

Bacterial swimming and oxygen transport near contact lines

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Aerobic bacteria often live in thin fluid layers near solid–air–water contact lines, in which the biology of chemotaxis, metabolism, and cell–cell signaling is intimately connected to the physics of buoyancy, diffusion, and mixing. Using the geometry of a sessile drop, we demonstrate in suspensions of *Bacillus subtilis* the self-organized generation of a persistent hydrodynamic vortex that traps cells near the contact line. Arising from upward oxygentaxis and downward gravitational forcing, these dynamics are related to the Boycott effect in sedimentation and are explained quantitatively by a mathematical model consisting of oxygen diffusion and consumption, chemotaxis, and viscous fluid dynamics. The vortex is shown to advectively enhance uptake of oxygen into the suspension, and the wedge geometry leads to a singularity in the chemotactic dynamics near the contact line.

bioconvection | chemotaxis | singularity | *Bacillus subtilis*

The interplay of chemotaxis and diffusion of nutrients or signaling chemicals in bacterial suspensions can produce a variety of structures with locally high concentrations of cells, including phyllotactic patterns (1), filaments (2), and concentrations in fabricated microstructures (3). Less well explored are situations in which concentrating hydrodynamic flows actually arise from these ingredients. Here we report a detailed experimental and theoretical study of an intriguing mechanism termed the “chemotactic Boycott effect.” Described briefly before (4), it is intimately associated with buoyancy-driven flows, metabolite diffusion, and slanted air–water menisci. The ubiquity of contact lines and their transport singularities (5) suggest importance of these observations in biofilm formation (6). The large-scale stirring created by these flows illustrate important advective contributions to intercellular signaling, as in quorum sensing (7).

The chemotactic Boycott effect takes its name from a phenomenon in sedimentation (8) that occurs when the chamber containing a fluid with settling particles is tilted from vertical. Settling depletes the fluid near the upper wall, making it buoyant relative to nearby fluid, whereupon it rises. This boundary flow stirs up the entire medium, greatly accelerating the settling process. In the chemotactic version, negatively buoyant aerobic bacteria swim up to the free surface of a sessile drop and slide down the slanted meniscus, producing high concentrations of cells near the three-phase contact line. In earlier work where this was observed (4), the detailed nature of hydrodynamic flows near the contact line was unclear. Here, by direct visualization and particle-imaging velocimetry (PIV), we show that the sliding surface layer drives a circulating hydrodynamic vortex in the meniscus region that is central to the microecology. Although counterintuitive in viscous flows, persistent circulation driven by forcing at the free surface is consistent with the classic analysis for vortex generation in wedge geometry (9).

The initial discussion of the chemotactic Boycott effect lacked a quantitative explanation in terms of the coupled dynamics of oxygen transport and consumption, chemotaxis, and viscous

fluid dynamics. Here we present numerical and analytical results on one such model and show that they provide a good accounting of the major experimental observations. The characteristic fluid velocity U and length scale L associated with the vortex are both significantly larger than those of a single bacterium. In comparing the relative importance of advective to diffusive transport of a solute, it is natural to incorporate U , L , and the diffusion constant D into the dimensionless Peclet number $Pe = UL/D$, with $Pe \ll 1$ indicating that diffusion is the dominant transport mechanism and $Pe \gg 1$ is the advection-dominated regime. We find that the Boycott-like flows lead to $Pe \gg 1$, just the opposite of the situation at the scale of a single bacterium. In addition, by analogy with evaporative singularities in sessile drops (5, 10), we find a singularity in the oxygen-uptake rate at the contact line. Along with the large-scale stirring of fluid in the drop, this flow significantly enhances the overall oxygen concentration in the medium, showing that collective effects can improve the viability of the population, as demonstrated by remarkable collective activity (4) of the extremely concentrated organisms near the drop edge.

Materials and Methods

Experiments were conducted with *Bacillus subtilis* strain 1085B. Samples were prepared by adding 1 ml of -20°C stock to 50 ml of terrific broth (TB) (Ezmix Terrific Broth, Sigma; 47.6 g of broth mix and 8 ml of glycerin in 1 liter of distilled water) and incubating for 18 h (VWR model 1217 shaker bath; 37°C , 100 rpm), after which 1 ml of the bacterial suspension was added to 50 ml of TB and incubated for 5 h. The 5-h culture was then slowly added to the chamber with a syringe (21-gauge needle). The -20° stock was prepared by adding spores on sand to 10 ml of TB at room temperature in a Petri dish and allowing for ≈ 24 h of growth. One milliliter of 24-h stock was added to 50 ml of TB and incubated for 18 h. One milliliter of the 18-h culture was added to 50 ml of TB and incubated for 5 h. Aliquots composed of 0.75 ml of 5-h culture mixed gently with 0.25 ml of glycerin were placed in cold storage. The chambers (Fig. 1A) were constructed from microscope slides cemented together with UV curing adhesive (Norland, Cranbury, NJ); care was taken to remove excess adhesive to avoid interference with visualizations near the contact line and to seal the chamber adequately to avoid evaporation and associated flows. The space between the vertical slides that form the front and back of the chamber was typically 1 mm. Imaging was achieved with a digital charge-coupled device camera [Hamamatsu (Ichinocho, Japan) C7300; $1,024 \times 1,024$ pixels; 12 bit] under computer control (National Instruments, Austin, TX) attached to a macrophotography bellows (PB-6, Nikon) with a 105-mm f/2.8 lens. Dark-field illumination was a 4-cm-diameter fiber-optic ring light (Navitar,

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Abbreviation: PIV, particle-imaging velocimetry.

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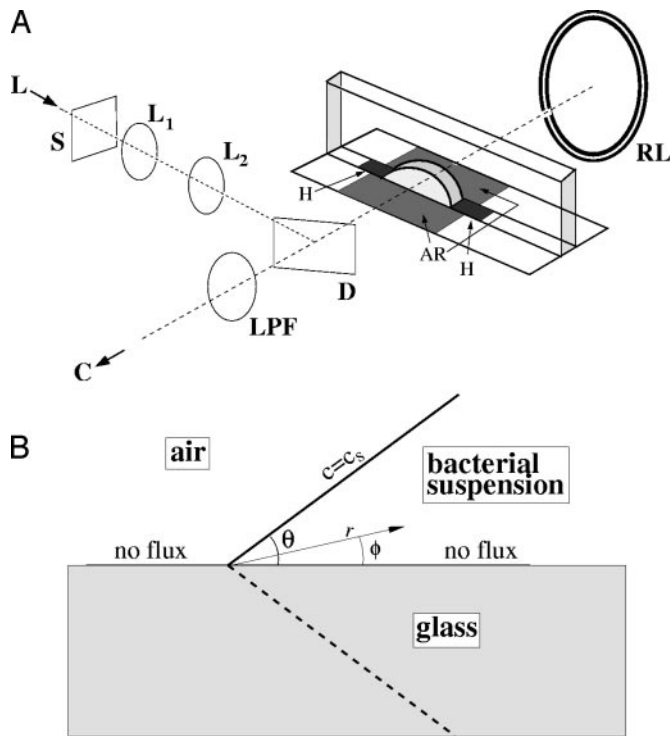


Fig. 1. Construct for quantitative analysis of bacterial dynamics at a slanting interface. (A) Apparatus for simultaneous dark-field and fluorescence imaging of fluid drops: laser (L), shutter (S), beam-expander lenses (L_1 and L_2), dichroic beam splitter (D), long-pass filter (LPF), fiber-optic ring light (RL), and digital camera (C). The chamber has antireflection areas (AR) to reduce glare and hydrophobic areas (H) to pin the drop. (B) Boundary conditions and coordinates in the wedge (described in *Mathematical Model*).

Rochester, NY) behind the sample chamber. PIV measurements were conducted by adding 5 μl of fluorescent microspheres (Molecular Probes, F8825 carboxylate modified, 1.0 μm , Nile red) to 1 ml of suspension, illuminating with a DPSS laser (100 mW, 532 nm) reflected from a dichroic mirror (Z542RDC, Chroma Technology, Rockingham, VT), and visualizing through a long-pass filter (HQ542LP, Chroma Technology). Analysis was performed with PIV software (Dantec Dynamics, Skovlunde, Denmark).

Results

Fig. 2 A–C shows images of the main stages of the chemotactic

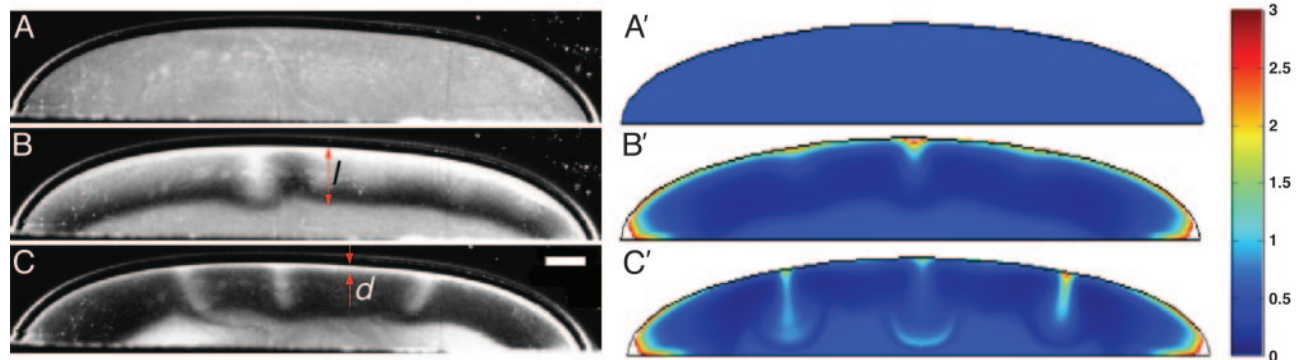


Fig. 2. Stages leading to self-concentration in a sessile drop, observed experimentally (A–C) and by numerical computations with the model described in text (A'–C'). (A and A') Drop momentarily after placement in the chamber. (B and B') Formation of depletion zone after 150 s, before appreciable fluid motion. (C and C') Lateral migration of accumulation layer toward drop edges and creation of vortex (shown in Fig. 3) after 600 s. The color scheme describes the rescaled bacteria concentration ρ as defined in *Appendix*. (Scale bar, 0.5 mm.)

Boycott effect. After a drop of well mixed suspension is placed in the chamber, the first spatial structure that forms is a “depletion layer” of thickness $\ell \approx 1$ mm below the fluid–air interface, which appears dark in our imaging method because of the absence of cells. This region arises from the consumption of dissolved oxygen by the uniformly dispersed cells, followed by their chemotactic migration up the oxygen gradient to the source of oxygen: the free surface. No cellular motion is seen below the depletion layer, suggesting that the oxygen concentration there has fallen to the critical value, denoted c^* , below which motility vanishes. In a flattened sessile drop, the bottom of the depletion layer follows the shape of the air–water meniscus, displaced downward by the layer thickness. This layer forms within 100 s, consistent with consumption of the saturation-dissolved oxygen concentration $c_s \approx 10^{17} \text{ cm}^{-3}$ by cells at concentration $n_0 \approx 10^9 \text{ cm}^{-3}$, with a consumption rate $\kappa \approx 10^6$ oxygen molecules per second. This interval is also consistent with the time $t_\ell = \ell/v_c$ for a cell with a typical chemotactic velocity $v_c \approx 10 \mu\text{m/s}$ to traverse the thickness ℓ . Ultimately, the cells congregate in a narrow surface “accumulation layer,” whose thickness $d \approx 100 \mu\text{m}$.

Although the accumulation layer slides along the meniscus to the contact line, it is unstable to plume formation on a length scale comparable to the layer thickness, consistent with the fundamental instability of bioconvection in fluids with a horizontal meniscus (11). The Boycott effect occurs at the slant region; the resultant surface and return flows distort the plumes that would otherwise fall straight down. This surface flow is opposite to that of the conventional Boycott effect, but the depletion layer here is buoyantly forced in the usual direction, creating a unique shear double layer. Typical fluid velocities at the free surface are in the range of 20–200 $\mu\text{m/s}$, accelerating as the meniscus slope increases near the contact line. Finally, because of incompressibility requirements, a well developed vortex appears near each of the contact lines and shows persistence over many tens of minutes. The closed streamlines (Fig. 3A) show the sense of circulation created by the downward gravitational forcing on the accumulation layer and the recirculation into the bulk required by fluid incompressibility. Despite the outward flow at the bottom of the vortex, the optical density indicates that cells are trapped near the contact line.

Mathematical Model. The dynamics of the oxygen concentration c , cell concentration n , and fluid velocity $\mathbf{u}$ are described by coupled partial differential equations (12),

$$c_t + \mathbf{u} \cdot \nabla c = D_c \nabla^2 c - n \kappa f(c) \quad [1]$$

$$n_t + \mathbf{u} \cdot \nabla n = D_n \nabla^2 n - \nabla \cdot [\mu r(c) n \nabla c] \quad [2]$$

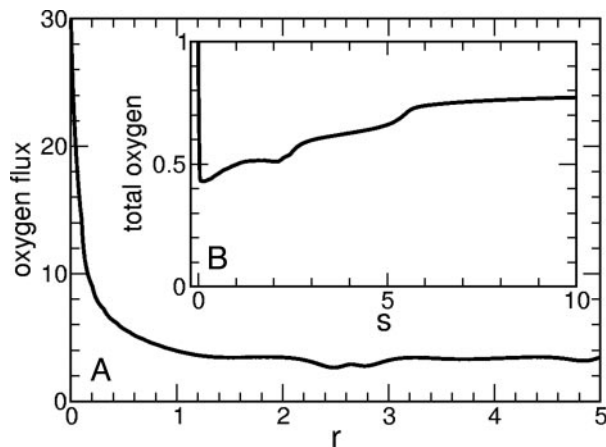


Fig. 5. Oxygen dynamics from numerical studies. (A) Inward flux of oxygen along upper surface of a drop, in units of $D_c c_s / L$, as a function of distance r from the contact line, showing near-singular behavior. (B) Average oxygen concentration in the drop as a function of rescaled time s , normalized to the initial value.

ance with respect to the direction along the contact line. The essential features of the flow are found as well in numerical studies by using Darcy's law for flow between the vertical plates of the experimental chamber. Overhead views of sessile drops reveal that in the third dimension the vortex breaks up into a radial form of bioconvective plumes (4). A further analysis of this globally driven instability is needed. Our two-dimensional computations, shown in Figs. 2 A'–C', reproduce the observations: the depletion layer tracing the shape of the meniscus, the variations in thickness of the accumulation layer over the boundary of the drop, and the plume instability. Fig. 3B shows that the vortex is also captured accurately.

Except close to the contact line, the accumulation layer is very thin compared to the depth of the drop, so the gravitational forcing that acts on it is essentially concentrated at the surface. When combined with the no-slip boundary condition at the bottom of the drop, this forcing defines one of the scenarios in Moffatt's analysis of viscous eddies in sharp corners (9). Theory predicts a set of progressively smaller vortices adjacent to the main vortex. We have not seen evidence of these vortices in either experiment or simulations, but they are expected to be extremely weak and are likely outside the resolution of both approaches. Theory also suggests that the conditions under which vortices develop can depend sensitively on the far-field conditions and the wedge angle. Our numerical results indicate the existence of a vortex at least over a range of angles from $\pi/4$ to $\pi/2$.

The velocities U in the vortex can reach 0.01 cm/s, with a size of 0.1 cm, so the Peclet number can approach $\approx 10^2$. Numerical studies show that the combination of accumulated bacteria and greatly enhanced stirring in the wedge lead to (i) a near-singular variation in oxygen flux near the contact line (Fig. 5A) and (ii) an increase in oxygen uptake into the drop. Fig. 5B shows that the average oxygen concentration initially drops precipitously as consumption dominates, but it slowly returns to a high value as stirring enhances the uptake from the air above. Without the hydrodynamic coupling between cell concentration and buoyancy, the oxygen concentration remains low after the initial consumptive drop. Not only oxygen but also nutrients will be ferried to the contact-line region from areas in the bulk of the drop.

Chemotactic Singularity. Some insight into the oxygen flux near the contact line is obtained by making use of the electrostatic

analogy mentioned above. Close enough to the contact line the numerics indicate that the velocity along the upper free surface tends to zero, so advective contributions vanish asymptotically there. The simplest steady-state oxygen-diffusion problem, for which $\nabla^2 c = 0$ inside the drop and $c = c_s$ on the free surface, is mathematically equivalent to the equation defining the electrostatic potential in that same region, the exterior of the drop being a conductor (5). This mapping reveals (14) that a singularity arises from a solution of the form

$$c(r, \phi) \sim c_s + \sum_{m=1}^{\infty} a_m r^{m\pi/2\theta} \cos(m\pi\phi/2\theta), \quad [5]$$

with polar coordinates (r, ϕ) as shown in Fig. 1B. This form enforces the condition $c = c_s$ on the drop surface ($\phi = \theta$) and the no-flux condition on the glass substrate ($\phi = 0$). After successive differentiation, the potentially most singular term is $m = 1$, and we expect $a_1 < 0$ because $c \leq c_s$ in the drop interior. Noting that $|\nabla c| \approx r^{\pi/2\theta-1}$ and $\nabla^2 c \approx r^{\pi/2\theta-2}$, singularities appear in two cases:

1. $\theta > \pi/2$, an overhanging meniscus. This case is like the familiar "lightning-rod" effect. Both the Fick's law oxygen flux, $-D_c \nabla c$, and the chemotactic flux, $\mu n \nabla c$, diverge as $r \rightarrow 0$, leading to a singular accumulation at the contact line.
2. $\pi/4 < \theta < \pi/2$, as shown in Figs. 2–4. Here, $|\nabla c|$ is finite as $r \rightarrow 0$ but has a diverging slope. Expanding the chemotaxis term in the dynamics (Eq. 3), we see terms of the form $\mu[\nabla n \cdot \nabla c + n \nabla^2 c]$, the former implying a potential cusp in the cell concentration n . Although weaker than case 1, there still is a singular accumulation driven by the diffusional singularity of oxygen.

Let us consider in more detail the typical case $\theta < \pi/2$. There is a positive, bidirectional feedback loop involving the chemotactic response to the oxygen singularity. The singularity is reinforced by the accumulation of bacteria that consume the oxygen. A rough idea of this can be gleaned by examining a steady-state balance between the dominant terms in the chemotaxis equation (Eq. 2), setting $D \nabla^2 n \approx \mu n \nabla^2 c$ to find a distribution $n \approx \exp(-\Gamma r^{\pi/2\theta})$, with $\Gamma > 0$, that decays away from the contact line very sharply. Because the local oxygen consumption rate is proportional to n , the inward flux of oxygen mirrors the bacterial concentration distribution, as shown in Fig. 5B. Although a more precise treatment requires a fully self-consistent calculation of the coupled oxygen and bacterial concentrations, this result illustrates the dramatic accumulation of bacteria in the contact region.

The development of the self-trapping vortex and the associated high concentration of bacteria near the contact line depend crucially on the no-flux boundary conditions at the substrate. A dramatic demonstration of this phenomenon is seen in the flows in a "supported" drop. This geometry was achieved by turning over the experimental chamber, allowing a previously sessile drop to slide down from the chamber base toward the opening at the opposite end. Surface tension supports the drop, with free uptake of oxygen around the whole meniscus. As shown in Fig. 6, the bottom interface is very flat, giving an effective contact angle exceeding $\pi/2$, but with no substrate the dynamics are nonsingular. We see the key stages in the chemotaxis and fluid instabilities in this geometry. Development of the depletion zone occurs rather symmetrically around the entire perimeter of the drop, producing the nonmotile region in the center. Later, plumes descend from above, and the accumulation layer slides down the drop meniscus, producing a clearly visible enhancement of concentration at the bottom of the meniscus beyond the local

$$\rho_s + \mathbf{v} \cdot \nabla \rho = \nabla^2 \rho - \alpha \nabla \cdot [r(\chi) \rho \nabla \chi] \quad [10]$$

$$\frac{1}{Sc} (\mathbf{v}_s + \mathbf{v} \cdot \nabla \mathbf{v}) = -\nabla \pi + \nabla^2 \mathbf{v} - \gamma \rho \hat{\mathbf{z}}, \quad [11]$$

where

$$\beta = \frac{\kappa n_0 L^2}{c_s D_n} \quad Sc = \frac{\nu}{D_c} \quad \gamma = \frac{\nu n_0 g(\rho_b - \rho) L^3}{\eta D_n}. \quad [12]$$

The time $L^2/D_n \approx 10^3$ s is that for diffusion across the drop, $\beta \approx 10$ is the ratio of the bacterial diffusion time to that for oxygen consumption, and the Schmidt number $Sc \approx 10^3$ measures the ratio of kinematic viscosity to diffusion of oxygen. Finally, $\gamma \approx 10^3$ is analogous to the Rayleigh number in thermal convection (11).

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