Figure 2a shows the location of the five averaging domains on a particular sample, and figure 2b shows the velocity profiles at three of those positions. Mean flow velocities are $\sim 45$ $\mu$m/s, which is roughly consistent with other measurements for a cell of radius $R = 460$ $\mu$m at a temperature of 298 K (Pickard 1974), though the low ambient light levels inside the coil may have reduced the streaming rate somewhat (Plieth & Hansen 1992). The helical pitch obtained from five short measurements 2 mm apart (figure 2a, arrowheads) is $18.6^\circ$/mm, giving a dimensionless wavelength of $\lambda/R = 42.0$, in good agreement with our estimate from the light-microscopy image in figure 1b.

Aligning and averaging the three datasets in figure 2b we further enhance the signal to noise ratio of the profile. The resulting cross-section (figure 3a) is in excellent agreement with the hydrodynamic solution, shown in figure 3b. As indicated in the previous section, we account for the $\sim 20^\circ$ of helical rotation along the measurement volume by averaging the theoretical expression over a length of 3 mm with the same Gaussian weighting as the MRV measurements. The wall-to-wall 1-dimensional profiles in figure 3c show close agreement with the theoretical solution. In figure 3d, measurement points are plotted against their theoretical values, in the manner of earlier velocity measurements (Pickard 1972). The color of the points indicates the radial distance from the centre of the cell. We see a remarkably good correspondence throughout the bulk of the cell, with deviations restricted primarily to points within a pixel from the cell wall, where partial-volume effects become significant.

In summary, we have established that the cytoplasmic streaming velocity field within a particular plant cell is consistent with direct transmission of shear through the vacuolar membrane. It is therefore accurate to represent the driving force from the actin-myosin system within the cytoplasm as a piecewise constant Dirichlet condition of specified velocity at the cell periphery. The clear implication of this result is that the tonoplast itself is carried along with the flow in each of the two hemicylinders of the cell. As the streaming velocities can reach 100 $\mu$/s in the two directions, and the transition region at the indifferent zones is $\sim 20$ $\mu$m wide, the shear rate experienced by the membrane there can reach the rather large value of 10 s$^{-1}$. Further work is needed to understand the membrane dynamics there, and to determine the manner in which the complex rheology of the cytoplasm is coupled to the tonoplast. On a more general level, these measurements show that magnetic resonance velocimetry can yield detailed information on the velocity distribution of cytoplasmic streaming within single plant cells, allowing quantitative comparison with fluid dynamical theories. Natural extensions to this work include studies of other streaming geometries found to elucidate the nature of their forcing by molecular motors, and the study of tracer particle dynamics as a probe of mixing (Esseling-Ozdoba et al. 2008).

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