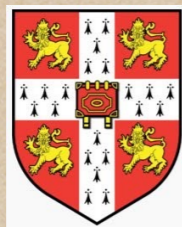


# The dawn of a new era: Exploring the Universe with Gravitational Waves

Ulrich Sperhake



DAMTP, University of Cambridge  
LIGO Scientific Collaboration



Cambridge University Astronomical Society  
*Cambridge, 24 Nov 2020*



This project has received funding from the European Union's Horizon 2020 research and innovation programme under the Marie Skłodowska-Curie grant agreement No 690904, from H2020-ERC-2014-CoG Grant No. "MaGRaTh" 646597, from NSF XSEDE Grant No. PHY-090003 and from STFC Consolidator Grant No. ST/L000636/1.

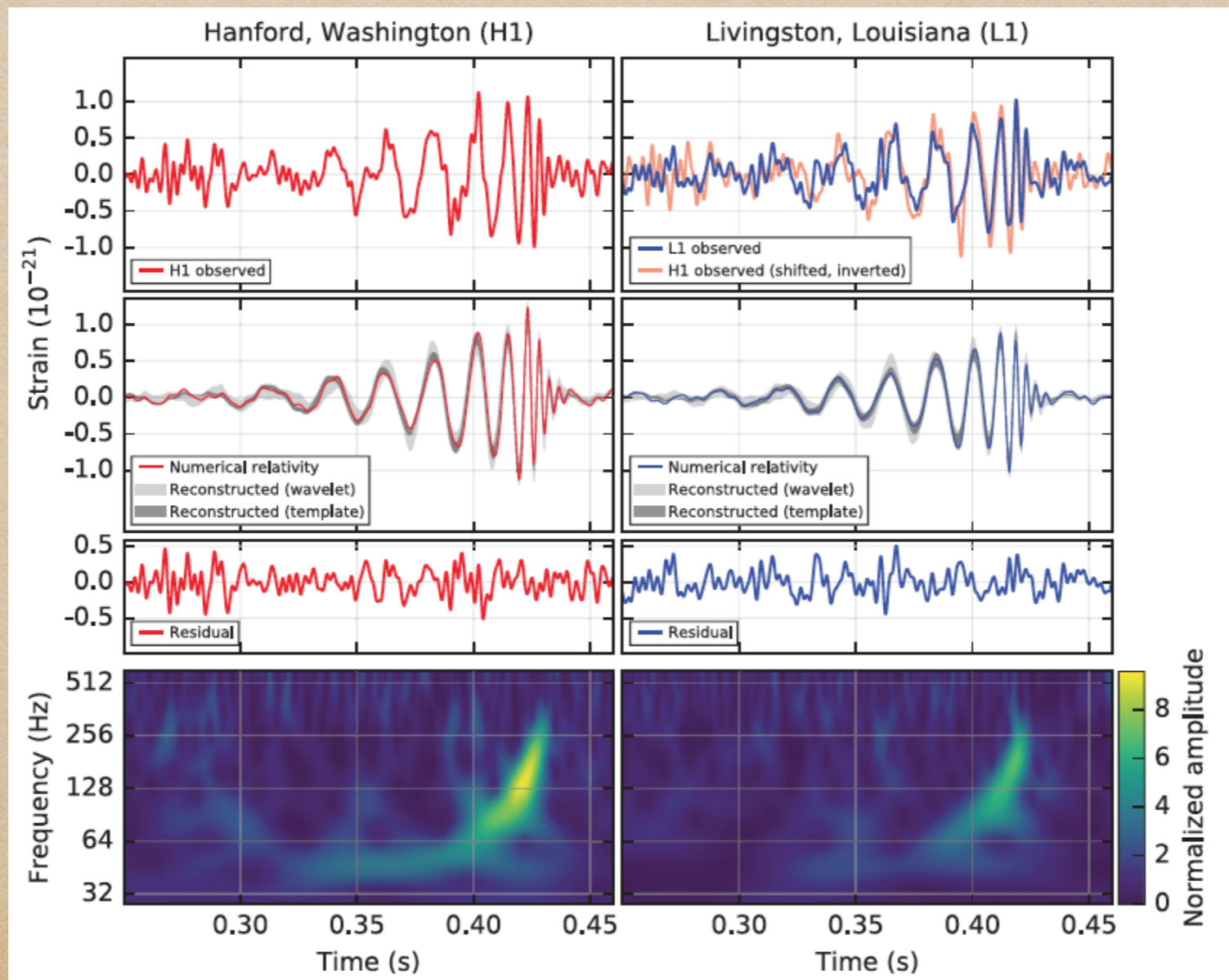
# Gravitational Waves: Ripples in spacetime

- Unusual news headlines on 11/12 February 2016
- First direct detection of gravitational waves: GW150914



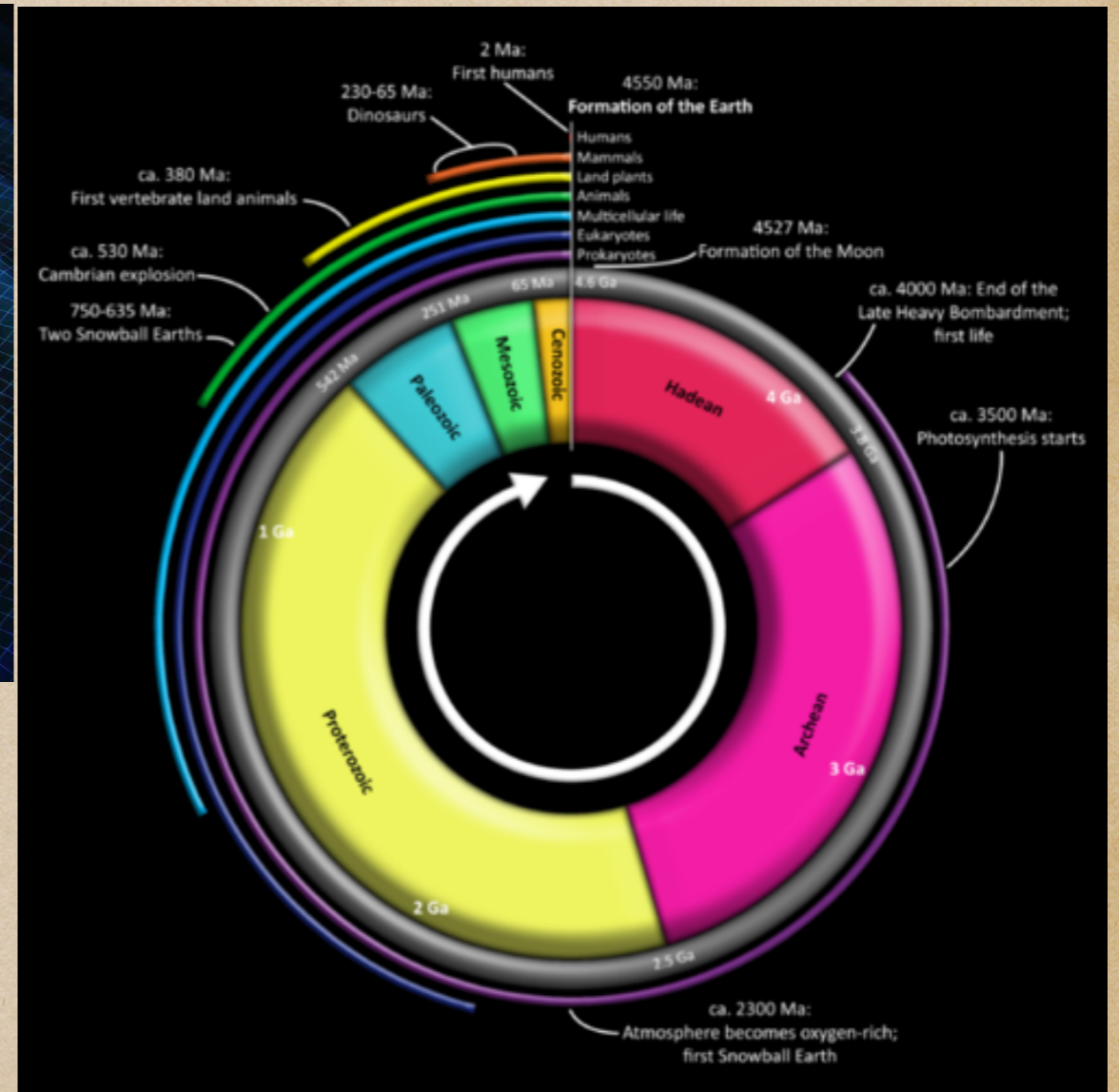
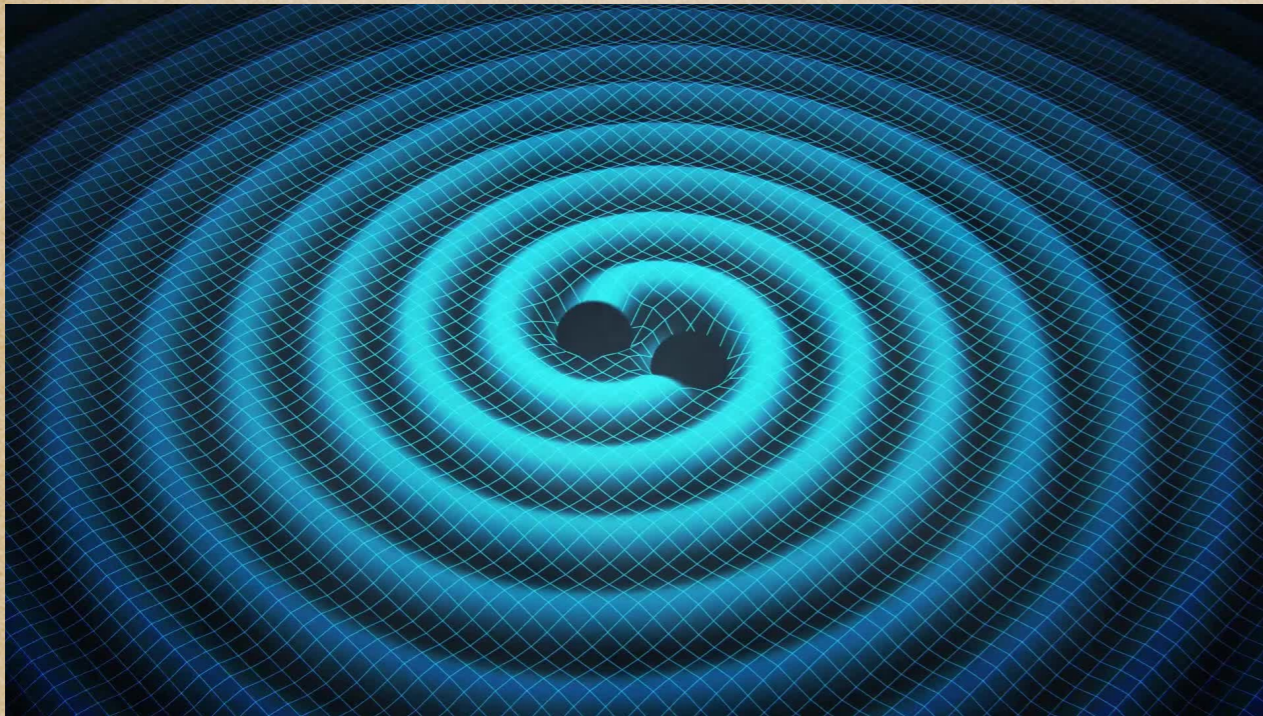
# So, what happened?

- Sep 14, 2015 at 09:50:45 UTC: SNR  $\sim 24$   
Abbott et al. PRL 2016, Abbott et al. 1606.01210
- BBH inspiral, merger and ringdown:  $m_1 = 35_{-3}^{+5} m_{\odot}$ ,  $m_2 = 30_{-4}^{+3} M_{\odot}$



# What really happened...

- Once upon a time:  $1.34_{-0.59}^{+0.52}$  Gyr ago, somewhere in the universe



- Deep Precambrian

# Overview

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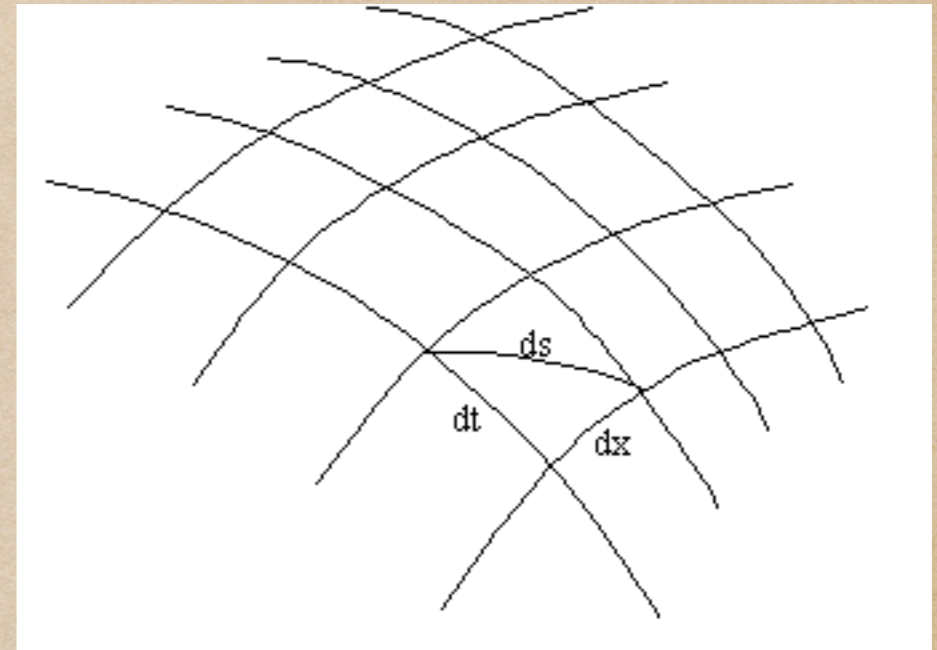
- A brief theory of gravitational waves
- Frequency windows, sources and detectors
- Parameter estimation and source modeling
- The GW events
- Some future applications
- Conclusions

**Gravitational waves**

# General relativity in 30 seconds

- Spacetime as a curved manifold
- Key quantity: spacetime metric  $g_{\alpha\beta}$
- Curvature, geodesics etc. all follow
- Einstein equations

$$R_{\alpha\beta} - \frac{1}{2}g_{\alpha\beta}R + \Lambda g_{\alpha\beta} = \frac{8\pi G}{c^4}T_{\alpha\beta}$$



- 10 non-linear PDEs for  $g_{\alpha\beta}$
- $T_{\alpha\beta} =$  Matter fields
- Conceptually simple,
- hard in practice
- E.g. Schwarzschild

$$g_{\mu\nu} = \begin{pmatrix} \left(1 - \frac{2GM}{rc^2}\right) & 0 & 0 & 0 \\ 0 & -\left(1 - \frac{2GM}{rc^2}\right)^{-1} & 0 & 0 \\ 0 & 0 & -r^2 & 0 \\ 0 & 0 & 0 & -r^2 \sin^2 \theta \end{pmatrix}$$

$$ds^2 = c^2 dt^2 \left(1 - \frac{2GM}{rc^2}\right) - \frac{dr^2}{1 - 2GM/rc^2} - r^2 d\theta^2 - r^2 \sin^2 \theta d\phi^2$$

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# Gravitational waves: weak-field solutions

- Consider small deviations from Minkowski in Cartesian coordinates
- "Background": Manifold  $\mathcal{M} = \mathbb{R}^4$ ,  $\eta_{\mu\nu} = \text{diag}(-1, 1, 1, 1)$
- "Perturbation":  $h_{\mu\nu} = \mathcal{O}(\epsilon) \ll 1 \Rightarrow g_{\mu\nu} = \eta_{\mu\nu} + h_{\mu\nu}$
- Coordinate freedom: "Transverse-traceless (TT)" gauge
$$h^\mu{}_\mu = 0, \quad \partial^\nu h_{\mu\nu} = 0$$
- Vacuum, no cosmological constant:  $T_{\mu\nu} = 0$ ,  $\Lambda = 0$
- Einstein's eqs.:  $\square h_{\mu\nu} = 0$
- Plane wave solution in z direction:  $h_{\mu\nu} = H_{\mu\nu} e^{ik_\sigma x^\sigma}$

$$k^\mu = \omega(1, 0, 0, 1) \quad H_{\mu\nu} = \begin{pmatrix} 0 & 0 & 0 & 0 \\ 0 & H_+ & H_\times & 0 \\ 0 & H_\times & -H_+ & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix}$$

# Effect on particles

- Geodesic eq.
- Particle at rest at  $x^\mu$  stays at  $x^\mu = \text{const}$  in TT gauge

- Proper separation:

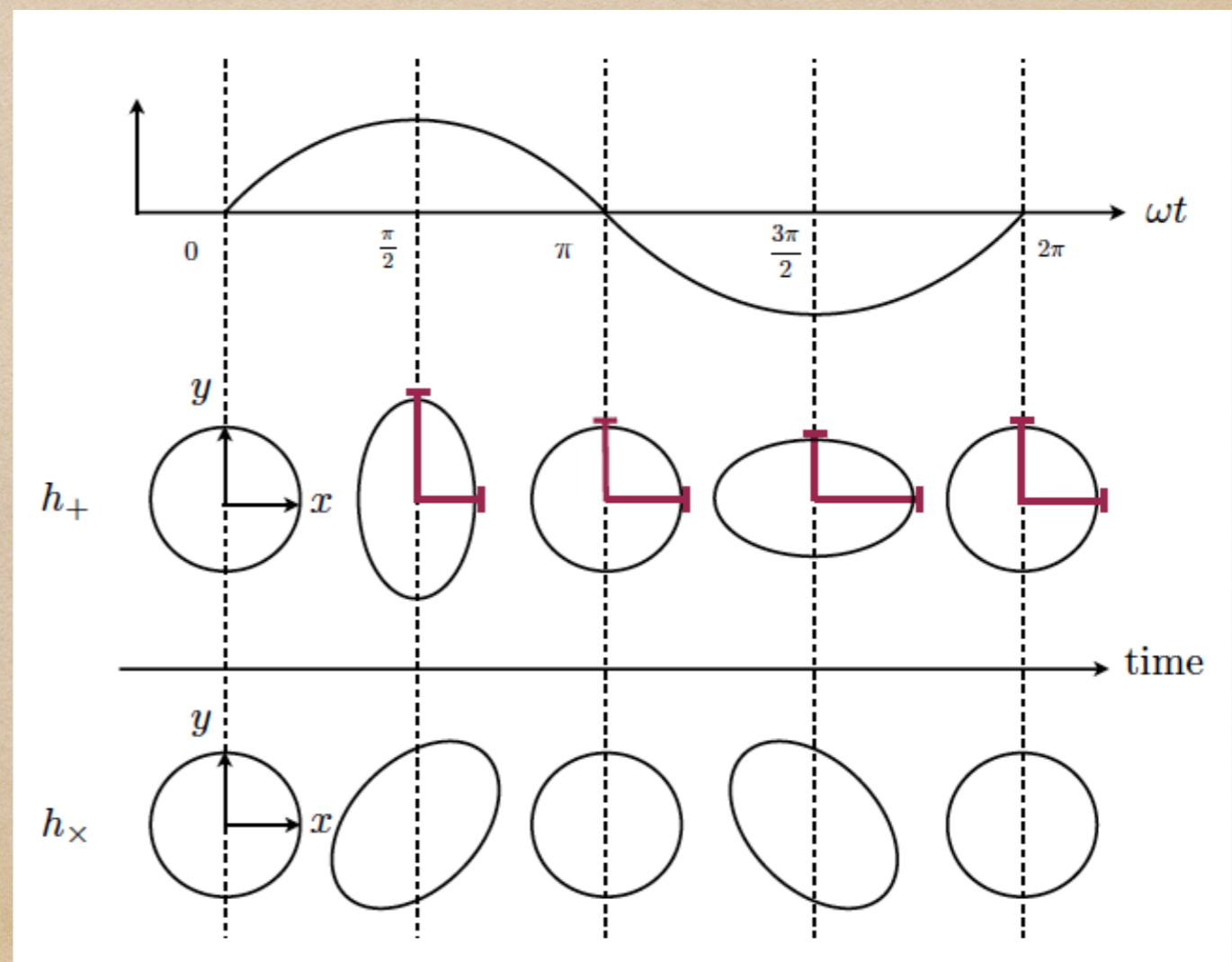
$$ds^2 = -dt^2 + (1 + h_+) dx^2 + (1 - h_+) dy^2 + 2h_\times dx dy + dz^2$$

- Effect on test particles:

Mirshekari 1308.5240

- Debate on physical reality until late 1950s

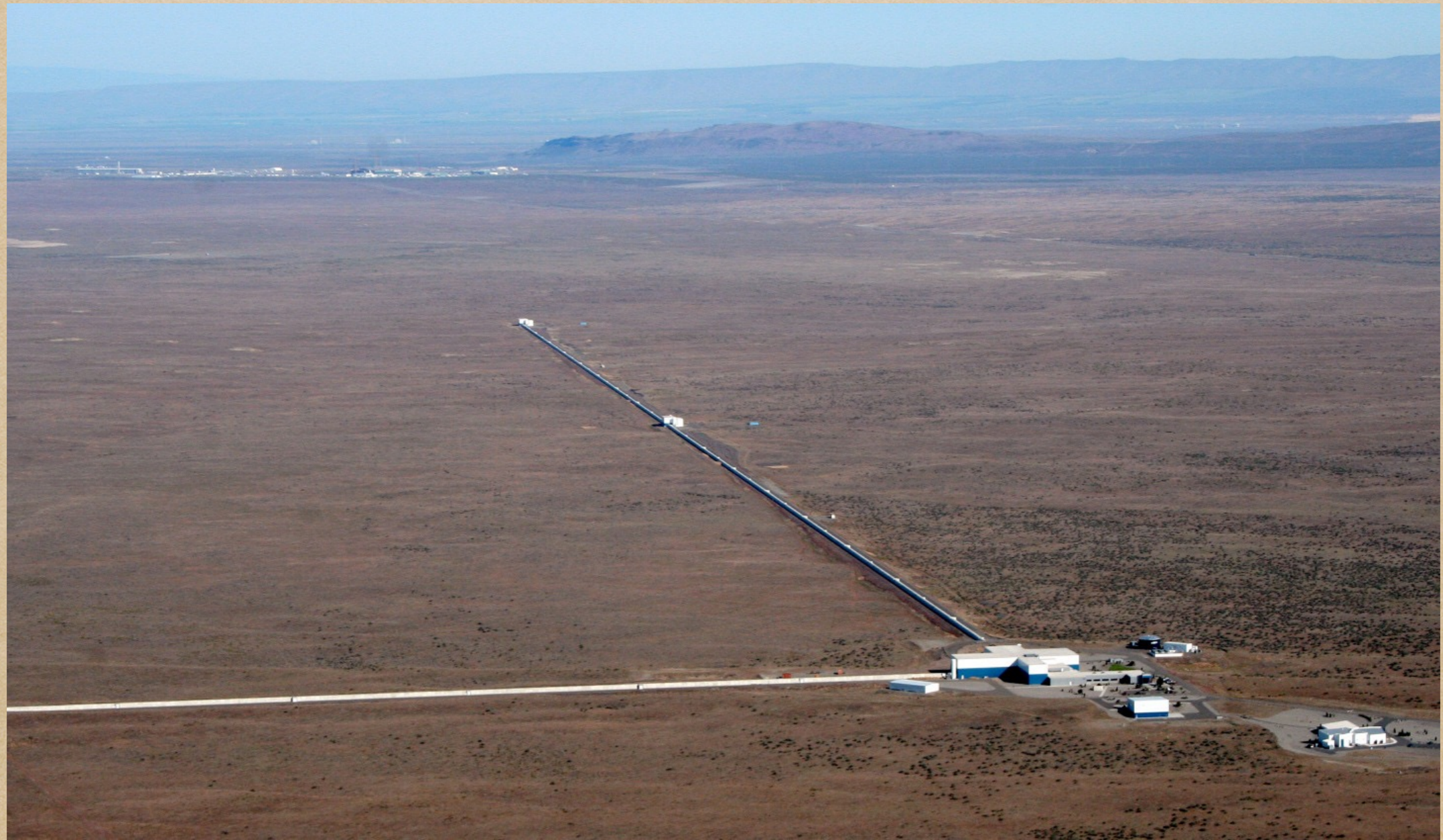
e.g. Saulson GRG (2011)



# Effect on particles

---

- Measure this effect; Michelson-Morley type interferometer



**The GW spectrum, sources and detectors**

# The gravitational wave spectrum

- Source types and detection strategies  $\Rightarrow$  4 regimes

Ultra low  $f \sim 10^{-18} \dots 10^{-15}$  Hz

Very low  $f \sim 10^{-9} \dots 10^{-6}$  Hz

Low  $f \sim 10^{-4} \dots 10^{-1}$  Hz

High  $f \sim 10^1 \dots 10^3$  Hz

- Major sources

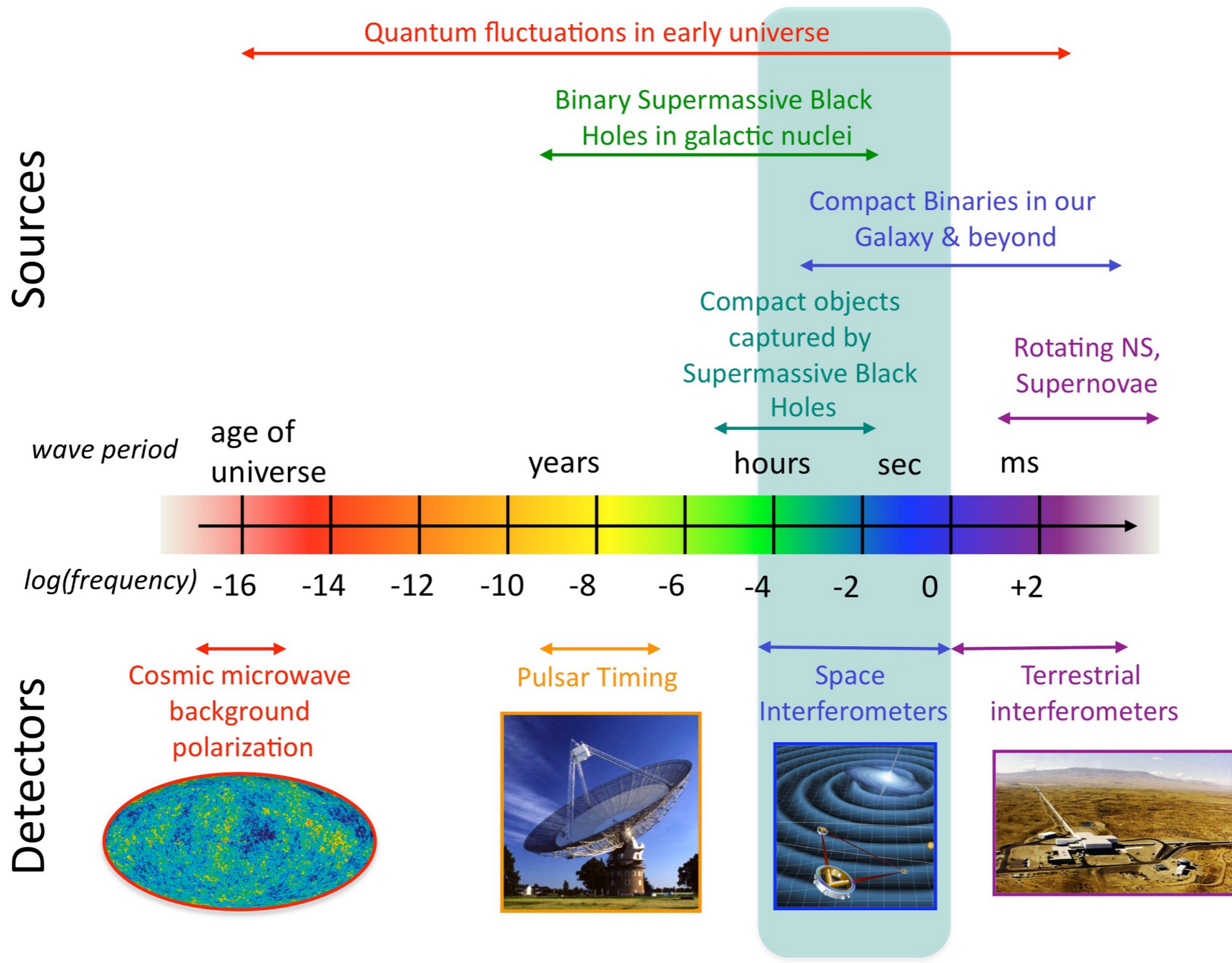
Ultra low: Fluctuations in the early universe

Very low: Supermassive BH binaries (high  $M$ ,  $z$ )

Low: SMBHs, EMRIs, Compact binaries,...

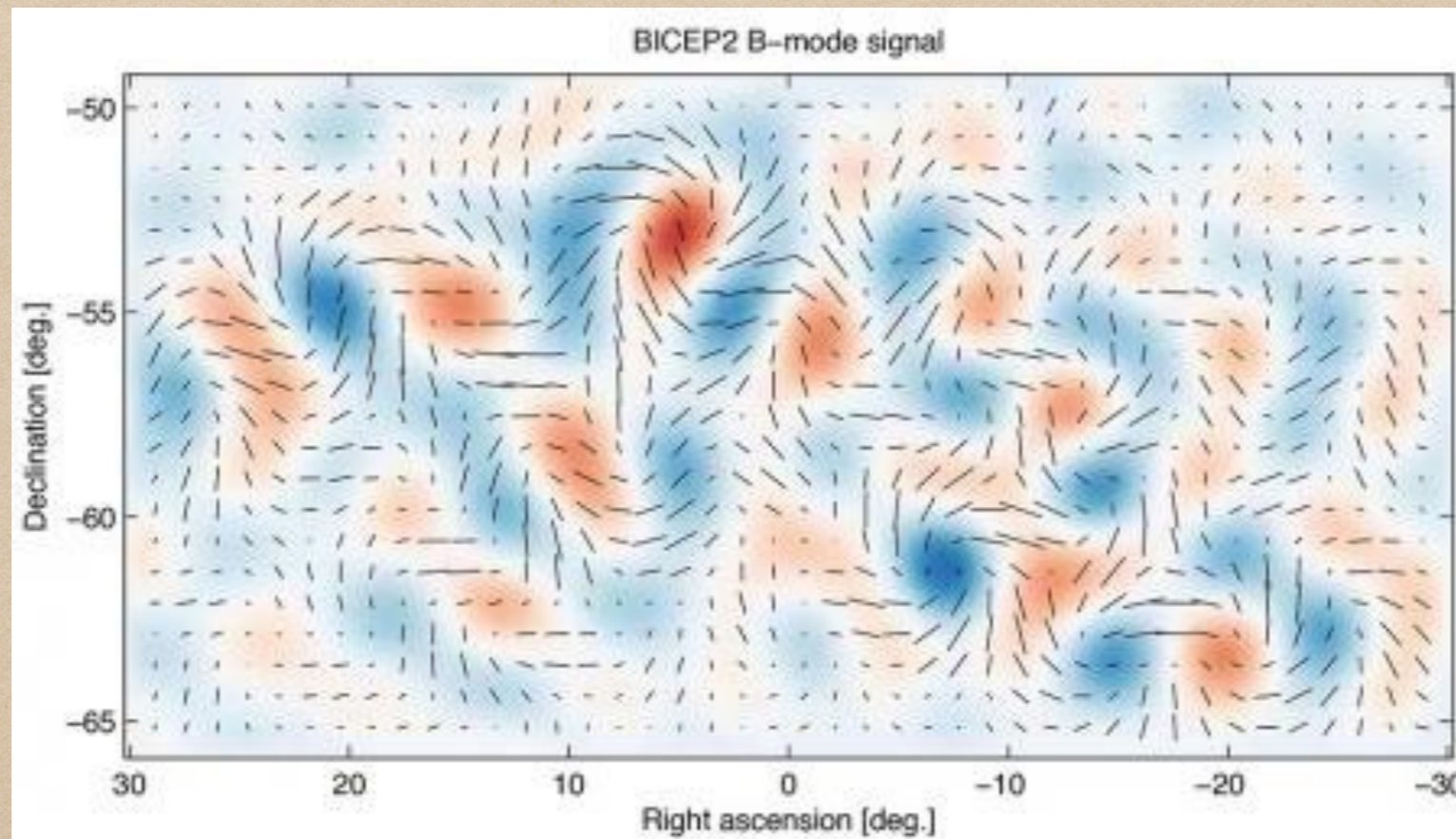
High: Neutron star / BH binaries, supernovae,...

# The gravitational wave spectrum



# The ultra low frequency regime

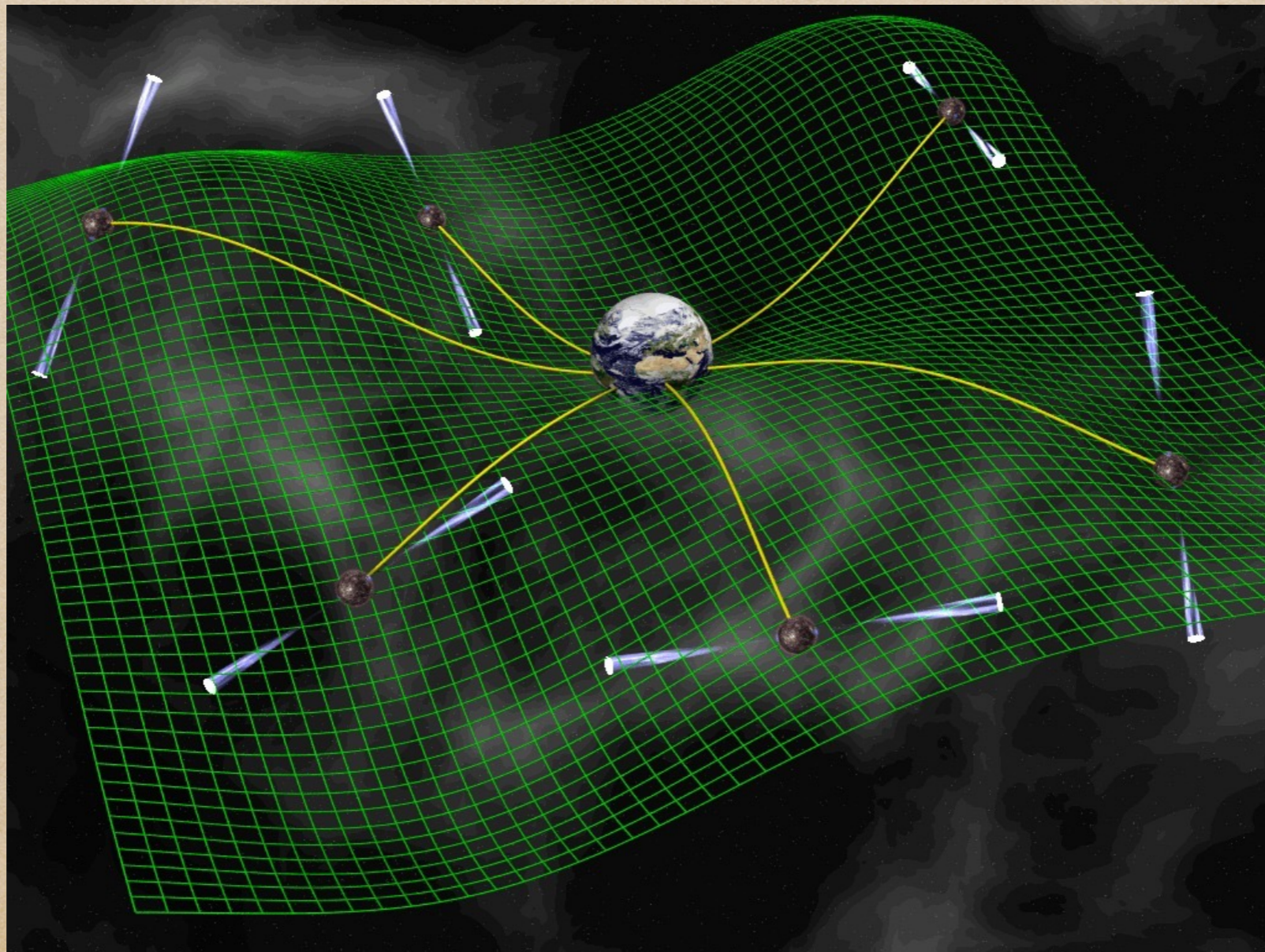
- Wave periods  $\sim$  Hubble time
- Primordial GWs  $\rightarrow$  Signature in polarization of CMB
- E.g. BICEP2



- Problem: Pattern can be attributed to galactic dust (BICEP2, Planck)  
See e.g. Flauger, Hill, Spergel 1405.7351

# The very low frequency regime

- Pulsar timing arrays PPTA, EPTA, NANOGrav
- Search for correlated arrival time delays of pulses





# The very low frequency regime

- Exotic sources: Topological defects, cosmic strings (early Universe)

- SMBH binaries  $\gtrsim 10^8 M_\odot$

Most/all galaxies host BHs hole-halo correlation:  $M_{\text{bh}} \propto \sigma^{4.8 \pm 0.5}$

Ferrarese & Merrit ApJ (2000), Gültekin et al, ApJ (2009)

- Galaxies merge  $\Rightarrow$  SMBH merger

But "Final parsec problem"

- Few individually observed systems possible.

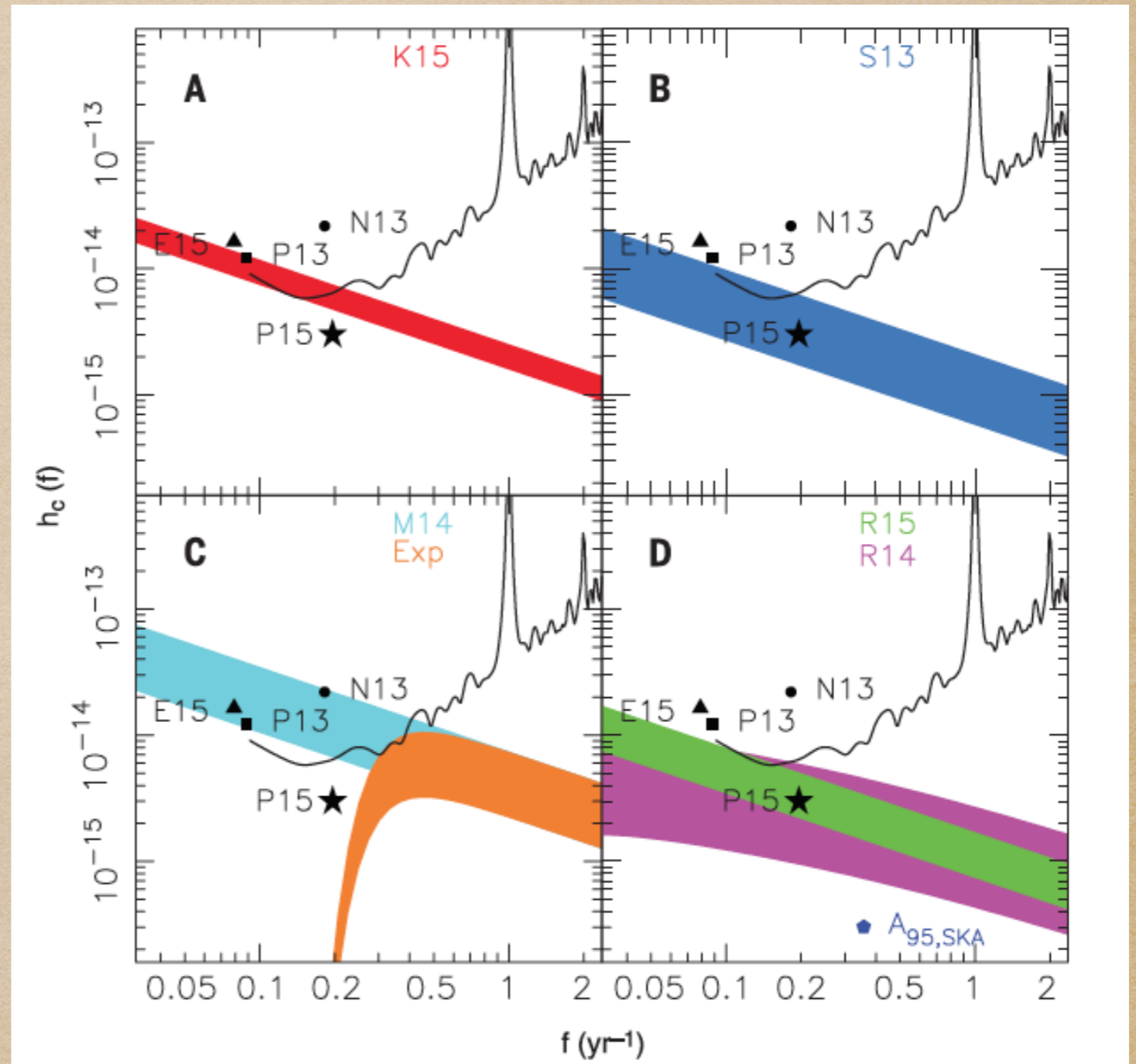
But mostly stochastic background.

Model as power law

$$h_c = A \left( \frac{f}{\text{yr}^{-1}} \right)^\alpha$$

# The very low frequency regime

- So far: upper limits
- E.g. PPTA
- Models excluded?
- Possible explanations:
  - Binaries stalled
  - Accelerated mergers
  - Eccentric orbits
  - ...
- Models too simple



Shannon et al (2015) Science

# The low frequency regime

Supermassive Black Hole Binaries

Compact Object Captures

Galactic White Dwarf Binaries

Cosmic Strings and Phase Transitions

**LISA**  
Laser Interferometer Space Antenna

*Gravity is talking. LISA will listen.*

NASA ESA

Black hole binary at  $z=15$ ,  $10^6 M_{\odot}$ , two hours before merger. Numerical waveform plus instrument noise and WD background (J. Baker)

Booth design by S. Bringham, D. Levitan, S. Finnerty, J. Schuchman, and M. Wellinger

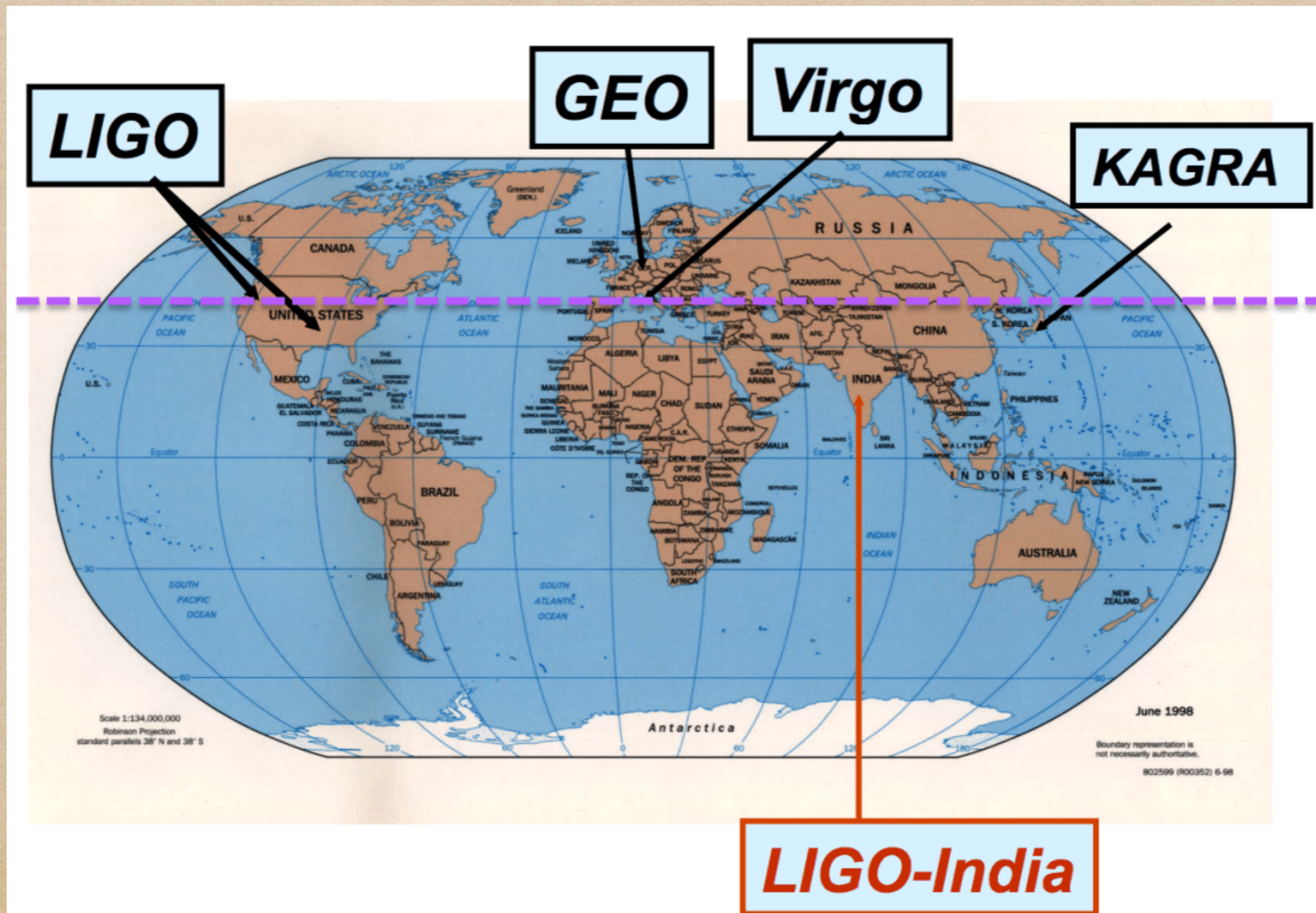
# The low frequency regime

- Interferometry with  $\sim 10^6$  km arms
- Realm of space missions
- LISA: L3 mission of ESA's "Cosmic Vision" Launch:  $\sim 2034$
- Configuration still uncertain:
  - 2 arms vs. 3 arms
  - $10^6$  km vs.  $5 \times 10^6$  km
  - 2 yr vs. 5 yr life span
- Verification binaries (WDs)
- Outstanding SNR
- LISA Pathfinder: Test mission
  - Launched 3 Dec 2015
  - Major success!!!

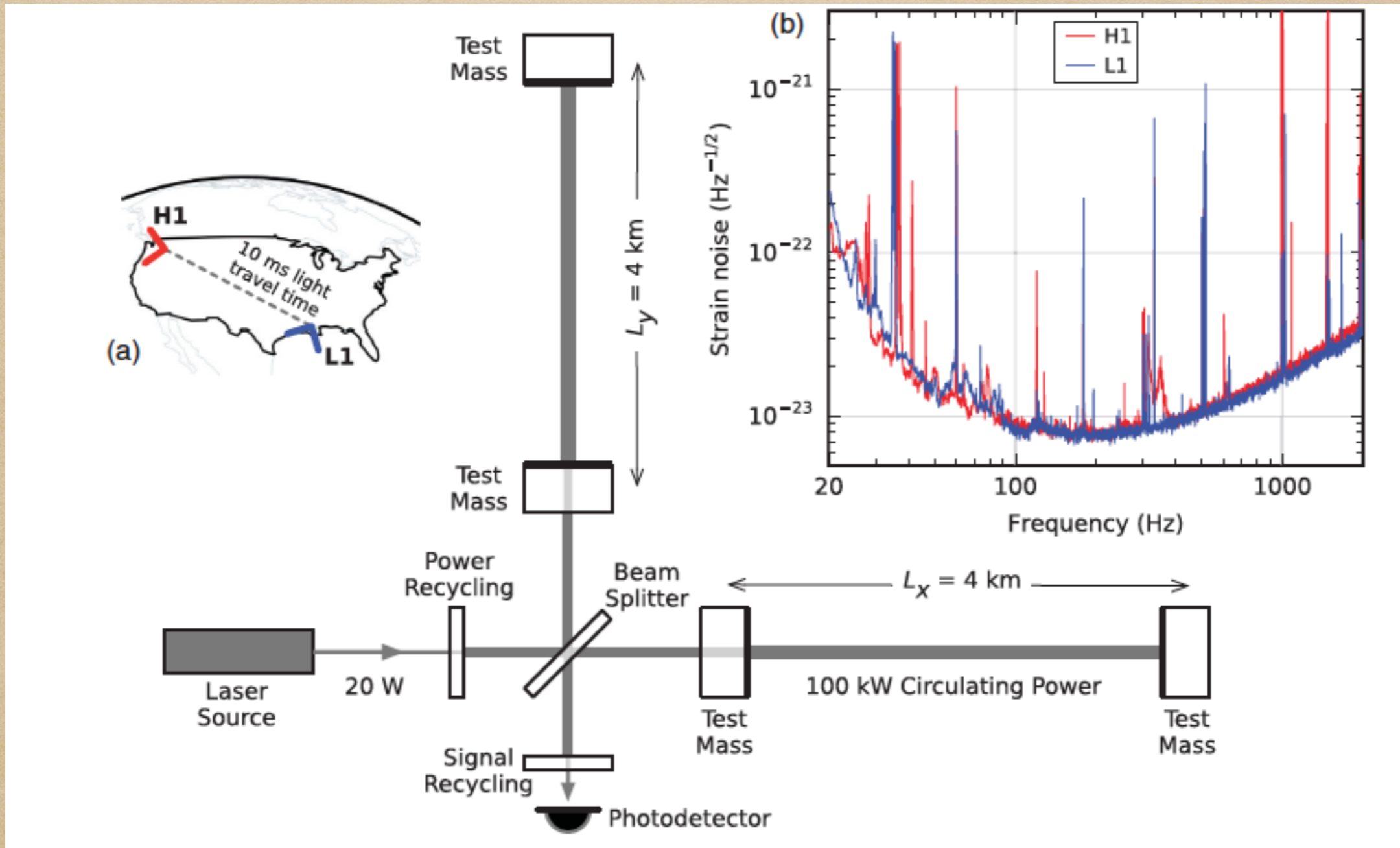


# The high frequency regime

- Interferometry with  $\sim$  km arms
- Detector network:  
2 LIGO (2015), Virgo (2017), GEO600, KAGRA (2020), LIGO-India



# The interferometer diagram: LIGO

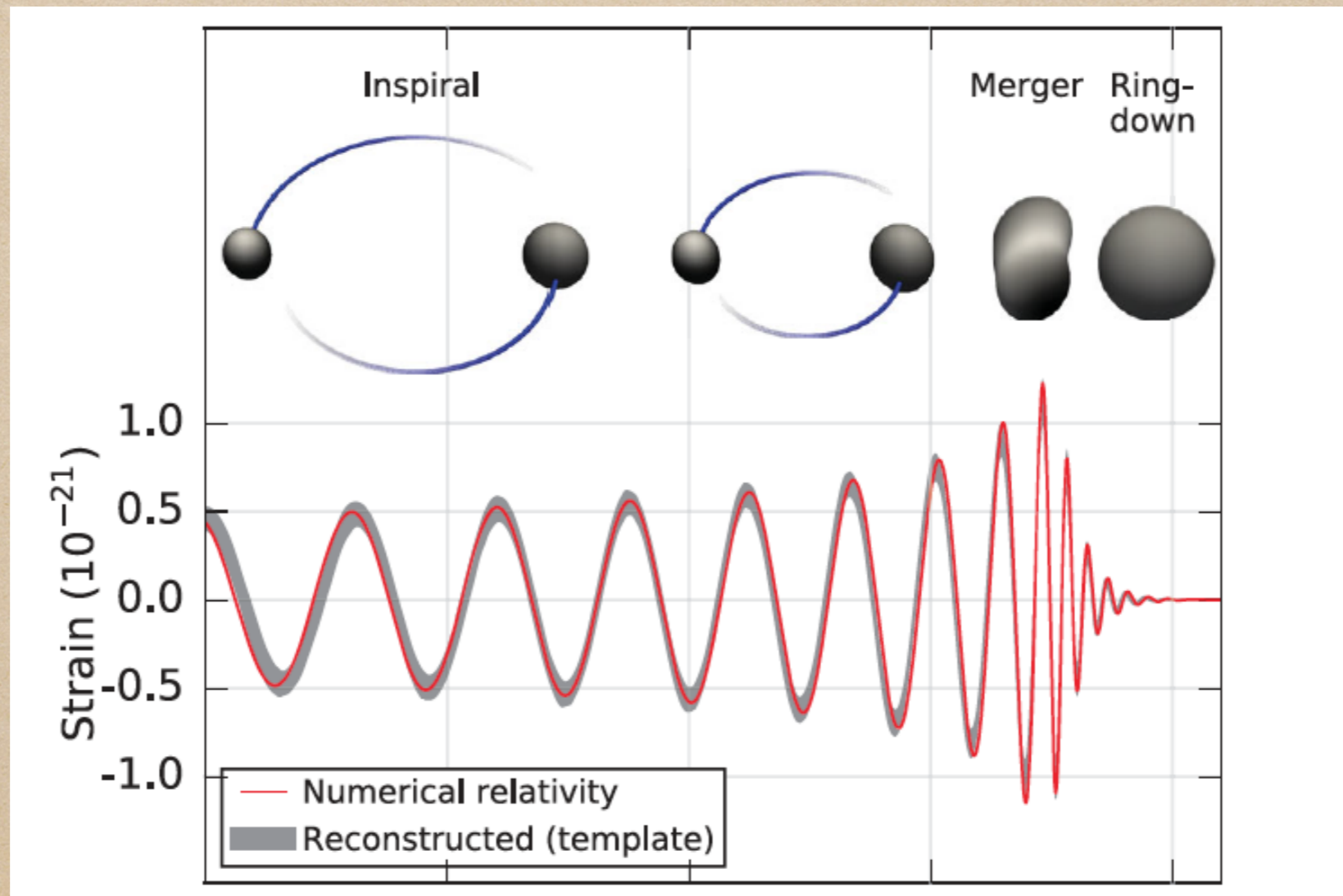


Abbott et al, PRL 116 (2016) 061102

Seismic, thermal, shot noise

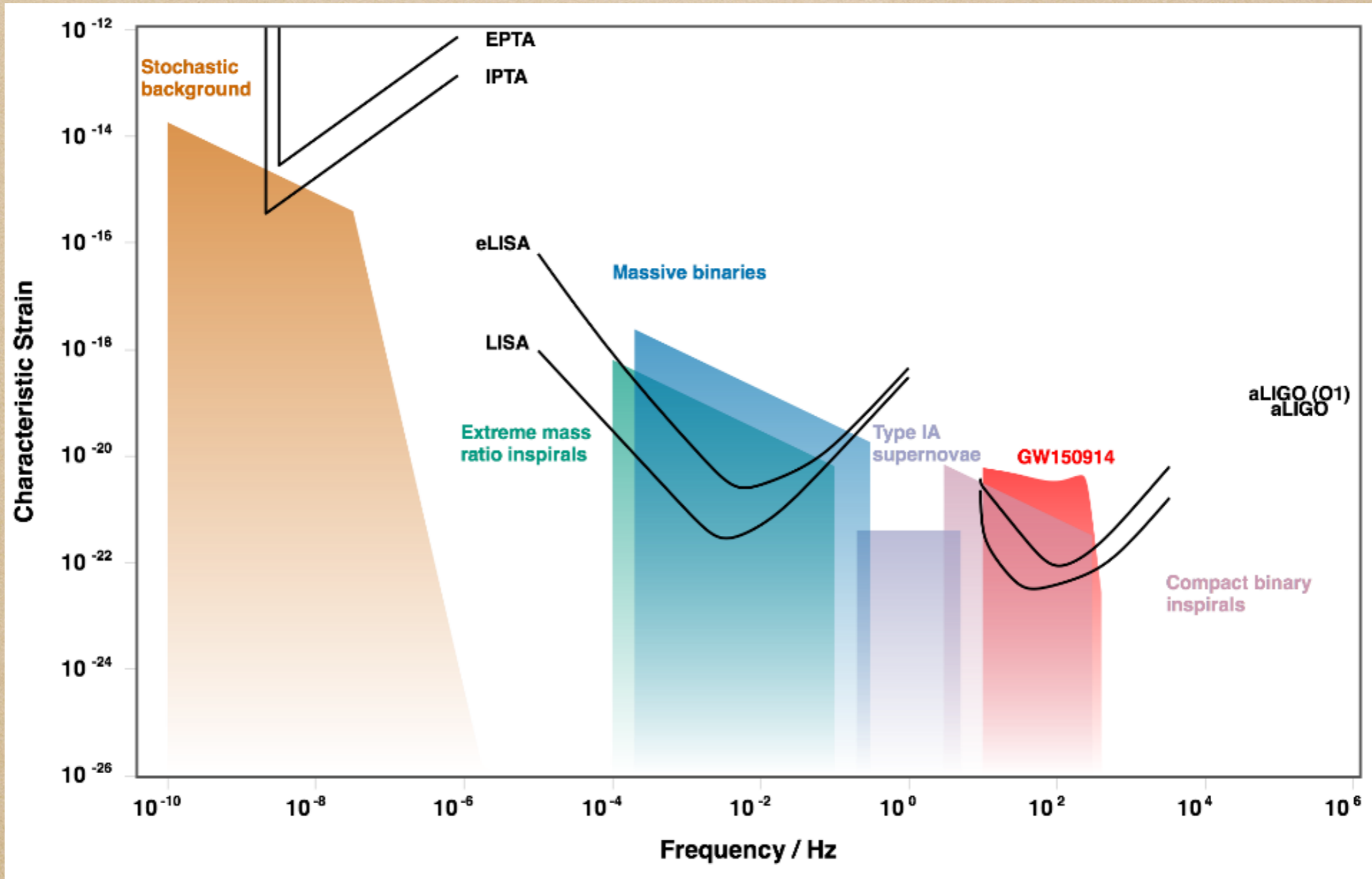
# The high frequency regime

- Supernovae
- Neutron star oscillations
- Neutron star / stellar-mass black hole binaries



Abbott et al, PRL 116 (2016) 061102

# Summary: sensitivity curves



<http://gwplotter.com>

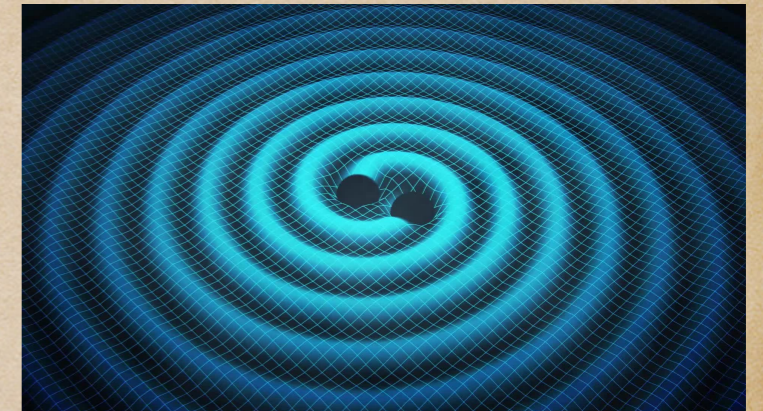


**Parameter estimation and  
source modeling**

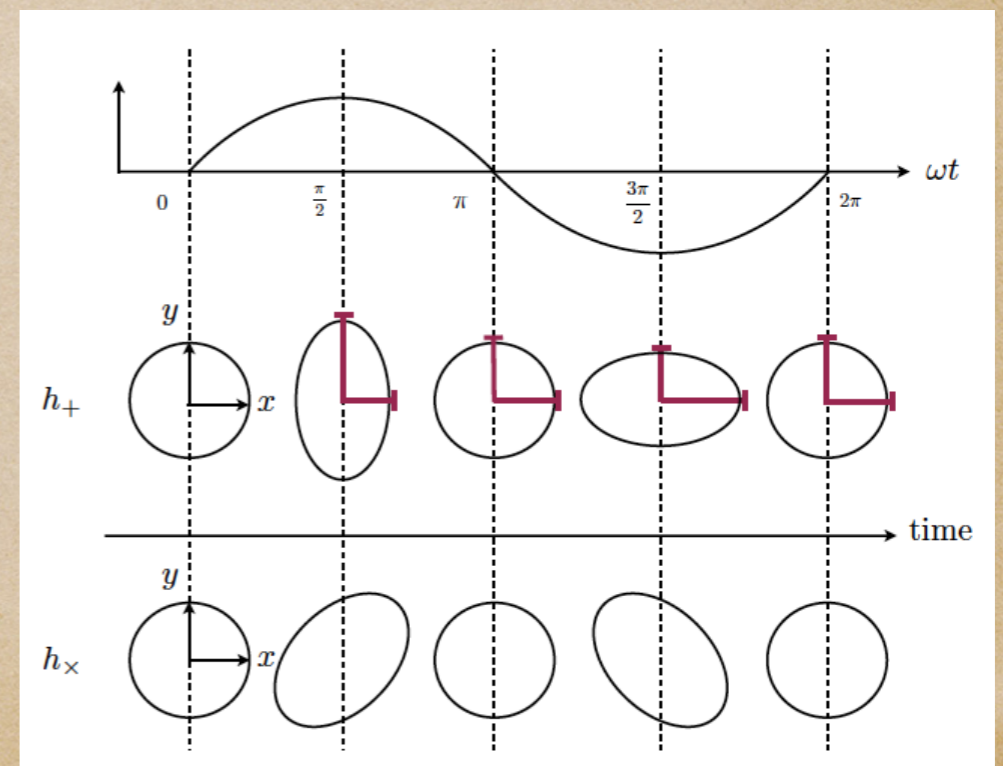
# The search for GWs in the data stream

- Einstein's field equations

$$G_{\mu\nu} = \frac{8\pi G}{c^4} T_{\mu\nu}; \quad \frac{8\pi G}{c^4} = 2.07 \times 10^{-43} \frac{\text{s}^2}{\text{m kg}}$$



- Weak effect of matter on geometry
- GWs carry huge energy but barely interact with anything
- Induced changes in length: < atomic nucleus / km



# Detection and parameter estimation

## Generic transient search

- No specific waveform model
- Identify excess power in detector strain data
- Use multi detector maximum likelihood Klimenko et al. 1511.05999

## Binary coalescence search

- "Matched Filtering"
- Compare data stream with GW templates ("Finger print search")
- Bayesian analysis:  
Prior  $\rightarrow$  Posterior



# Black-hole binaries: parameters

- 8+1 Intrinsic parameters

Masses  $m_1, m_2$

Spins  $S_1, S_2$

Eccentricity (often ignored; GW emission circularizes orbit)

- 7 Extrinsic parameters

Location: Luminosity distance  $D_L$ , Right ascension  $\alpha$ , Declination  $\delta$

Orientation: Inclination  $\iota$ , Polarization  $\psi$

Time  $t_c$  and Phase  $\phi_c$  of coalescence

- Other parameters

Anything beyond vacuum GR.... (ignored for starters...)

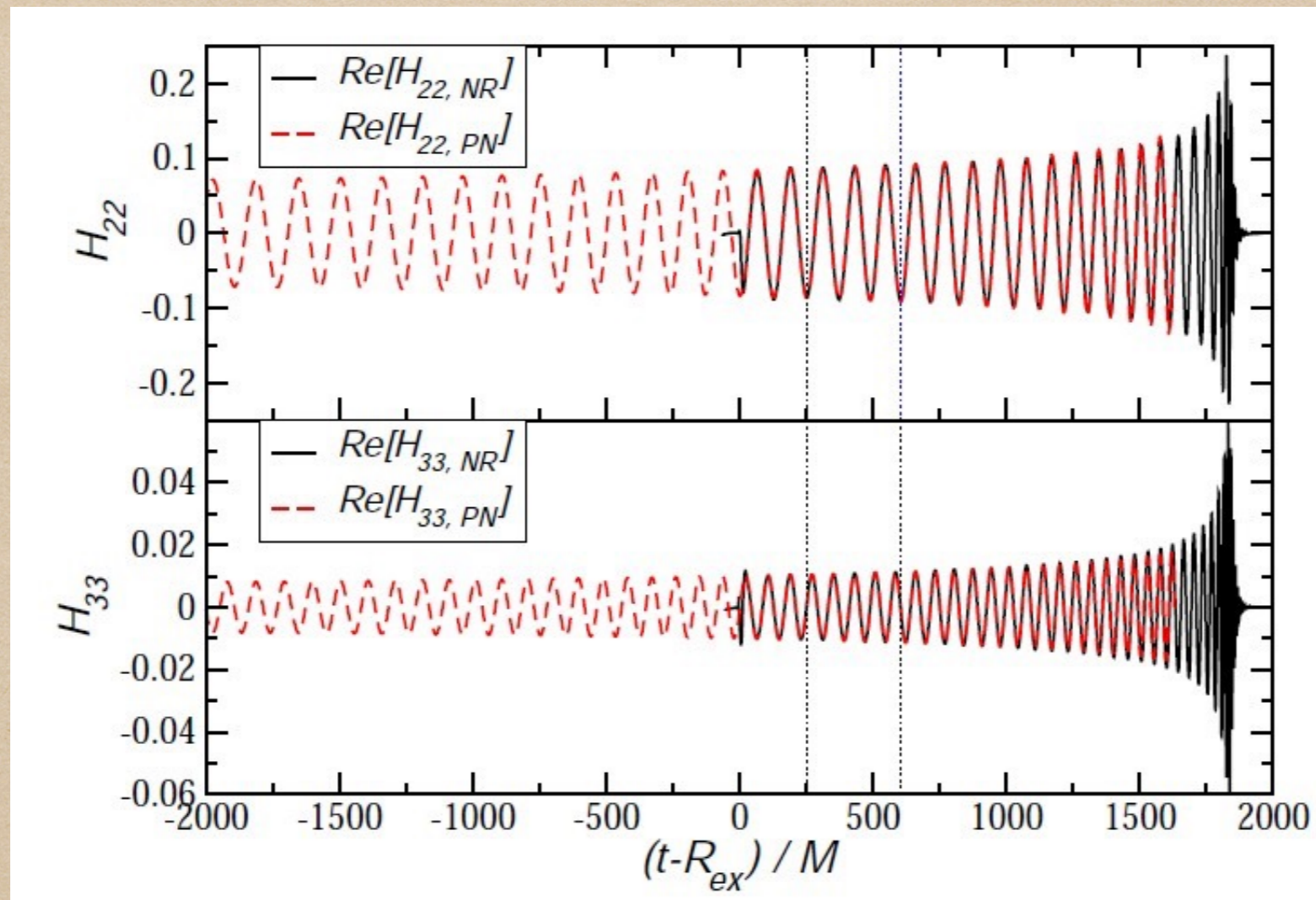
# GW source modeling

- Key requirement for matched filtering: GW template catalog
- Model black holes in general relativity
  - Post Newtonian theory → Inspiral Blanchet Liv.Rev.Rel. 2006
  - Numerical relativity → final orbits, merger  
Pretorius PRL 2005, Baker et al PRL 2006, Campanelli et al PRL 2006
  - Perturbation theory → Ringdown
- Combine "NR" with "Post-Newtonian", "Effective one body" methods
- 2 families in use: Phenomenological, Effective one body
- Use reduced bases or similar to cover parameter space
- Multipolar decomposition

$$h_+ - ih_\times = \sum_{\ell m} -2Y_{\ell m}(\theta, \phi)h_{\ell m}(t)$$

# Hybrid waveforms and catalogs

- Stitch together PN and NR waveforms



US et al CQG 2011

- Mass produce waveforms;

Hinder et al CQG 2013, Mroué et al PRL 2013, Boyle et al CQG 2019

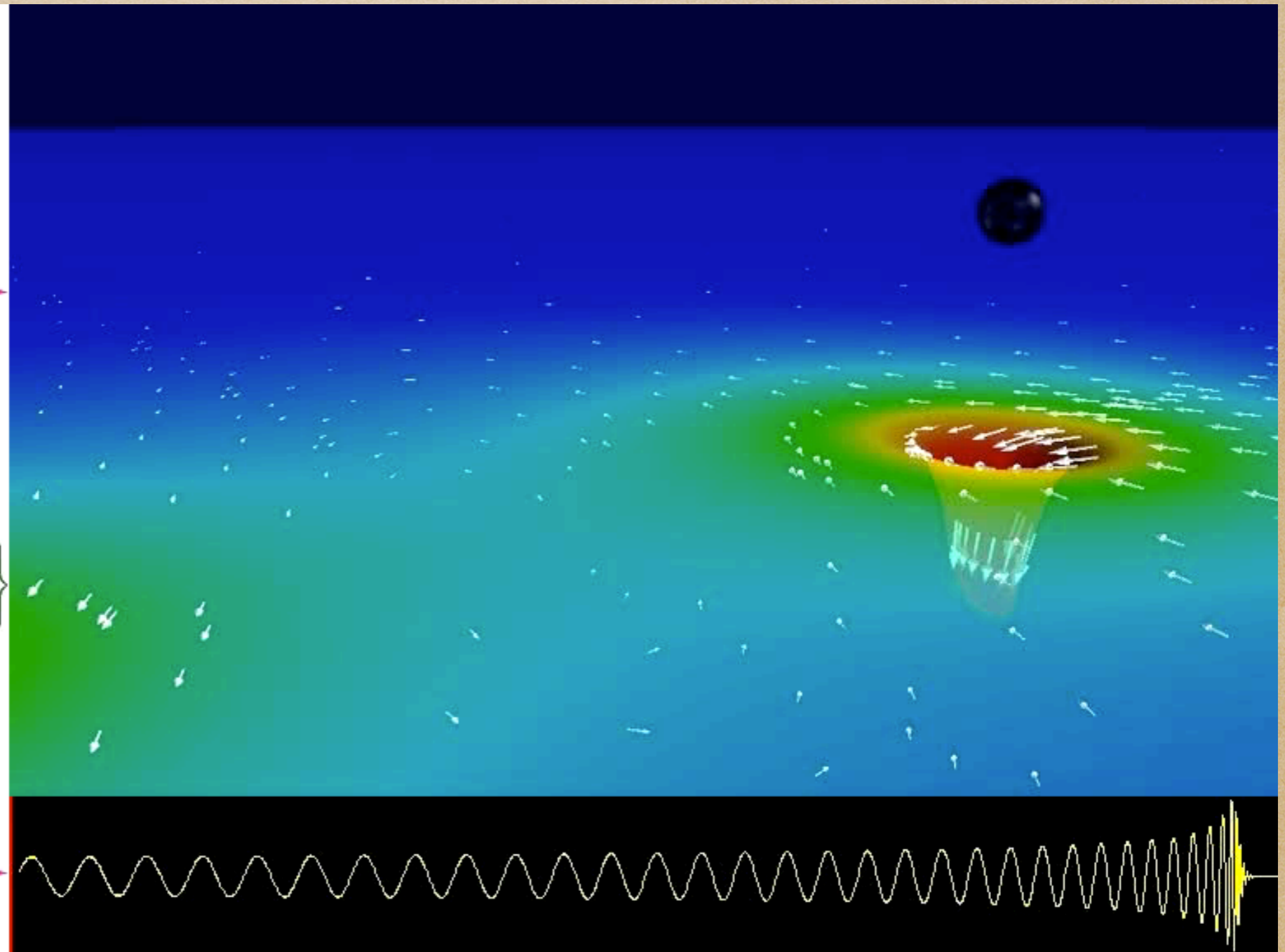
# Anatomy of a BHB coalescence

Binary Black Hole Evolution:  
Caltech/Cornell Computer Simulation

Top: 3D view of Black Holes  
and Orbital Trajectory

Middle: Spacetime curvature:  
Depth: Curvature of space  
Colors: Rate of flow of time  
Arrows: Velocity of flow of space

Bottom: Waveform  
(red line shows current time)

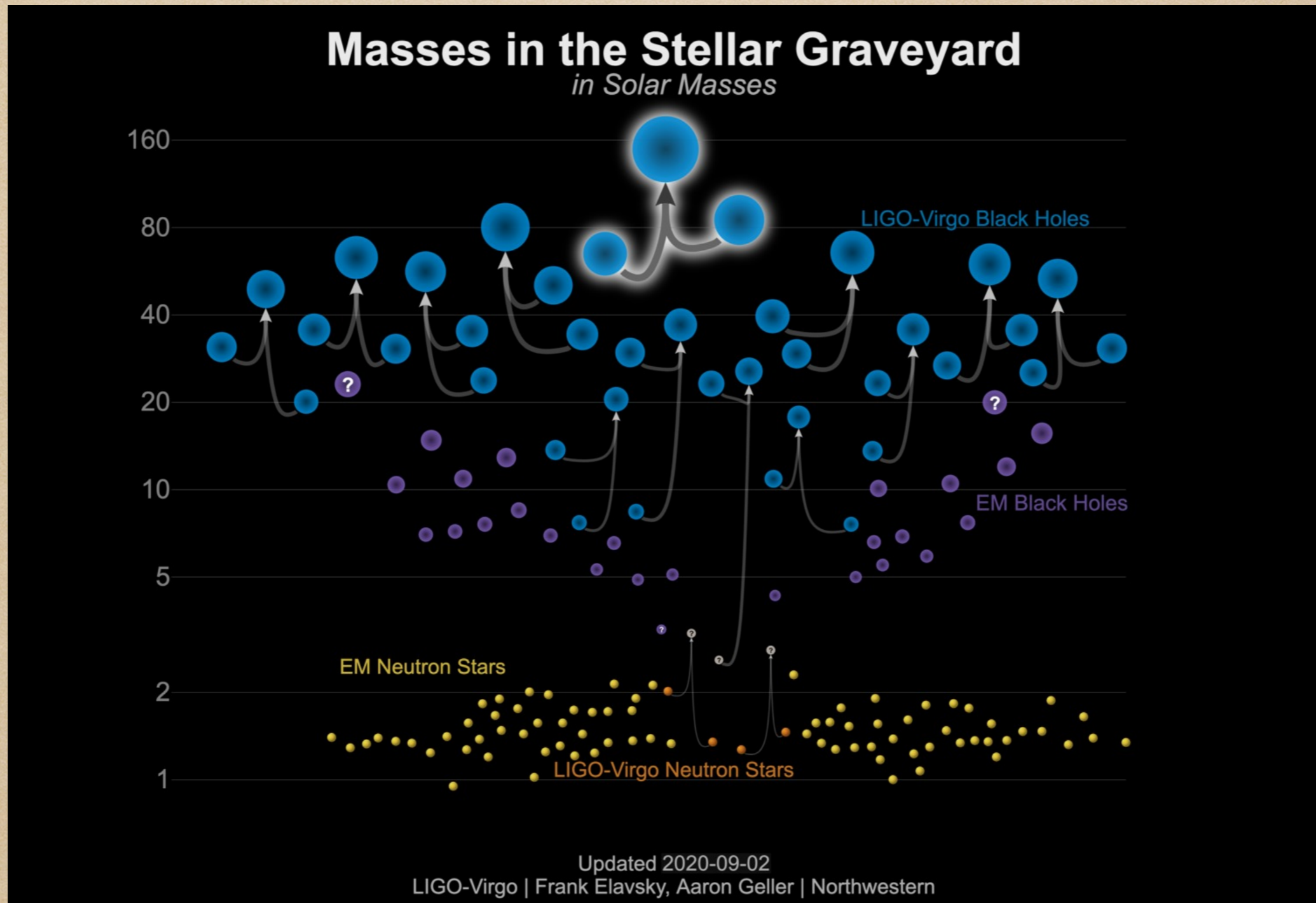


Thanks to Caltech-Cornell groups

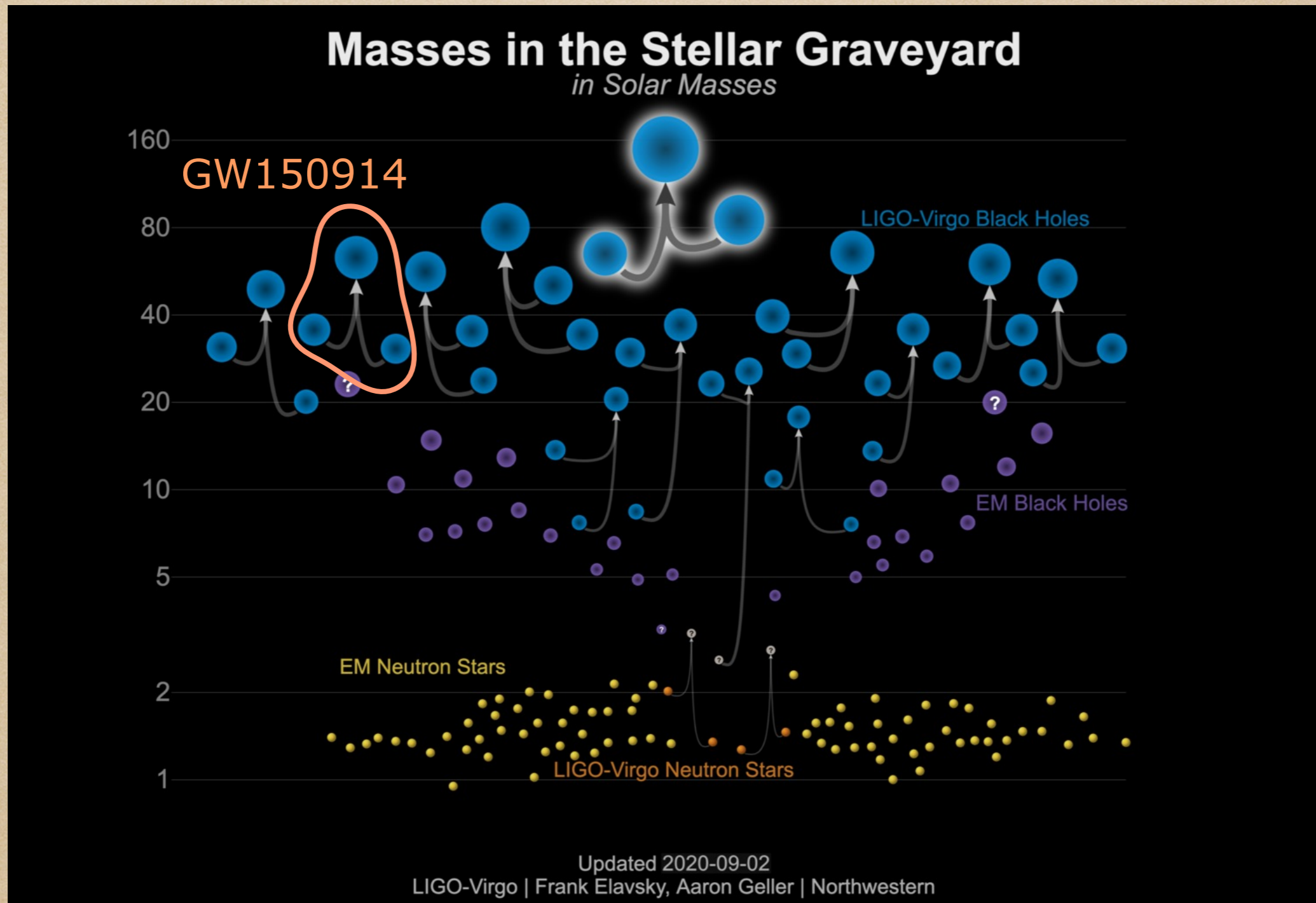
**The GW events**



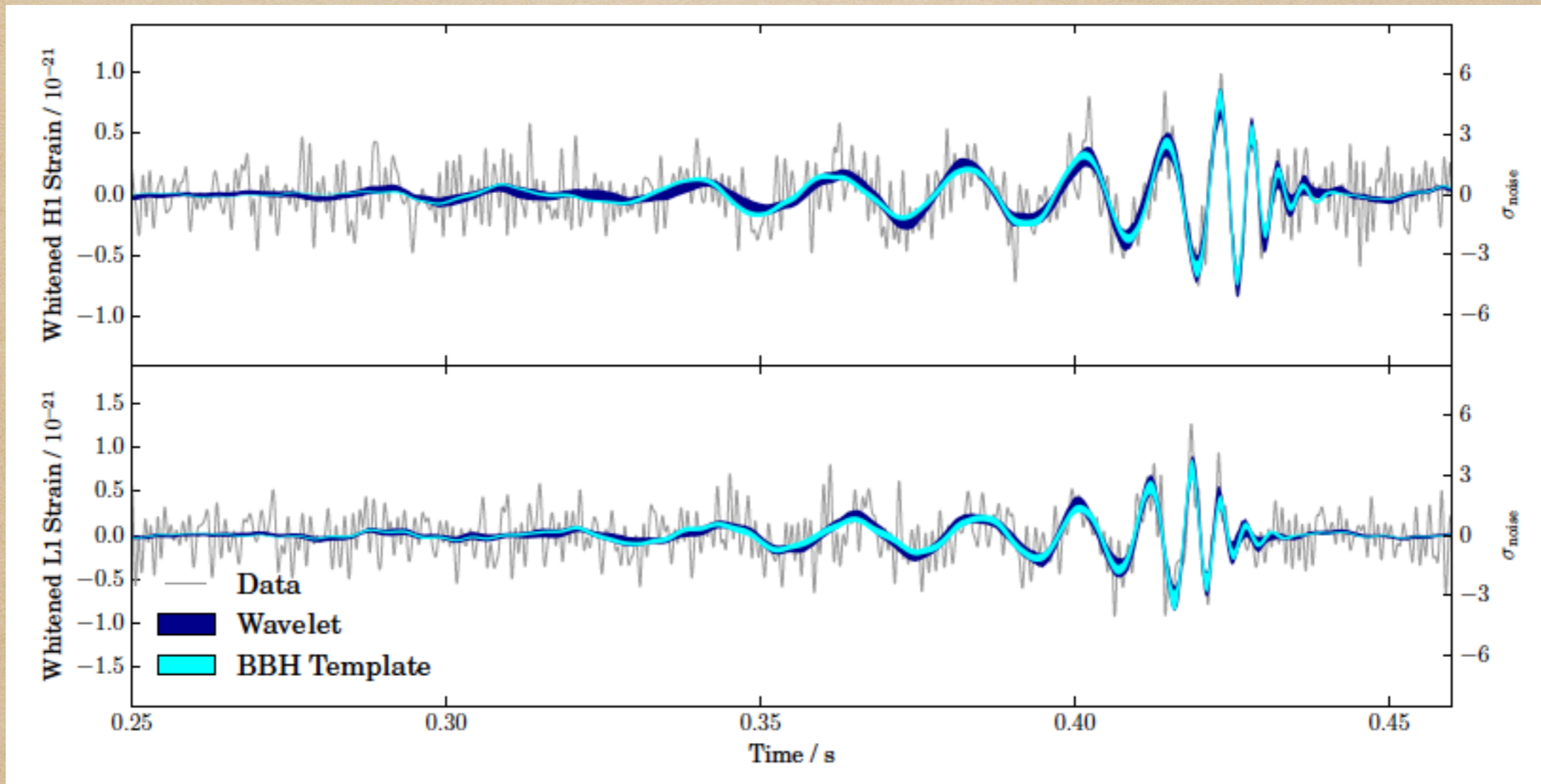
# GW detections as of 2020



# GW150914



# GW150914: The signal



Abbott et al 1602.03840

- Whitened by power spectral density
- Wavelet = Linear combination of sine-Gaussian pieces

# GW150914: BH masses

- Source frame
- 2 Waveform models

Abbott et al. 1602.03840

$$m_1 = 36^{+5}_{-4} M_{\odot}$$

$$m_2 = 29^{+4}_{-4} M_{\odot}$$

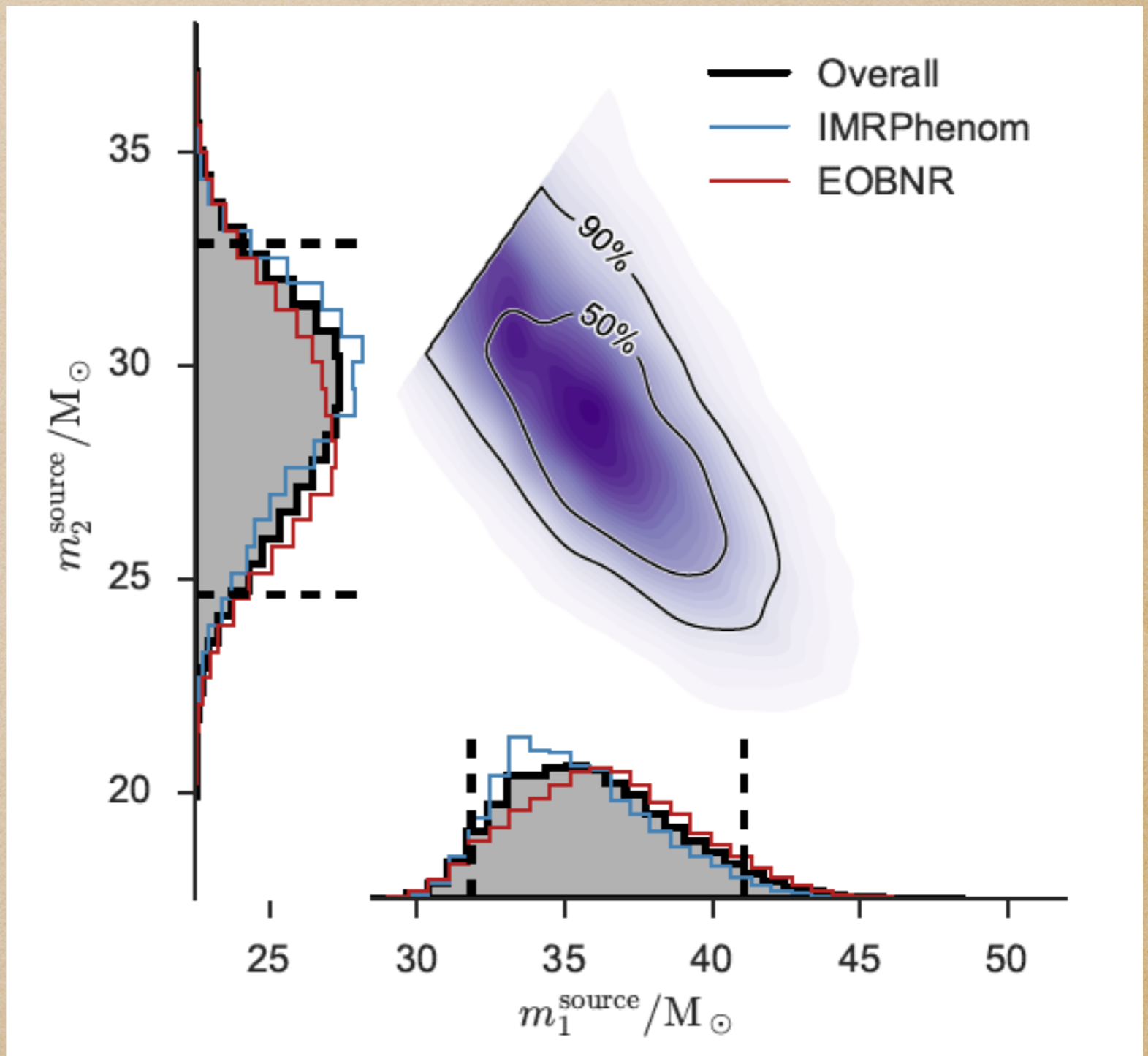
$$M_{\text{fin}} = 62^{+4}_{-4} M_{\odot}$$

- Deficit in GWs!

$$\Delta M \approx 3 M_{\odot}$$

$$\approx 5.4 \times 10^{54} \text{ erg}$$

$$L_{\text{max}} \approx 3.6 \times 10^{56} \text{ erg/s}$$



Abbott et al 1602.03840

# GW150914: BH parameters

- Mass ratio  $q \equiv \frac{m_2}{m_1} = 0.65 \pm 0.03$

- Spins harder to measure: few cycles, no full-precession catalog

$$\chi_1 = \frac{|\mathbf{S}_1|}{m_1^2} < 0.7, \quad \chi_2 = \frac{|\mathbf{S}_2|}{m_2^2} < 0.9$$

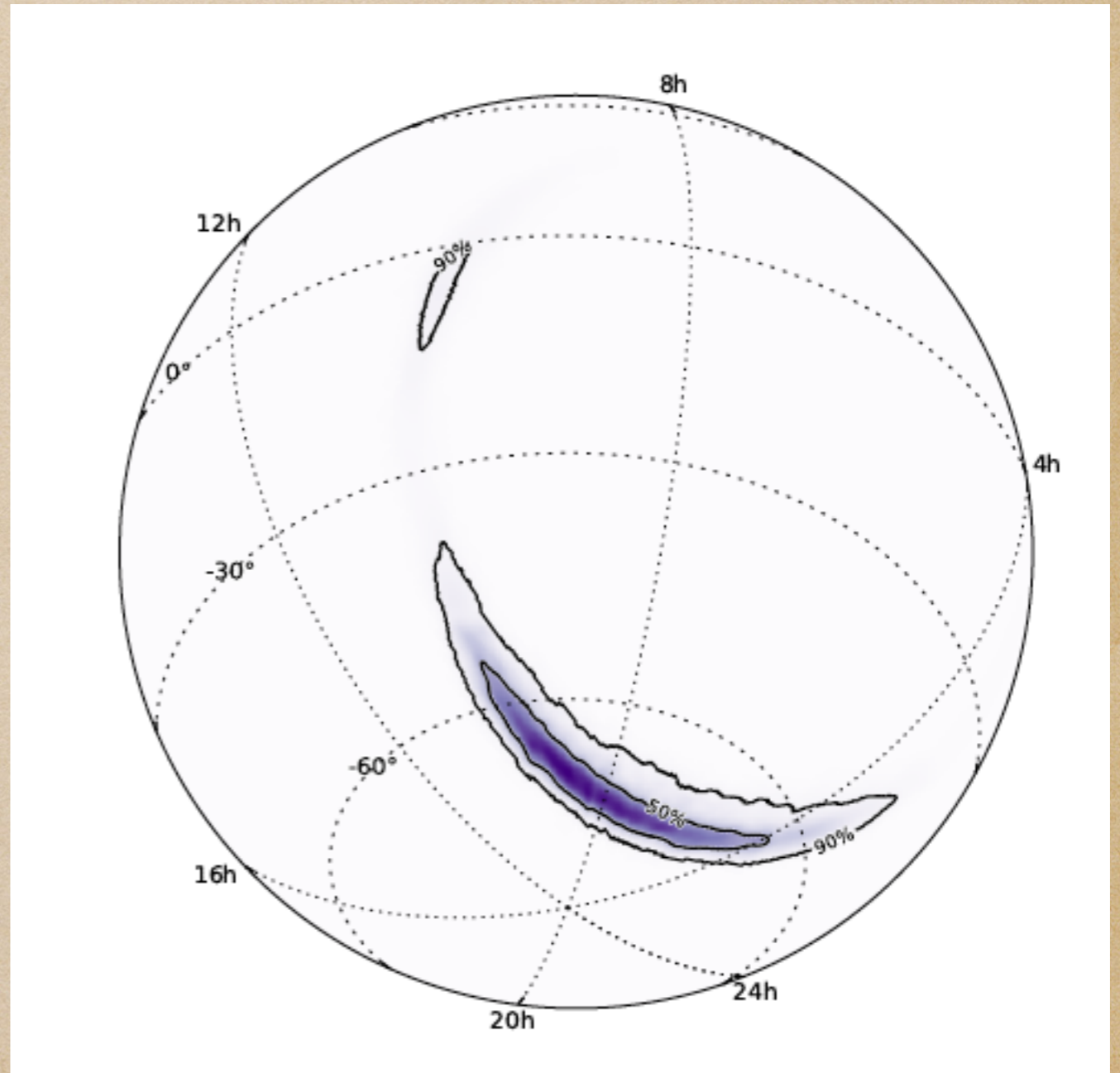
$$\chi_{\text{fin}} = 0.67^{+0.05}_{-0.07}$$

- Luminosity distance  $D_L = 410^{+160}_{-180}$  Mpc

- Source redshift  $z = 0.088^{+0.031}_{-0.038}$

# GW150914: Sky location

- Important for EM follow-up
- GW detectors are all-sky
- Via triangulation
- 2 detectors
  - ~ 590 deg<sup>2</sup>
- Southern hemisphere
- To be improved with  
Virgo, KAGRA, LIGO India

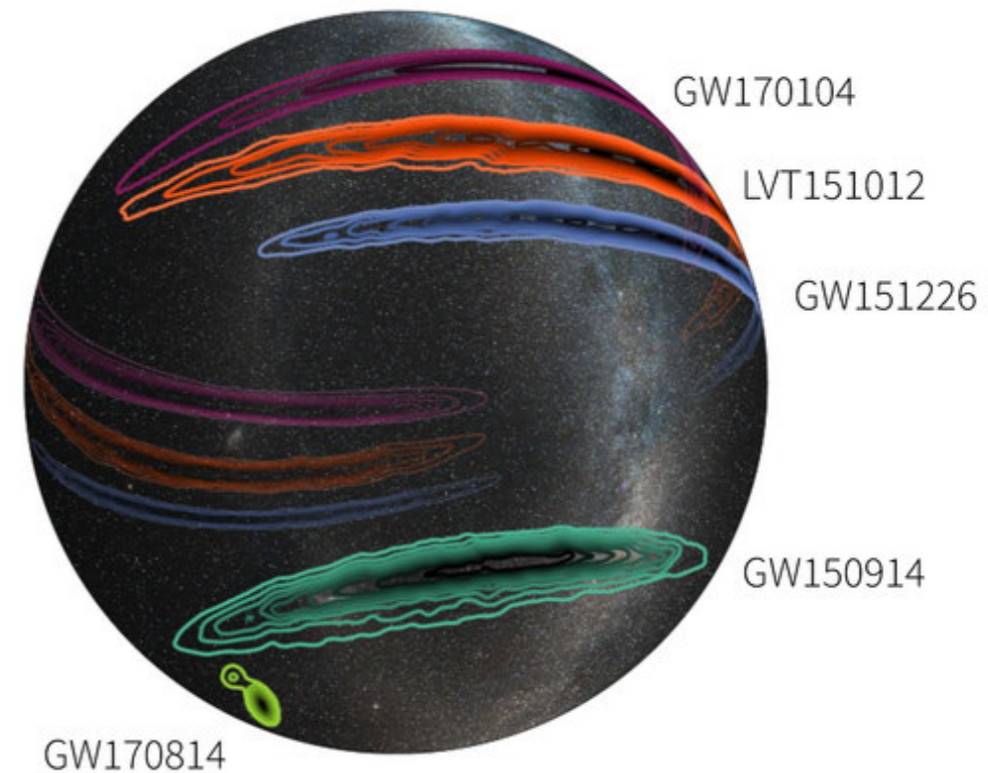


Abbott et al 1602.03840

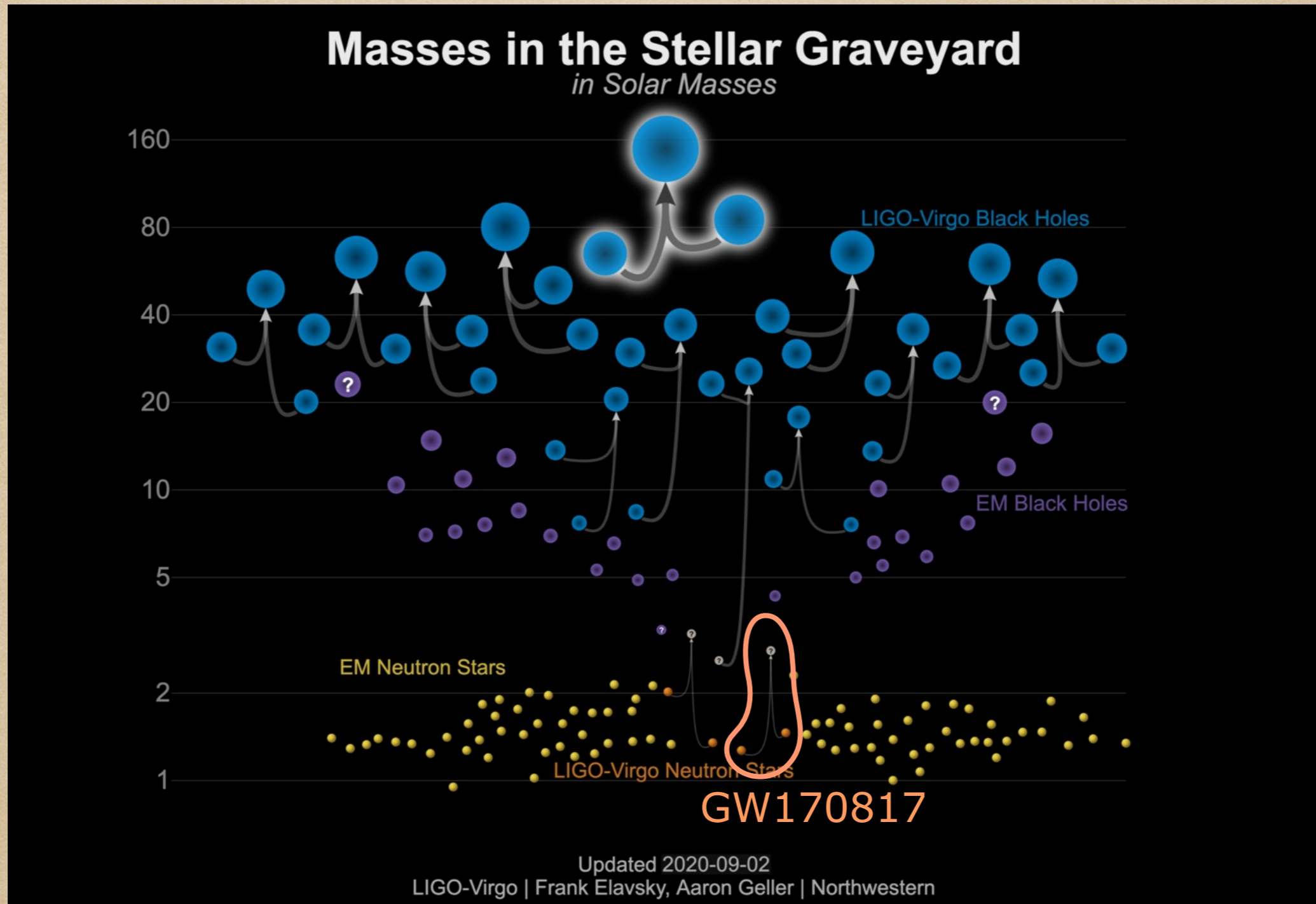
# 2017: Virgo joins O2



- 3 detectors
- much improved sky location!
- First triple coincidence detection GW170814



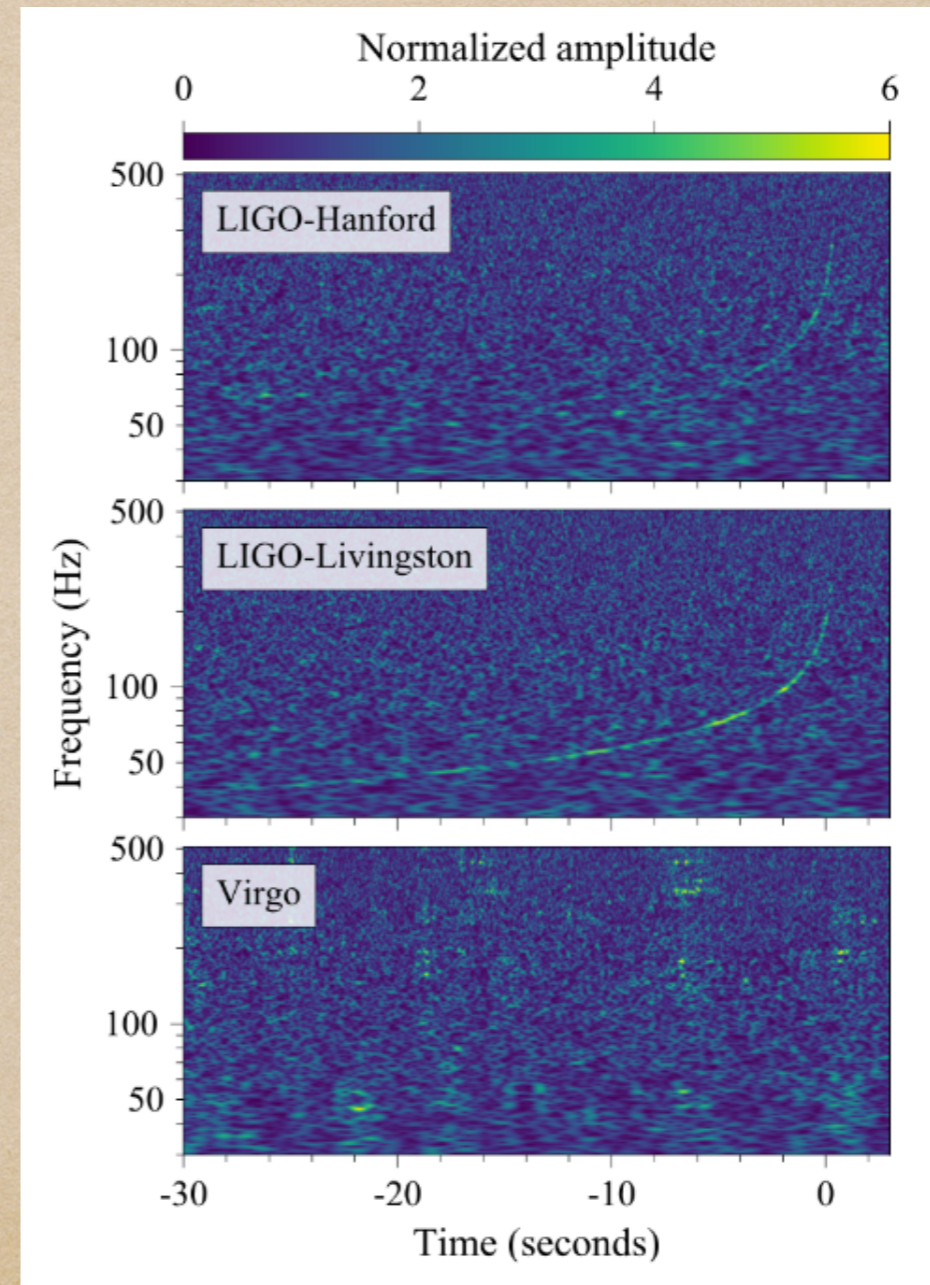
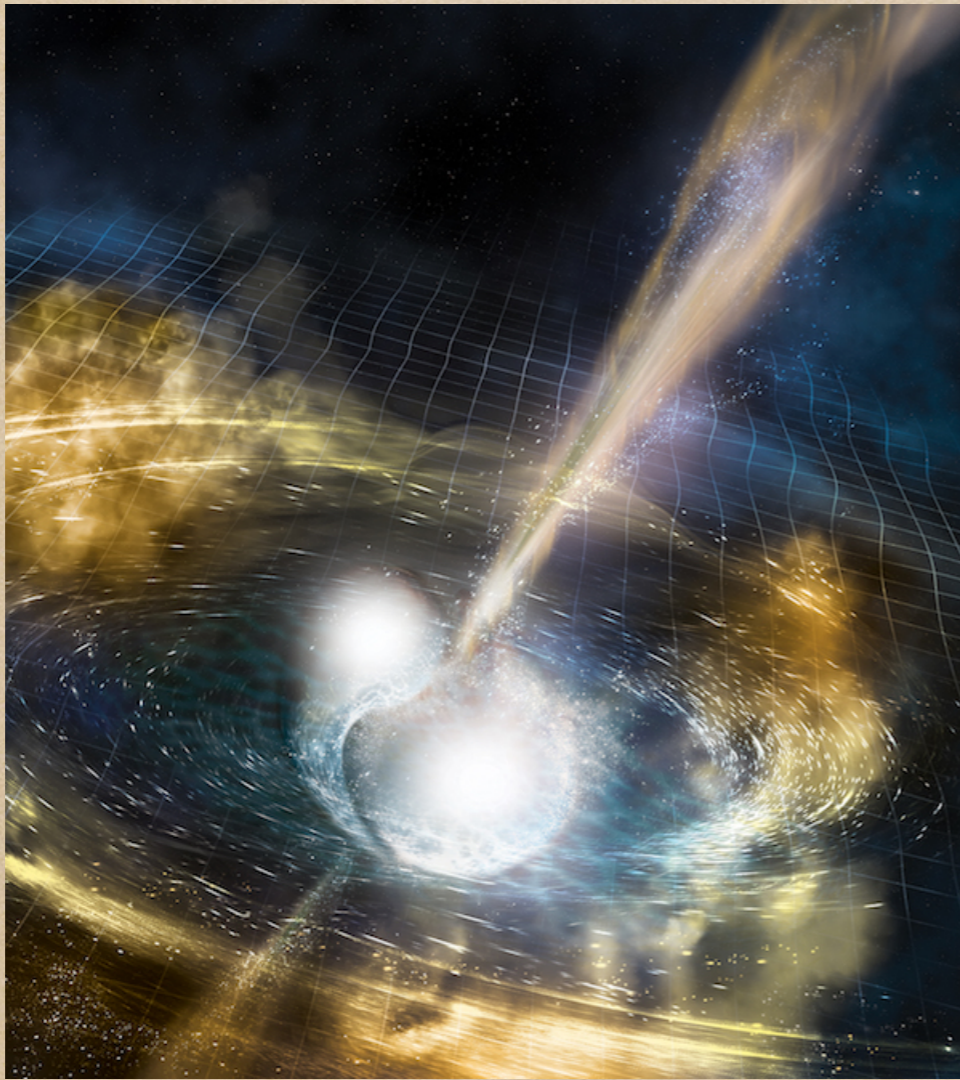
# GW170817





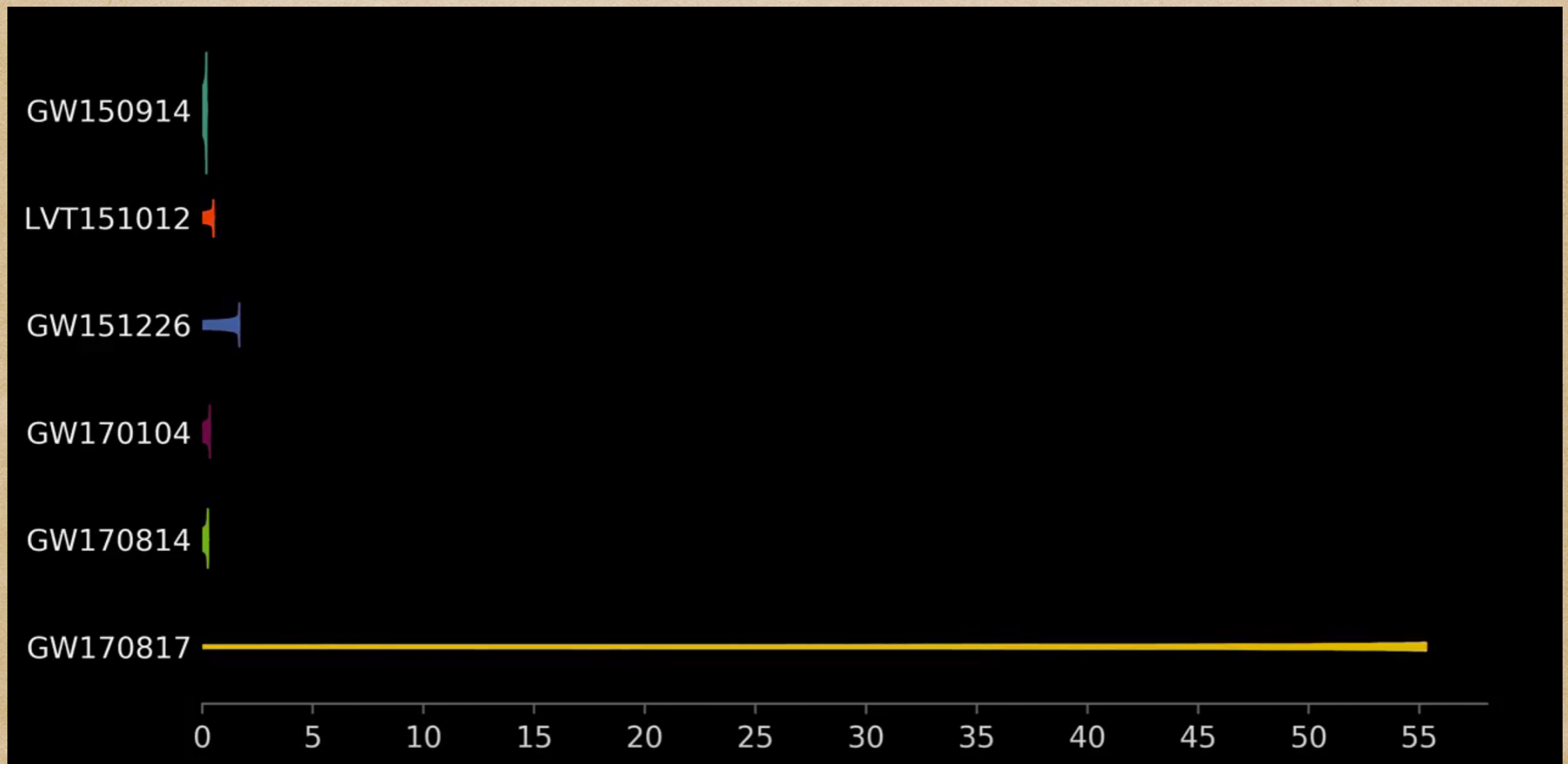
# GW170817: Binary Neutron Star Merger

- Fermi and Gamma-Ray Burst Monitor send GRB170817A alert
- Within 6 minutes, LIGO, Virgo find GW170817 in the data stream



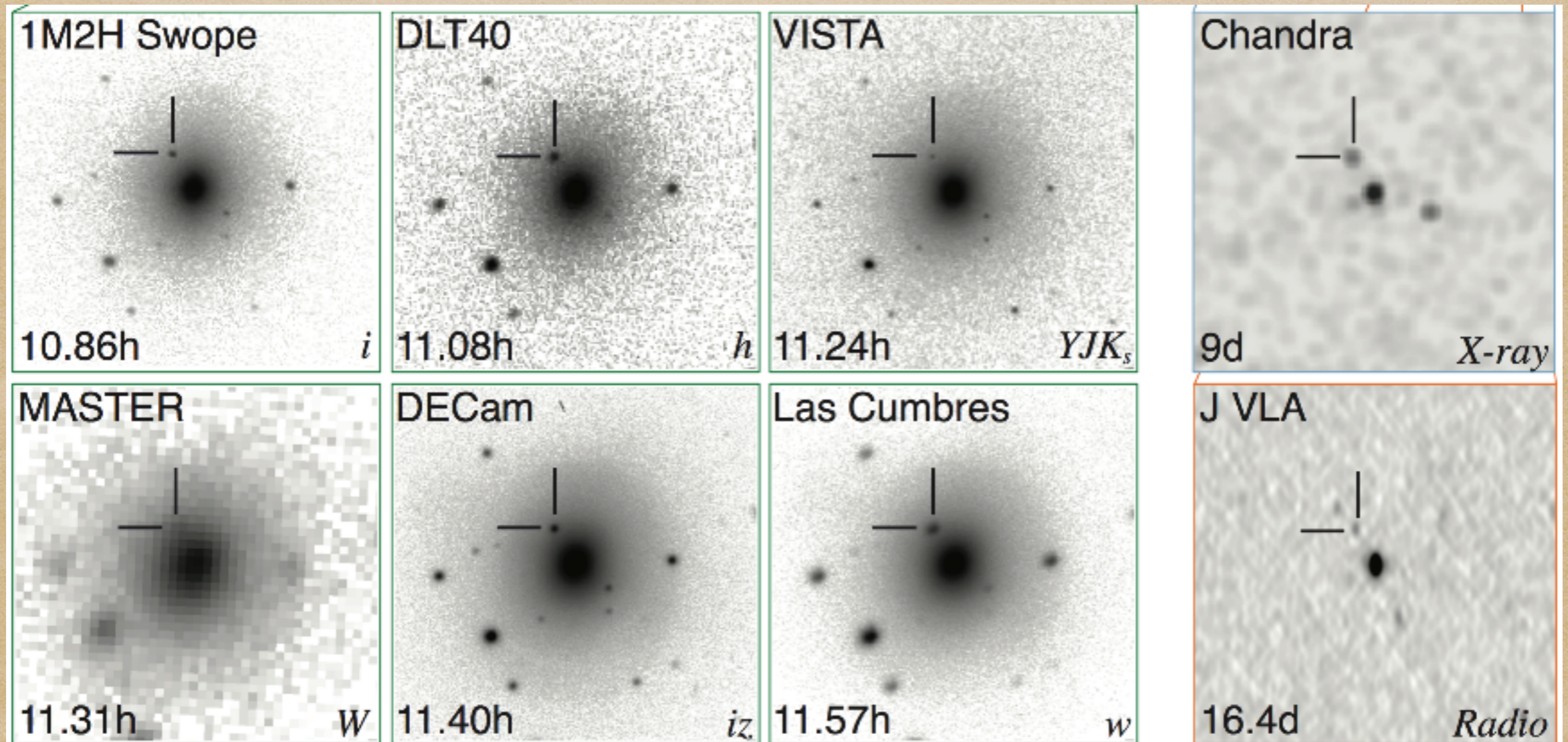
# GW170817: Binary Neutron Star Merger

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- Within 6 minutes, LIGO, Virgo find GW170817 in the data stream
- Note the duration!!!

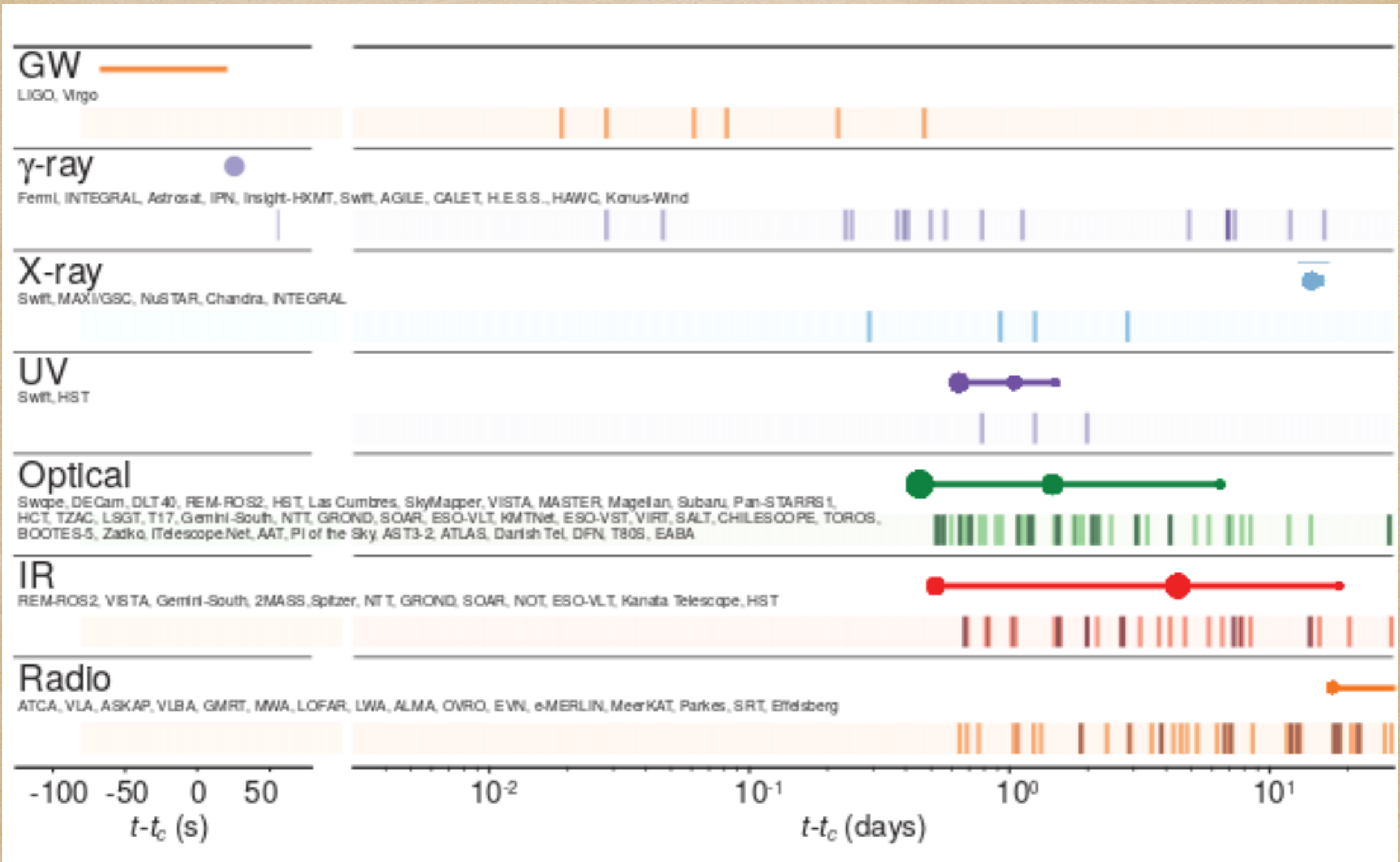


# GW170817: Multi messenger astronomy

- Gravitational Waves, Gamma rays
- Optical: 6 left panels
- X-ray, Radio: Chandra, Jansky VLA



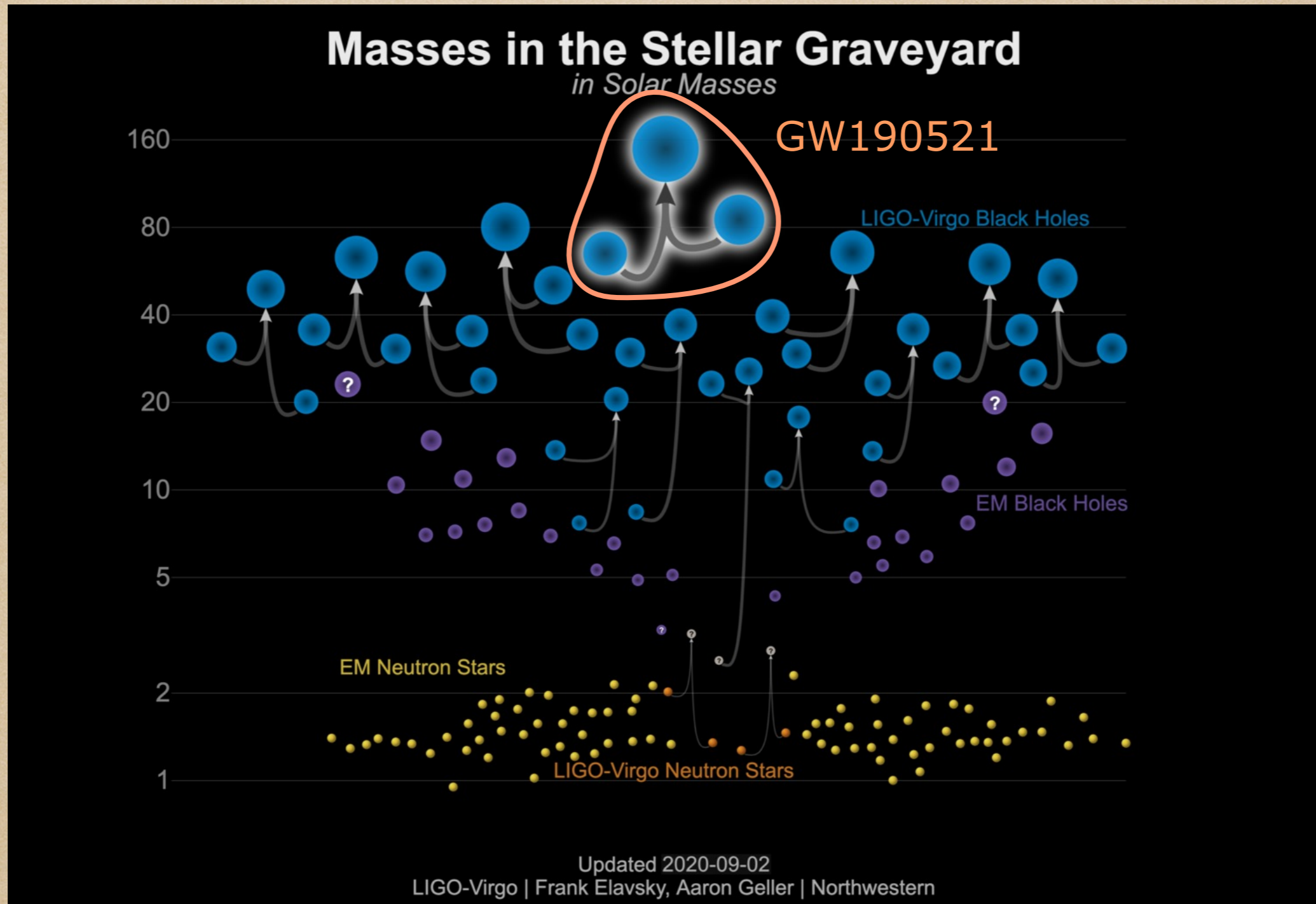
# GW170817: Multi messenger astronomy



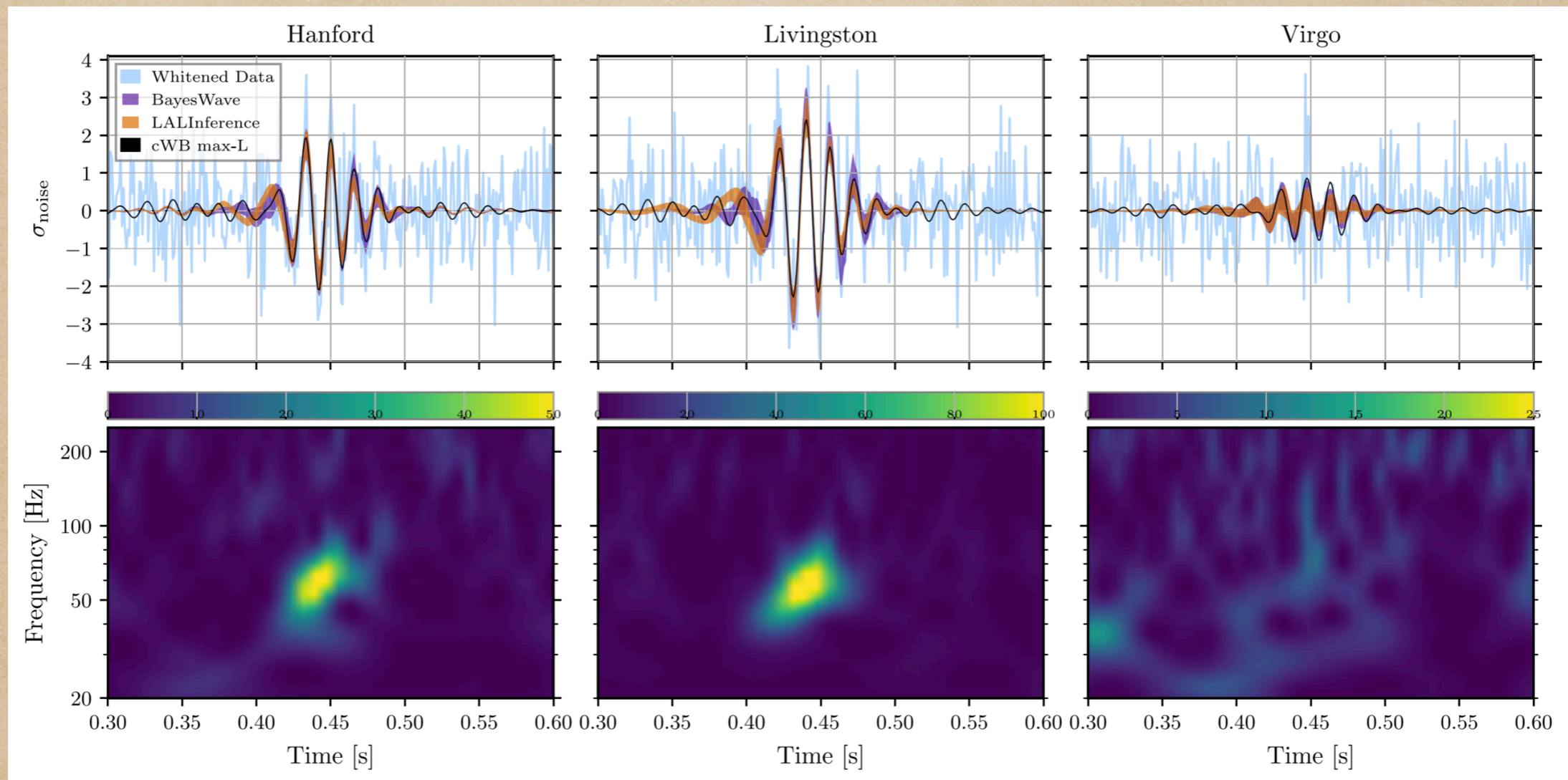
# Some things we have learned

- GRB associated with Binary Neutron Star Merger
- Kilonova (infrared transient) due to decay of heavy elements
- Independent measurement of Hubble constant:  
$$H_0 = 70_{-8}^{+12} \text{ km s}^{-1} \text{ Mpc}^{-1}$$
- Binary NS merger rate:  $1540_{-1220}^{+3200} \text{ Gpc}^{-3} \text{ yr}^{-1}$
- First insight into EOS at supernuclear densities through tidal effects
- Results will improve with more NS events

# GW190521

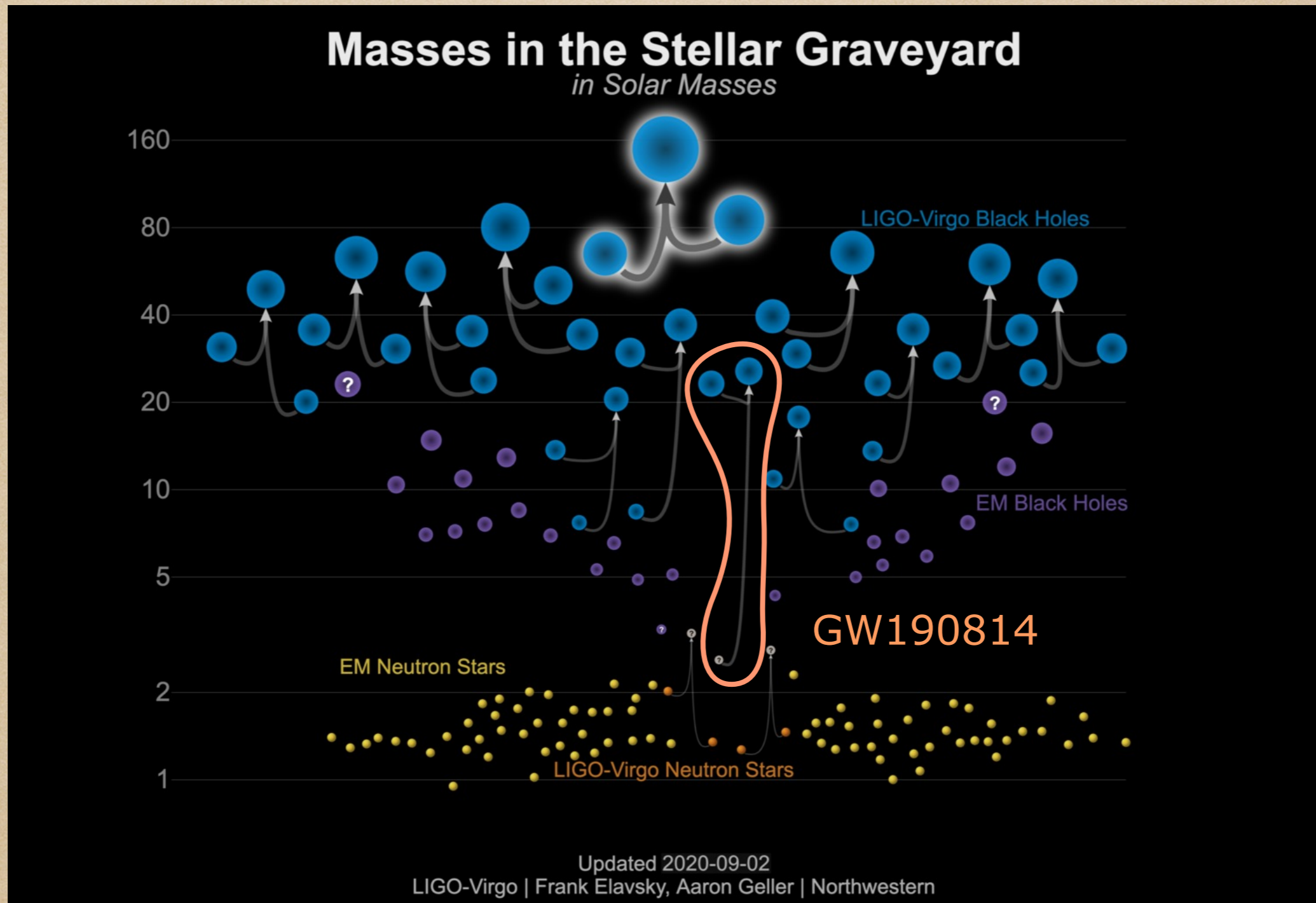


# GW190521



- Progenitor masses:  $m_1 = 91 M_{\odot}$ ,  $m_2 = 67 M_{\odot}$
- Remnant mass:  $M = 150 M_{\odot} \stackrel{!}{=} m_1 + m_2$  Abbott et al. 2010.14527
- Mass defect  $\Delta M \approx 8 M_{\odot}$  ; cf. Tsar Bomba:  $\Delta M \approx 2.65 \text{ kg}$
- Open questions: How did the progenitor BHs form? Is it a BBH?

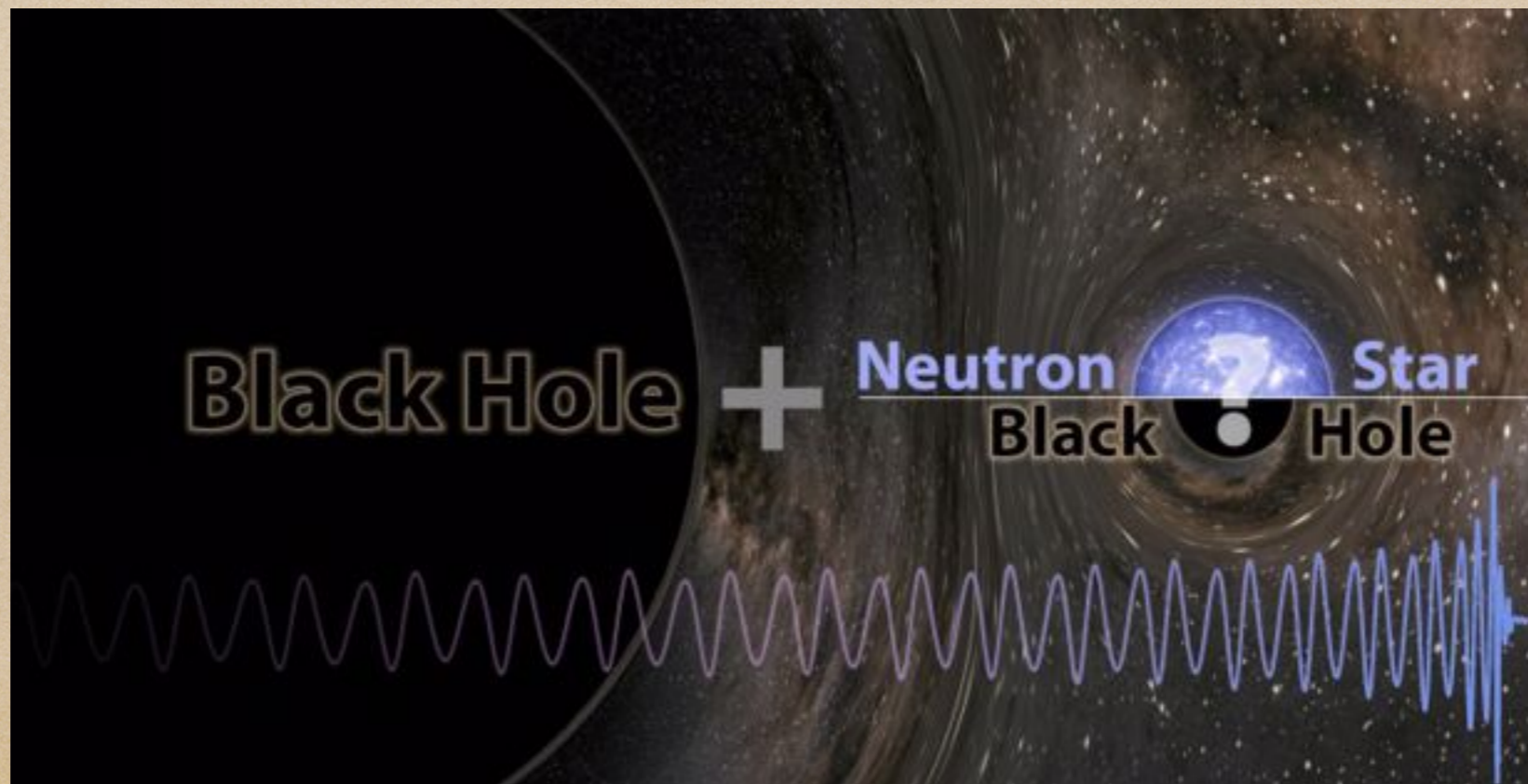
# GW190814





# GW190521

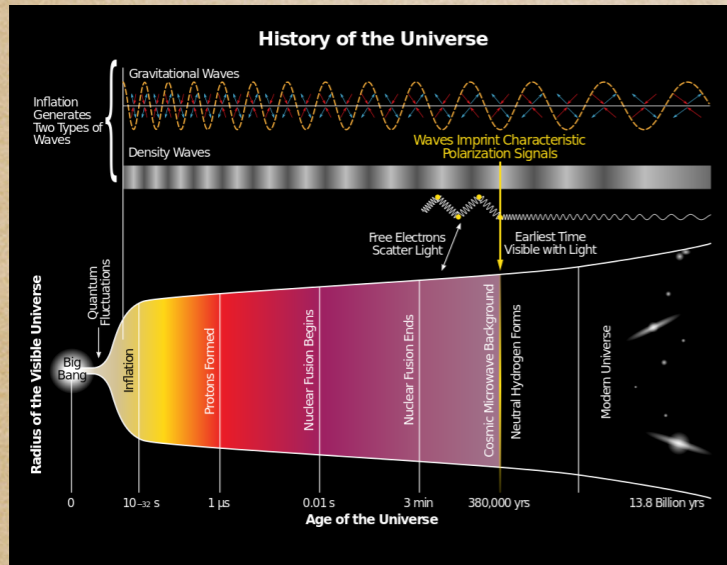
- Progenitor masses:  $m_1 = 23.2 M_{\odot}$ ,  $m_2 = 2.59 M_{\odot}$
- Remnant mass:  $M = 25.6 M_{\odot}$  Abbott et al. 2010.14527
- Key question: What is the secondary?
  - The heaviest neutron star ever seen?
  - The lightest black hole ever seen?
  - An exotic compact object? Wormhole or Boson Star or ...



**(Selected) Future applications**

# Overview

## Early Universe



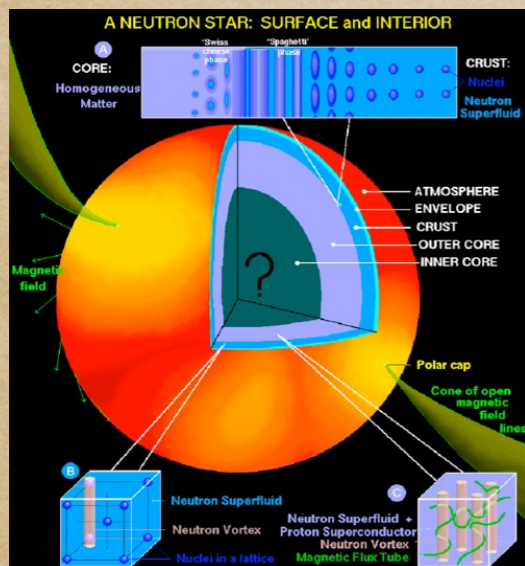
## Testing Einstein's theory



## Galaxy history



## Equation of state



## BH populations



## The unknown...



# Testing GR with GW170817: Graviton mass

- Phenomenological model
- Massive graviton  $\Rightarrow$  Compton wavelength  $\lambda_g = \frac{h}{m_g c}$
- Dispersion relation:  $\frac{v_g^2}{c^2} = 1 - \frac{h^2 c^2}{\lambda_g^2 E^2}$

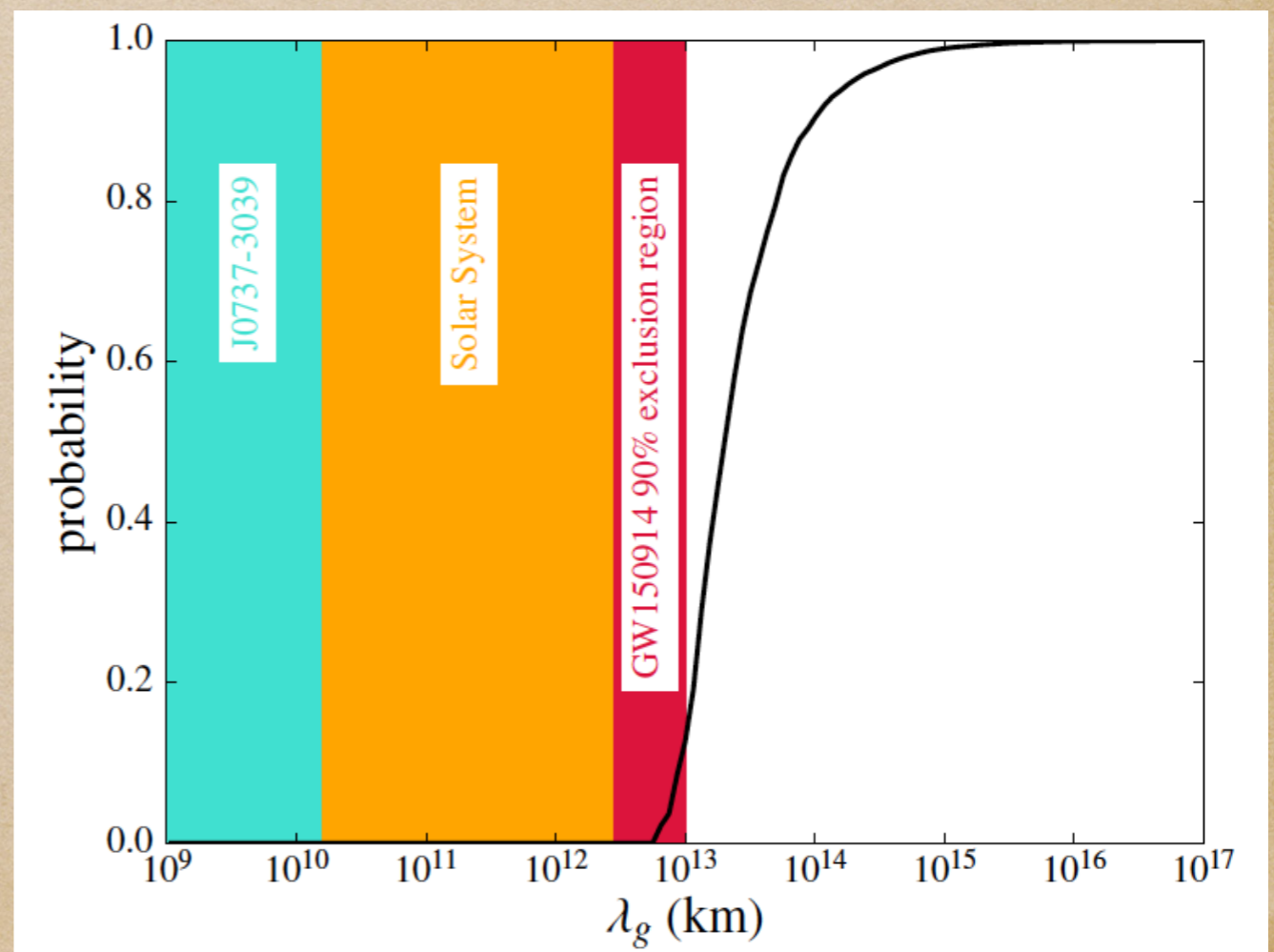
$\Rightarrow$  Quasi-1PN phase term

$$\phi_{\text{MG}}(f) = -\frac{\pi D c}{\lambda_g^2 (1+z) f}$$

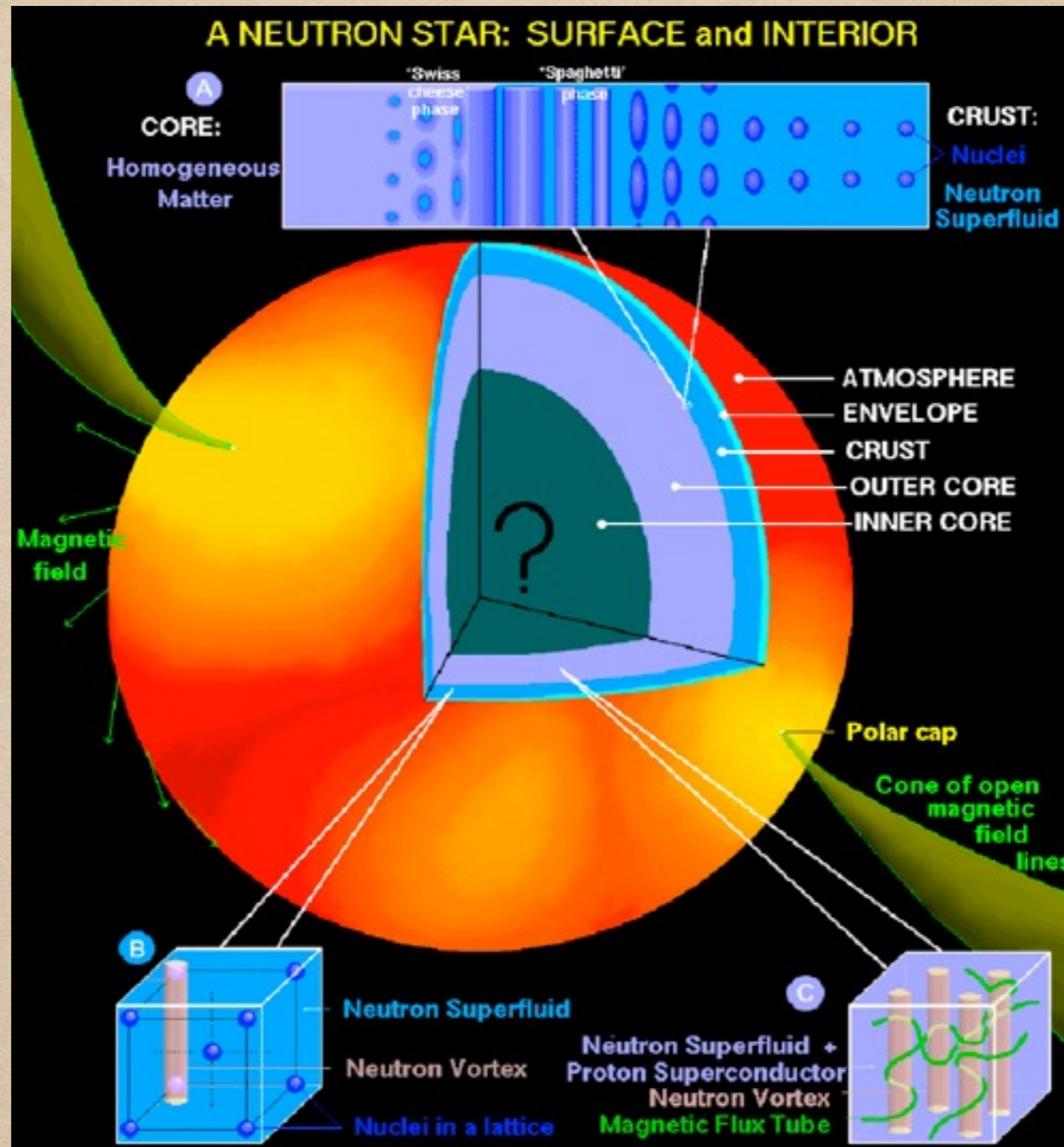
Will 1998 PRD

$$m_g \leq 1.2 \times 10^{-22} \text{ eV}/c^2$$

Abbott et al 1602.03841



# Equation of state of matter



- E.g. through tidal effects

# Cosmological distance ladder

## The Cosmic Distance Ladder

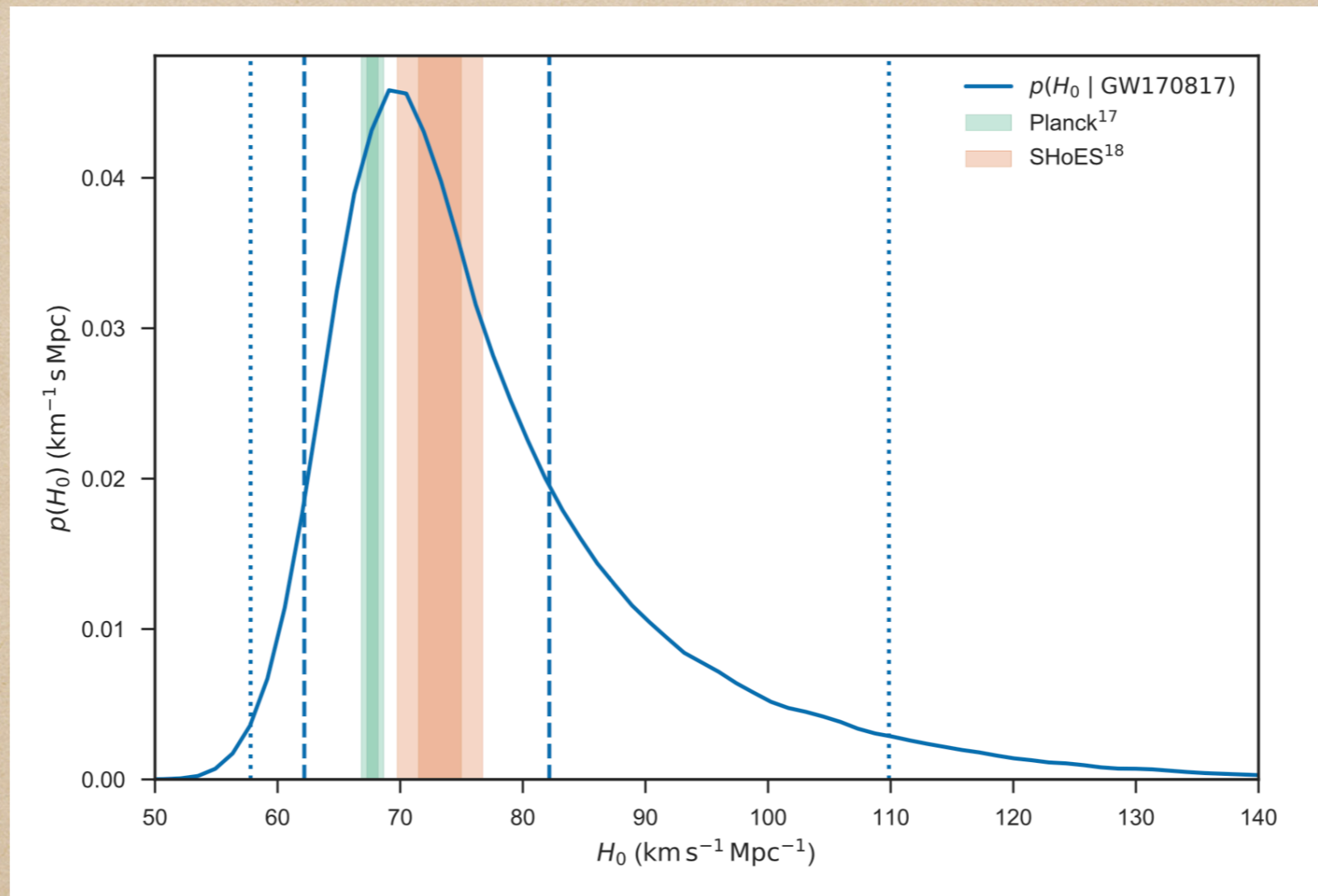
How do astronomers measure the distance to celestial bodies?

Presented by: Ross Dubois

- Need electromagnetic counterpart or large number of events !

# Standard Sirens: $H_0$ from GW170817

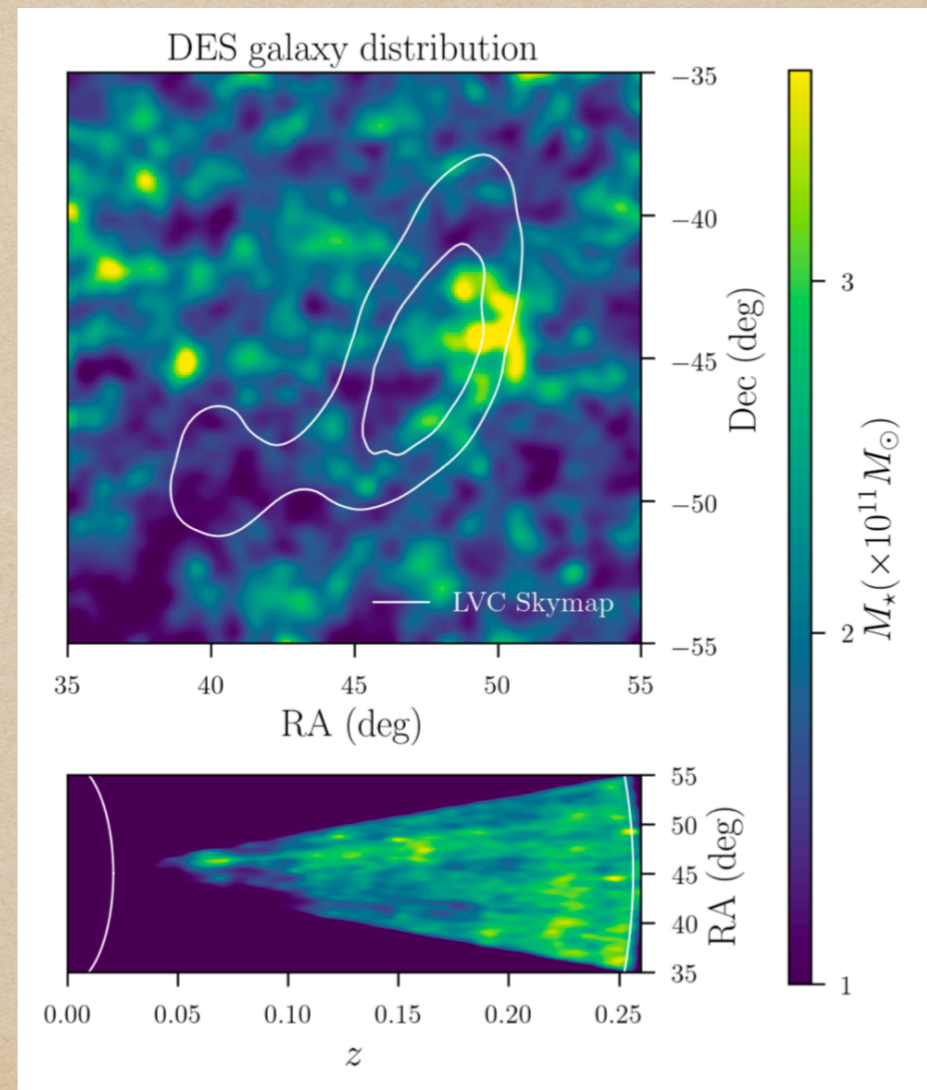
Abbott et al 1710.05835



- Redshift  $z$  from EM, Luminosity distance  $D_L$  from GWs
- $H_0 = 70_{-8.0}^{+12.0} \text{ km s}^{-1} \text{ Mpc}^{-1}$
- More sirens needed to resolve tension

# Dark Sirens: $H_0$ from BH binaries

- No EM signal  $\Rightarrow$  redshift unknown
- Solution: Statistical analysis using galaxies in sky window
- Combine sky localization from LIGO with galaxy surveys
- Here for GW170814
  - Prather well localized!
  - Dark Energy Survey "DES"
  - Not yet competitive, but will improve with many events



Soares-Santos et al 1901.01540



# Conclusions

# Conclusions

- GW150914 marks the dawn of GW astronomy
- “We” measured the change in length by a fraction of an atomic nucleus caused by sth. 1 Gyr away!
- >1 BBH! Not merely a lucky shot.
- First surprises: BHs heavier than expected GW190521  
Compact objects in the mass gap GW190814
- GW170817 marks the dawn of multi messenger astronomy!
- Applications: Test GR, BH census, History of universe, EOS,...
- A new window to the universe reveals interesting things...



# GW detections as of 2020

