

---

# How to Mimic a Cosmic Superstring

---

David Tong



hep-th/0506022 (JCAP) with Koji Hashimoto  
+ work in progress

Copenhagen, April 2006

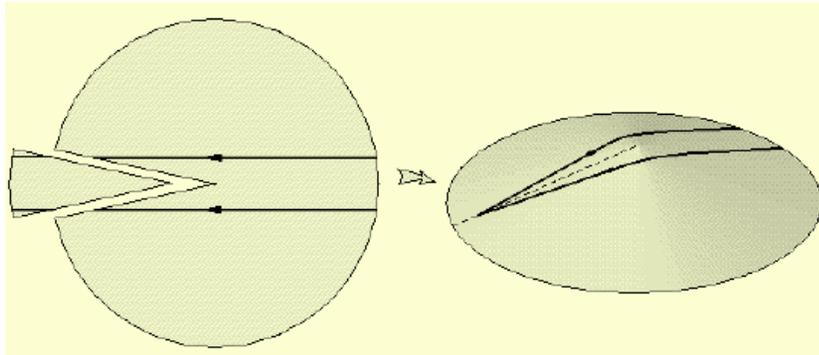
# Motivations

- Cosmic Strings stretch across the Heavens
  - both across the horizon
  - and in loops measured in astronomical units (lightdays +)
- They have the width of elementary particles, but are very dense and very long

$$G\mu \leq 10^{-7}$$

- They have not been observed. They are not predicted by any established law of physics...
  - But they are a robust prediction of many theories beyond the standard model. They would provide a window onto new microscopic physics that is not accessible in terrestrial experiments.

# Observation by Lensing

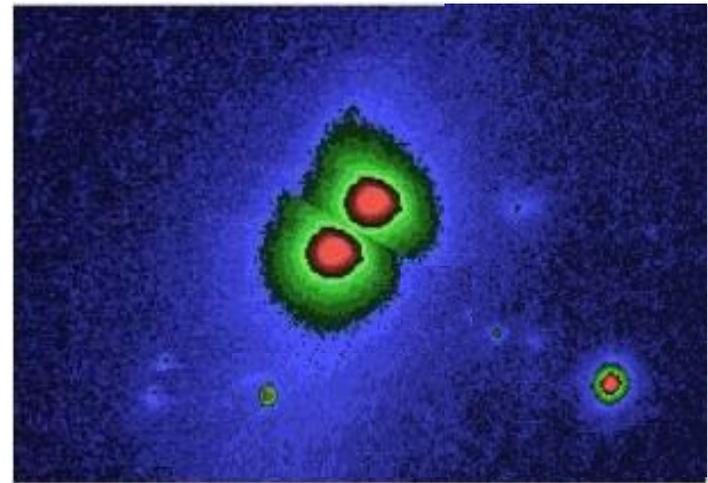


Cosmic strings leave a conical deficit angle in space

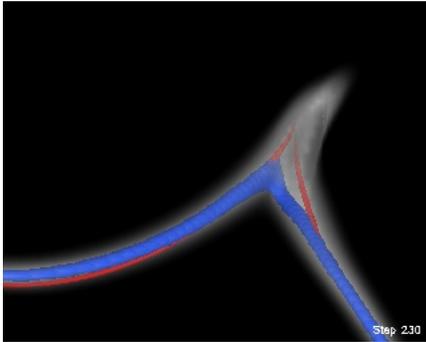
$$\delta = 8\pi G\mu$$

This gives rise to a distinctive lensing signature in the sky.

(Vilenkin '81)



# Observation by Gravitational Waves



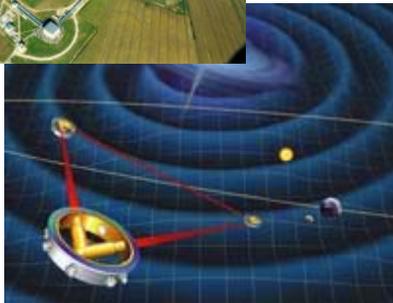
Cusps in string loops emit an intense burst of gravitational radiation in the direction of the string motion.

(Damour and Vilenkin '01)

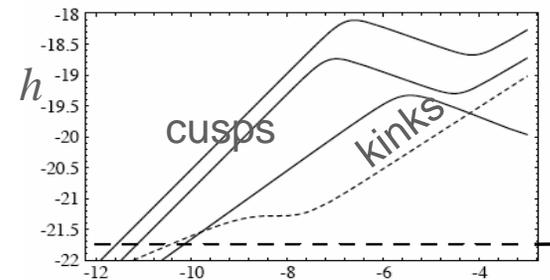
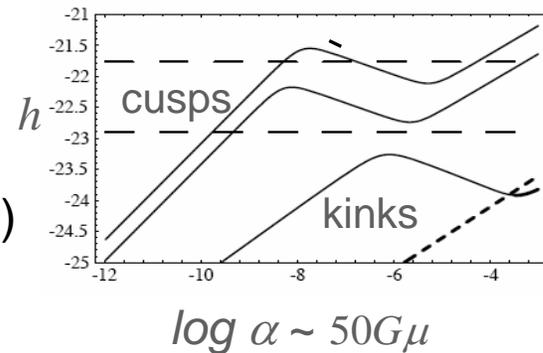
(Olum)



LIGO 1 (online) and  
Advanced LIGO (2009)



LISA (2015?)



---

# Cosmic Superstrings

- Could cosmic strings be fundamental strings stretched across the sky?
    - First proposed by **Witten** in 1985 in heterotic string theory.
    - The strings are too heavy and unstable.
  - Revisited in type IIB flux compactifications.  
(**Tye et al, Copeland, Myers and Polchinski**)
    - Strings live down a warped throat, ensuring they have a lowered tension.
    - Strings can be stable.
    - Strings naturally produced during reheating after brane inflation.
-

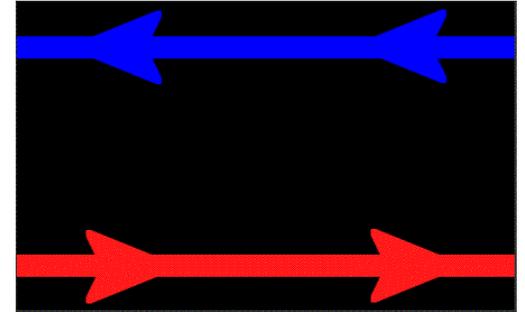
---

# Smoking Superstring Guns

- Suppose we discover a cosmic string network in the sky. Do we have evidence for string theory? Or merely for the abelian Higgs model?
  - There are two features which may distinguish superstrings from simple semi-classical solitons
    - Reconnection probability
    - $(p,q)$  string webs
  - Let's look at each of these in turn....
-

# Reconnection

- When two strings intersect, reconnection swaps partners, leaving behind kinks.
- When a single string self-intersects, reconnection cuts off a loop.

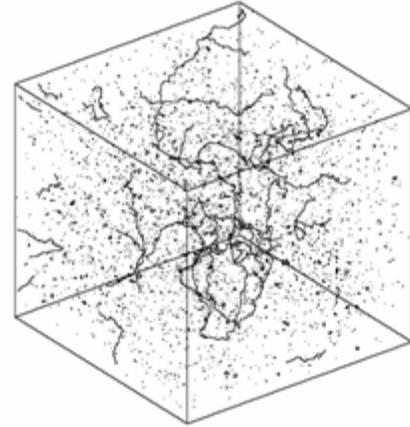


- Abelian vortices reconnect with probability  $P = 1$
- Superstrings intersect with probability  $P \sim g_s^2$   
The full angle and velocity dependence was computed by [Jackson, Jones and Polchinski '04](#).

The probability  $P$  is potentially observable

# Effects of Reduced Reconnection

The evolution of a string network leads to a “scaling solution”, with a few strings stretched across the horizon, together with loops of many sizes. The properties of this solution depend only on  $G\mu$  and  $P$ .



Allen and Shellard (1990)

As the universe expands:

- more of the stretched strings are revealed,
- the loops decay through gravitational radiation.

Reduced probability of reconnection means:

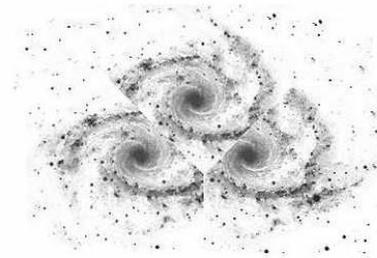
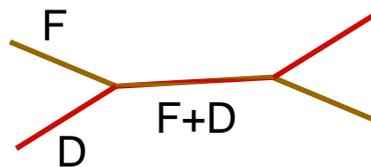
- Fewer kinks
- Fewer loops, and hence more string:  $N \sim 1/P$
- Better chance to see strings.

# (p,q) String Webs

- The spectrum of IIB string theory includes
  - Fundamental strings, with tension  $\mu_F \sim 1/\alpha'$
  - D-Strings, with tension  $\mu_D \sim \mu_F/g_s$
  - Bound states of (p,q) strings with tension

$$\mu_{(p,q)} = \sqrt{p^2 \mu_F^2 + q^2 \mu_D^2}$$

Bound states means 3-string junctions, with angles determined by tensions



Schlaer and Wyman '06

---

# Smoking Superstring Guns?

Can we cook up a simple field theory model which mimics the cosmic superstring?

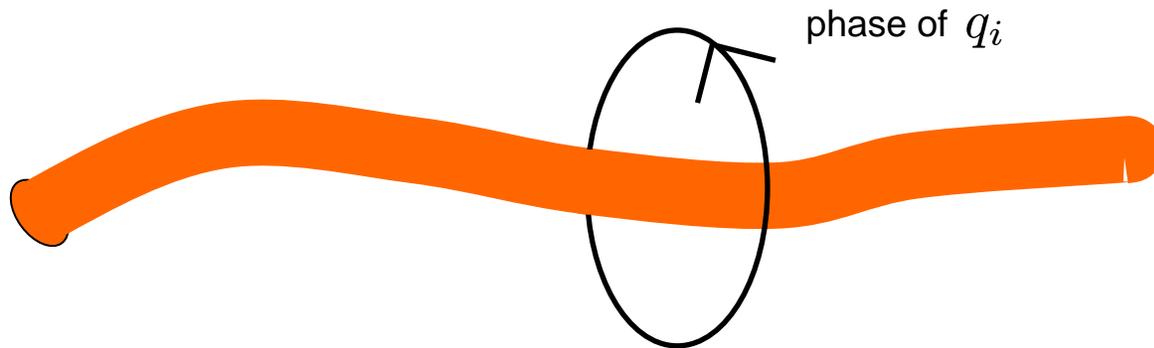
For example: flux tubes in  $SU(N)$  Yang-Mills have probability of reconnection  $P \sim 1/N^2$

---

# The Abelian Higgs Model

$$L = \frac{1}{4e^2} F_{\mu\nu} F^{\mu\nu} + |\mathcal{D}q|^2 - \frac{\lambda e^2}{2} (|q|^2 - v^2)^2$$

Broken U(1) gauge symmetry  $\longrightarrow$  vortices

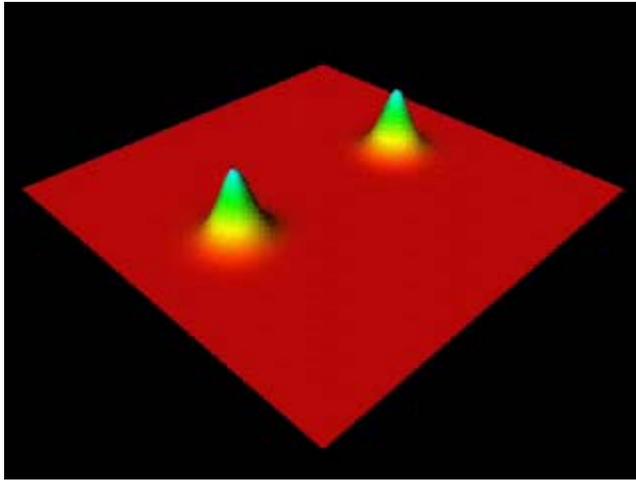


$$\mu = 2\pi v^2 f(\lambda)$$

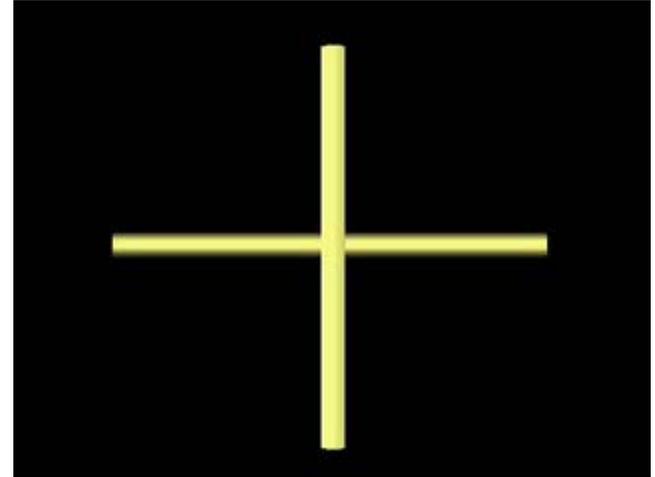
Nielsen and Olesen, '73

# Reconnection

The reconnection of cosmic strings follows from classical field equations. In general this requires numerical work. [Matzner](#)



[Moore and Shellard](#)



[Battye and Shellard](#)

The key to reconnection is the right angle scattering of vortices.

# Reconnection at Small Velocity

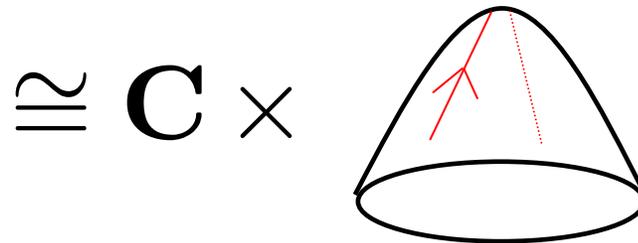
For strings intersecting at small velocity, and with small angle of incidence, one can use the moduli space (or adiabatic) approx.

(Copeland and Turok)

$$\mathcal{M}_{2-vortex} \cong \mathbb{C} \times \mathbb{C}/\mathbf{Z}_2$$

center of mass      relative separation

← identical particles



right angle scattering



reconnection

# Non-Abelian Higgs Model

Consider  $U(N_c)$  gauge group with  $N_f$  fundamental scalars

$$L = \frac{1}{4e^2} \text{Tr} F_{\mu\nu} F^{\mu\nu} + \sum_{i=1}^{N_f} |\mathcal{D}_\mu q_i|^2 - \frac{\lambda e^2}{2} \text{Tr} (\sum_{i=1}^{N_f} q_i \otimes q_i^\dagger - v^2)^2$$

The simplest model has  $N_c = N_f$ . The vacuum is  $q_i^a = v \delta_i^a$   
(where  $a = 1, \dots, N_c$  and  $i = 1, \dots, N_f$ )

$$q \rightarrow U q V^\dagger \quad \longrightarrow \quad U(N_c) \times SU(N_f) \rightarrow SU(N)_{\text{diag}}$$

↑                    ↑  
gauge                flavor

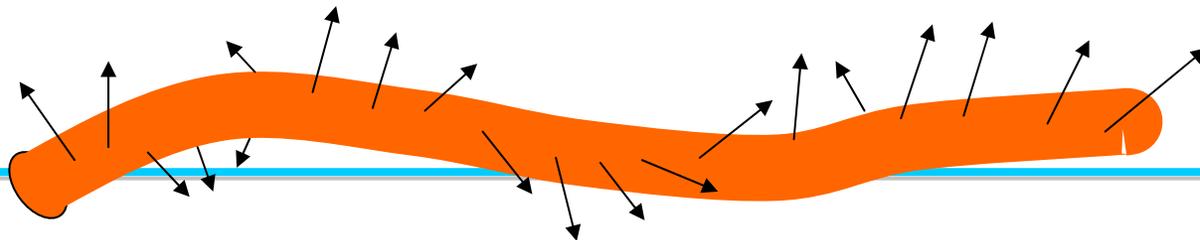
# Non-Abelian Vortices

Suppose we have an abelian vortex solution  $B_\star, q_\star$ . We can trivially embed this in the non-abelian theory.

$$B = \begin{pmatrix} B_\star & 0 & \dots & 0 \\ & \ddots & & \\ & & \ddots & \\ & & & 0 \end{pmatrix} \quad q = \begin{pmatrix} q_\star & v & \dots & \\ & \ddots & & \\ & & \ddots & \\ & & & v \end{pmatrix}$$

Different embeddings  $\longrightarrow$  internal degrees of freedom for single vortex

$$SU(N)_{\text{diag}} / SU(N-1) \times U(1) \cong \mathbf{CP}^{N-1}$$



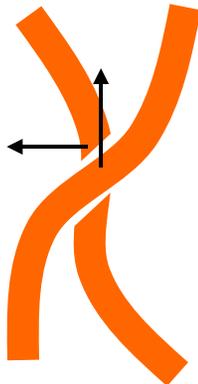
# Simple Idea:

Hashimoto and Tong

The strings can miss each other in the internal space.



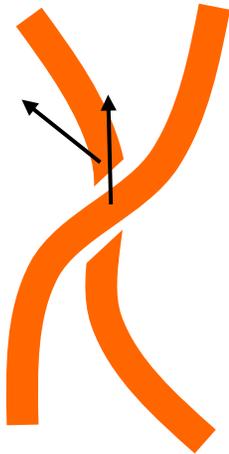
Same orientation → Live in same  $U(1)$  subgroup  
→ Reconnect



Opposite orientation → Don't see each other  
→ Don't reconnect

# Probability of Reconnection

What happens for intermediate angles?



Expectation: there exists a critical angle

$\theta < \theta_c$  → Reconnect

$\theta > \theta_c$  → Miss each other

Coarse graining over  $\theta$  could then give probability  $P < 1$ .

What really happens:  $\theta_c = \frac{\pi}{2}$  → Always reconnect except for finely tuned initial conditions.

→  $P=1$  !!!!

# But...

There are two subtleties

## ■ Quantum Effects

- In  $d=1+1$ , the groundstate wavefunction smears over the string.
- Massless spin waves get a mass  $\Lambda \sim ev \exp(-4\pi/e^2 N)$
- We can't even fine tune!

## ■ Fermion Zero Modes

- Charged fermions in four dimensions induce massless fermionic excitations on the string
- These change the quantum physics considerably...

# Effects of Fermions

- Consider adding the following fermion coupling in four dimensions.

$$L_{\text{Yuk}} = \sum_{i=1}^{N_f} \bar{\psi}_i \lambda q_i$$

fundamental                  adjoint



- This gives rise to fermion zero modes  $\chi_i$  on the cosmic string
- The axial symmetry  $\chi_i \rightarrow e^{i\beta\gamma_5} \chi_i$  is anomalous:  $U(1) \rightarrow Z_{2N}$
- A condensate forms on the string  $\langle \chi\chi \rangle \sim \Lambda$ , breaking  $Z_{2N} \rightarrow Z_2$
- This means that the cosmic string has  $N$  ground states.

# The Punchline

- The presence of fermi zero modes cause the vortex to have  $N$  quantum ground states
- These are identified with the string sitting in the  $N$  different diagonal components of the gauge group
- The strings reconnect in the same state, and pass through each other in different states.
  - At energies  $E \ll \Lambda$  we have  $N$  types of string, and  $P=1/N$ .
  - At energies  $E \gg \Lambda$  we have  $P=1$ .

# (p,q) Strings in Field Theory

Unpublished work with Matt Strassler  
and Mark Jackson.

- Making strings bind isn't hard...the difficult part is getting the right tension formula  $\mu_{(p,q)} = \sqrt{p^2 \mu_F^2 + q^2 \mu_D^2}$  (e.g. Saffin)
- Two hopeful possibilities
  - Binding of Electric Fluxes and Magnetic Fluxes
  - Binding different magnetic flux tubes (F-term and D-term vortices)

# Electric and Magnetic Fluxes

- Consider  $SU(N)$  theories with adjoint matter
  - Higgs phase has  $Z_N$  magnetic flux tubes; electric charge screened
  - Confining phase has  $Z_N$  electric flux tubes; magnetic charge screened
- Need more exotic phases. 't Hooft showed that phases of  $SU(N)$  are characterized by dimension  $N$  subgroup of the lattice  $Z_N \times Z_N$ 
  - e.g. Take  $N=pq$  and a symmetry breaking such that  $SU(N) \rightarrow SU(p)$   
This has  $Z_q$  magnetic strings and  $Z_p$  electric strings.
  - Big Question: Do the strings bind?! What is their energy? (Can we use S-duality e.g. in  $N=1^*$  theory?)

# Magnetic and Magnetic Fluxes

- Vortex flux tubes come in two different types
  - D-term:  $D = |q|^2 - |\tilde{q}|^2 - \zeta$  is real. Vortices are BPS in both N=1 and N=2 susy theories
  - F-term:  $F = \tilde{q}q - \xi$  is complex. Vortices are BPS in N=2 susy theories, but non-BPS in N=1 susy theories.
- Consider  $U(1)^k$  theories. What is binding energy between F- and D-term vortices? Bogomolnyi bound gives

$$\mu_{(p,q)} \geq \sqrt{|p\mu_F|^2 + q^2\mu_D^2}$$

- But: There are no solutions saturating the bound!

---

# Conclusions

- We've seen
    - Semi-classical strings that have an effective, velocity-dependent  $P < 1$ .
    - Semi-classical strings that (almost) mimic the IIB string spectrum.
  - If a cosmic string network is discovered, the task of distinguishing between these models may become an experimental question.
-